

# Atomic Spectral Lines

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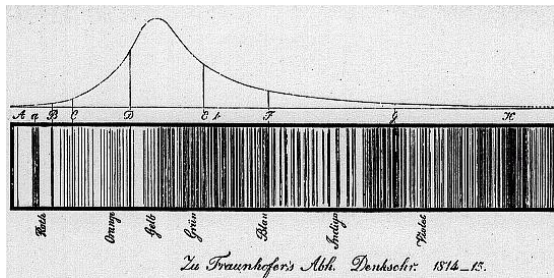


Hale COLLAGE, Boulder, Feb 18, 2016

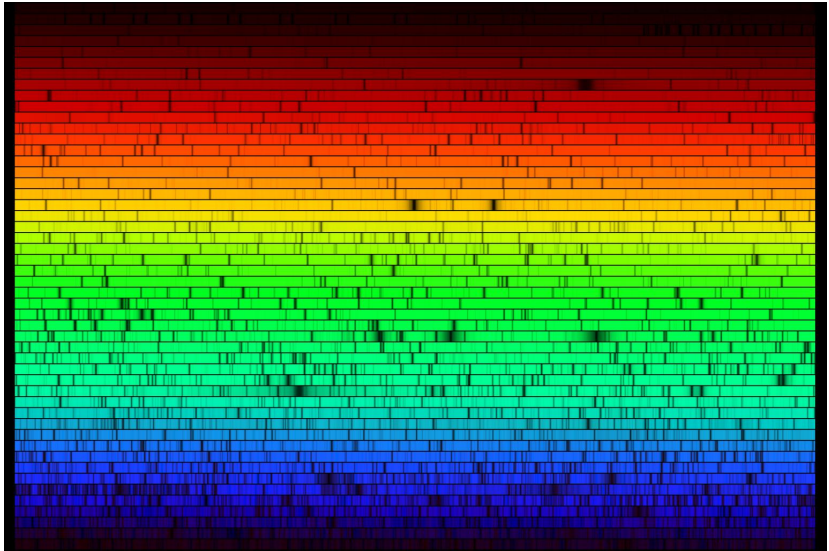
- How do we get absorption and emission lines in the spectrum?
- Atomic line- and continuum transitions
- Non-LTE radiative transfer in atomic models
- Real world examples:
  - Ca II H& K lines
  - He I 1083 nm line

# Some History

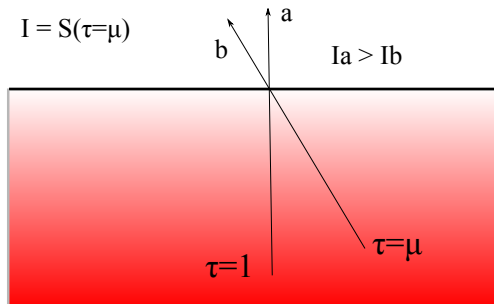
- **1802** Wollaston was the first to observe dark gaps in spectrum: spectral lines.
- **1814** Fraunhofer rediscovers lines. Assigns names that we still use, e.g., C ( $H\alpha$ ), D ( $Na I$ ), F ( $H\beta$ ), G (CH molecules), and H ( $Ca II$ ).



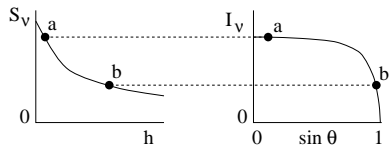
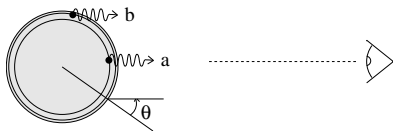
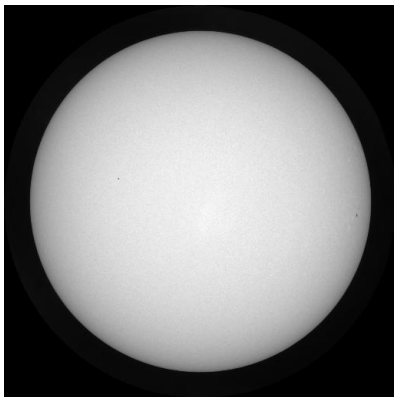
# The spectrum at much better resolution



# Remember: Eddington-Barbier approximation

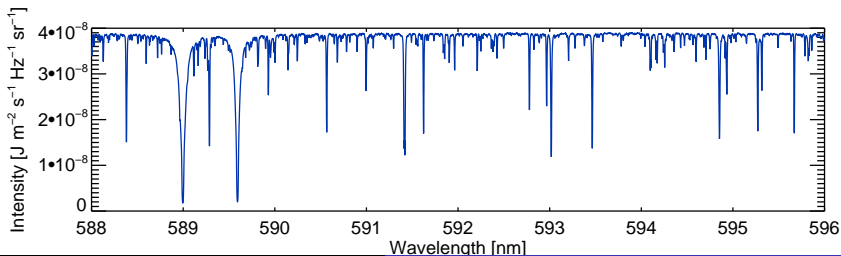
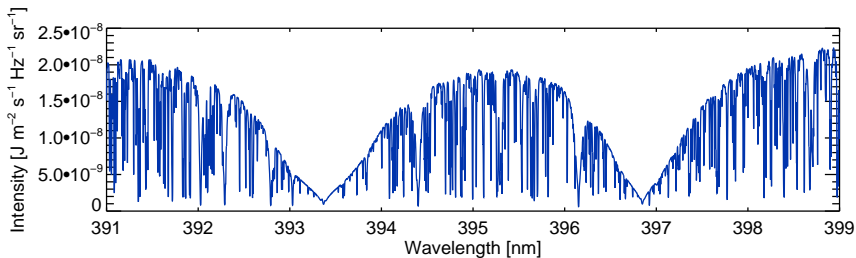


# Limb Darkening Explained

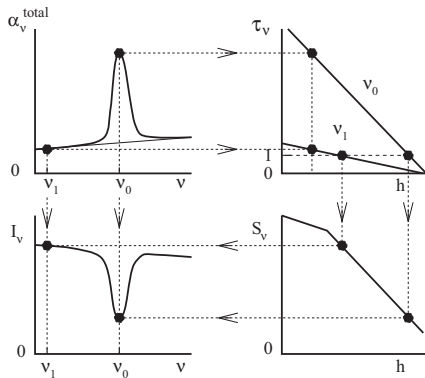


$$r/R = \sin \theta$$

# Can we now explain the Darkening in the Cores of Spectral Lines?

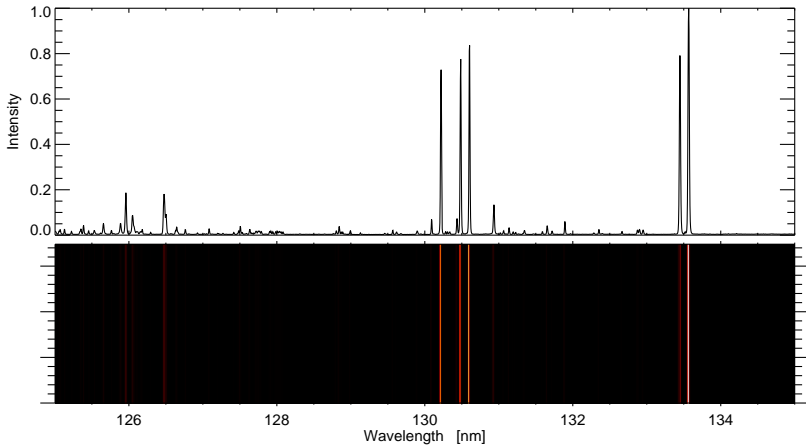


# Explanation of Absorption Lines in the Spectrum

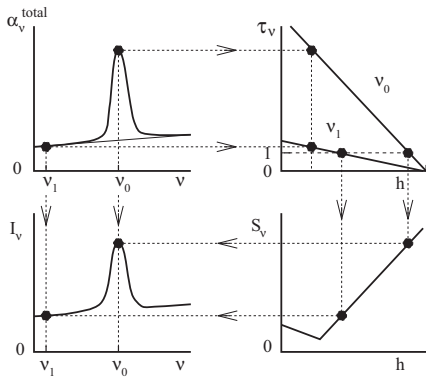




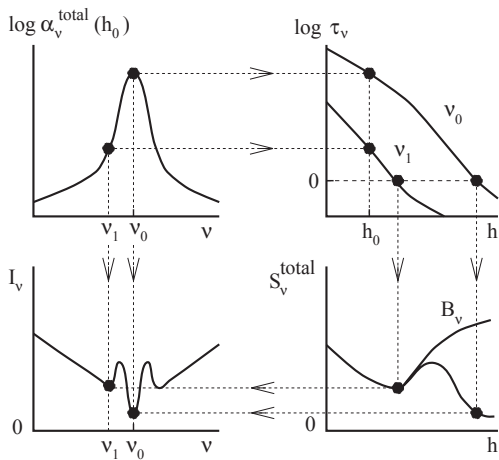
# In the UltraViolet the Spectral Lines are in Emission



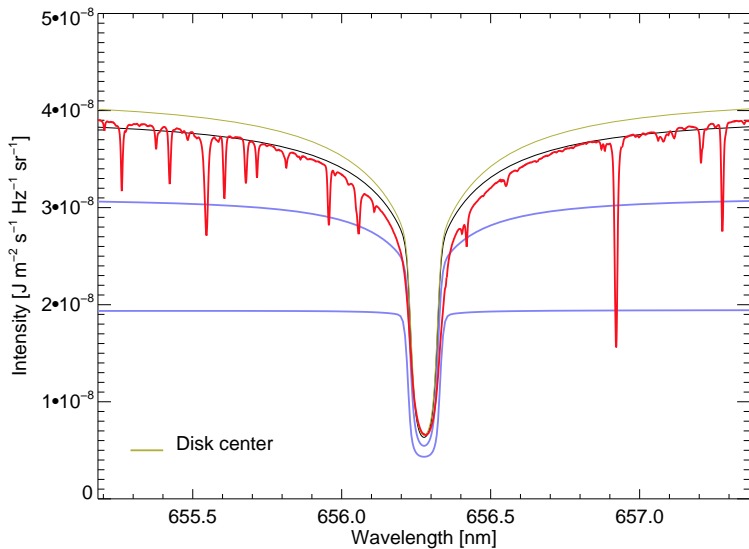
# Explanation of Emission in Spectral Lines



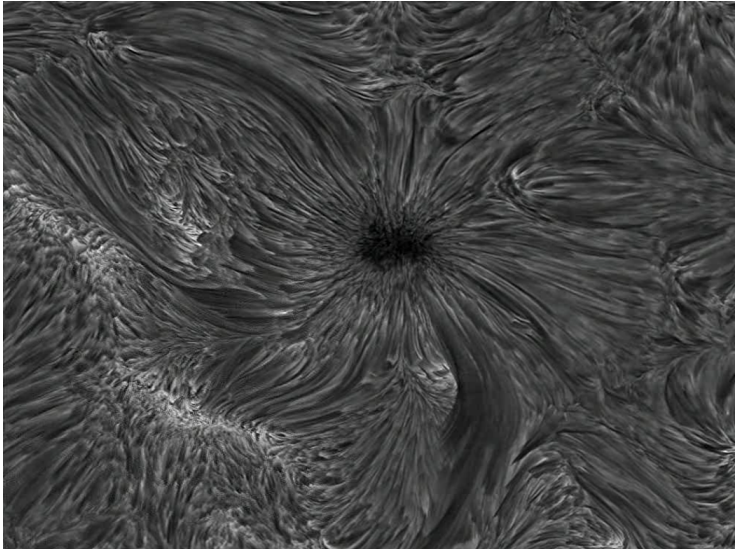
# Explanation of the Shape of the Call Resonance Lines



# H $\alpha$ Spectral Line

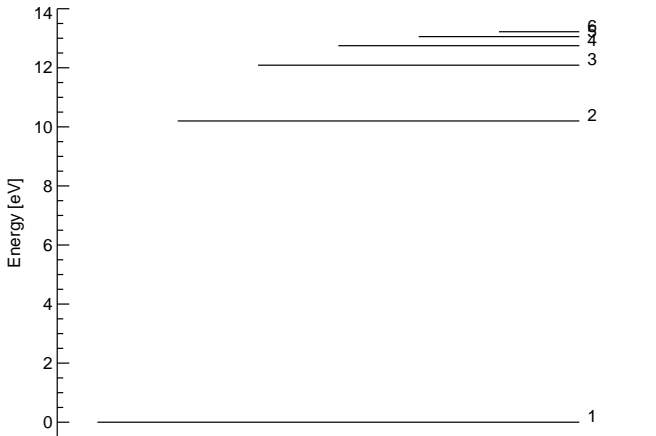


# Image of the Sun in the light of $H\alpha$



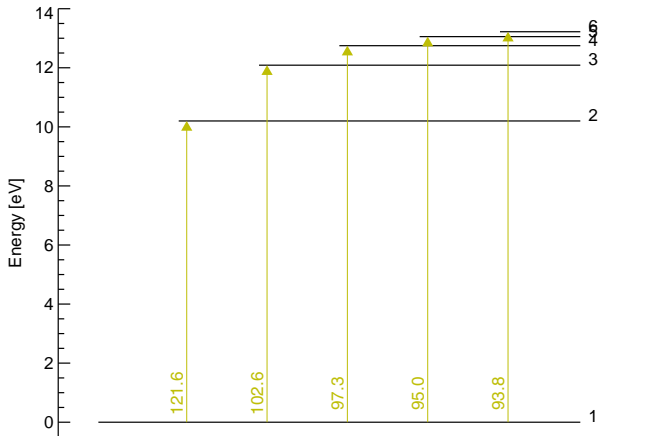
# Energy Levels and Transitions in Hydrogen Atom

$$\Delta E = h\nu = \frac{hc}{\lambda}$$



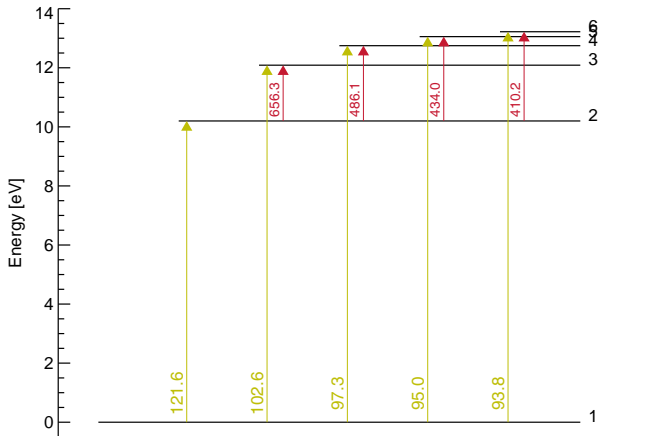
# Energy Levels and Transitions in Hydrogen Atom

$$\Delta E = h\nu = \frac{hc}{\lambda}$$



# Energy Levels and Transitions in Hydrogen Atom

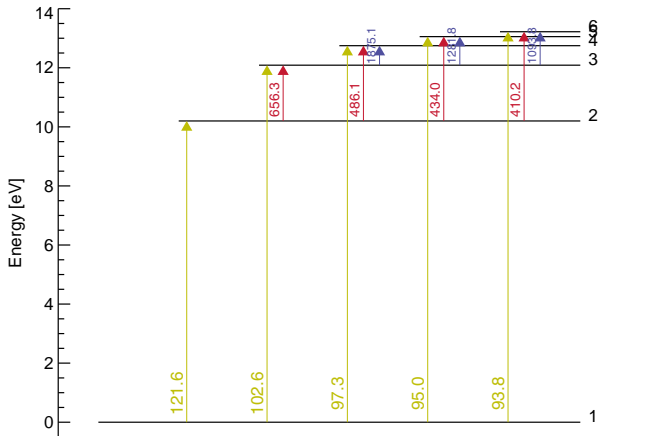
$$\Delta E = h\nu = \frac{hc}{\lambda}$$



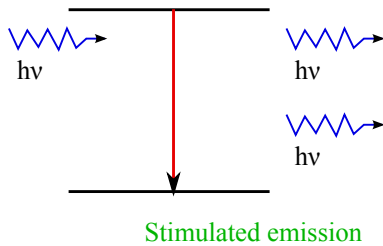
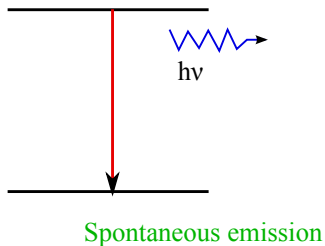
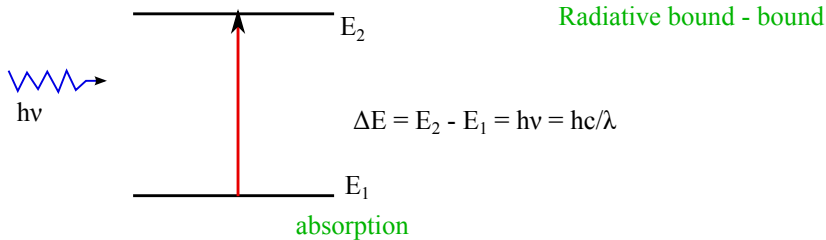


# Energy Levels and Transitions in Hydrogen Atom

$$\Delta E = h\nu = \frac{hc}{\lambda}$$

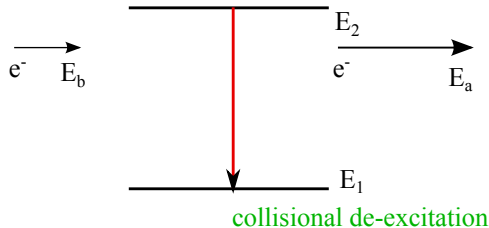
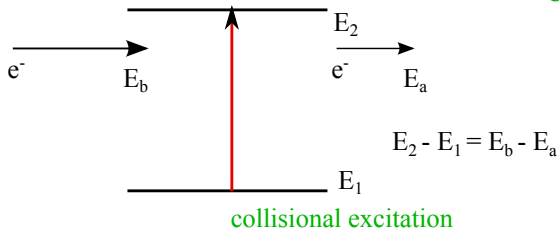


# Radiative bound-bound Transitions

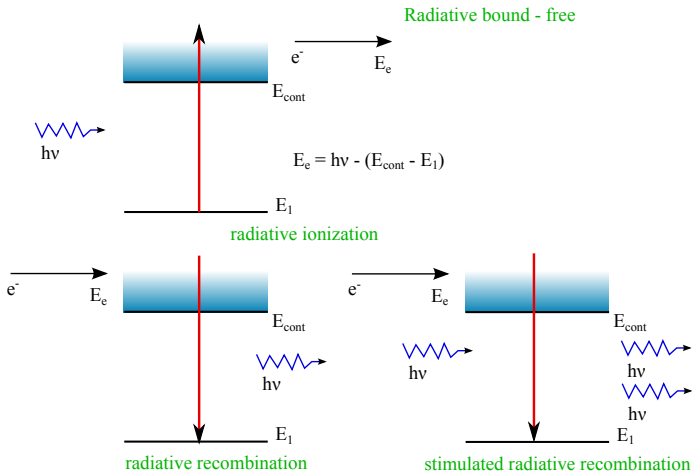


# Collisional bound-bound Transitions

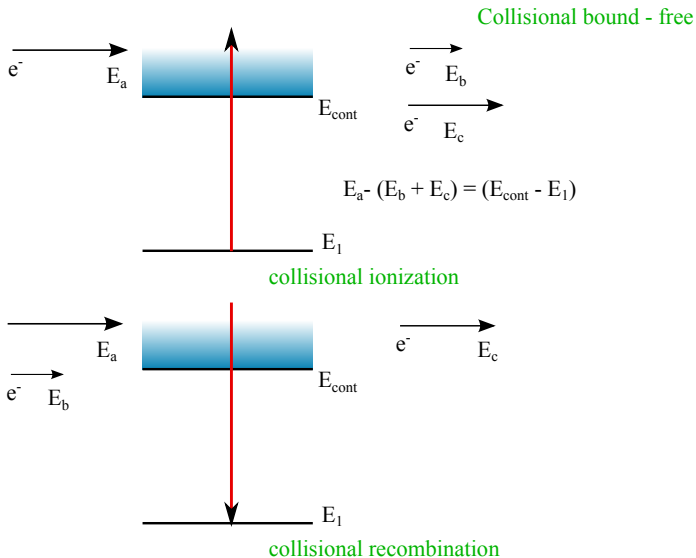
Collisional bound - bound



# Radiative bound-free Transitions



# Collisional bound-free Transitions



# Absorption and Emission Coefficients for bound-bound Transitions

Spontaneous emission  $j \rightarrow i$ :

$$j_{\nu}^{\text{spont}} = n_j (A_{ji} h\nu_{ij} / 4\pi) \phi_{\nu}$$

Stimulated emission  $j \rightarrow i$ :

$$j_{\nu}^{\text{stim}} = n_j (B_{ji} h\nu_{ij} / 4\pi) \phi_{\nu} I_{\nu}, \quad A_{ji} = (2h\nu^3 / c^2) B_{ji}$$

Absorption  $i \rightarrow j$ :

$$\alpha_{\nu} = n_i (B_{ij} h\nu_{ij} / 4\pi) \phi_{\nu}, \quad g_i B_{ij} = g_j B_{ji}$$

# Source Function of bound-bound Transition

## Transfer equation:

$$\begin{aligned}\frac{dl_\nu}{ds} &= j_\nu^{\text{spont}} + j_\nu^{\text{stim}} - \alpha_\nu l_\nu \\ &= n_j(A_{ji}h\nu_{ij}/4\pi)\phi_\nu - h\nu_{ij}/4\pi\phi_\nu(n_i B_{ij} - n_j B_{ji})l_\nu\end{aligned}$$

## Source function:

$$\begin{aligned}S_\nu &= \frac{j_\nu}{\alpha_\nu} = \frac{n_j A_{ji}}{n_i B_{ij} - n_j B_{ji}} \\ &= \frac{2h\nu_{ij}^3}{c^2} \frac{n_j}{g_j/g_i n_i - n_j} \\ &= (1 - \epsilon)\bar{J} + \epsilon B_\nu\end{aligned}$$

$$\epsilon \equiv \frac{C_{ji}}{C_{ji} + A_{ji} + B_{ji}\bar{J}}; \quad \bar{J} \equiv \int J_\nu \phi_\nu d\nu; \quad B_\nu \equiv \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/kT} - 1}$$

## Radiative excitation

$$\begin{aligned}R_{ij} &= B_{ij} \frac{h\nu}{4\pi} \int d\Omega \int \frac{d\nu}{h\nu} I_\nu \phi_\nu \\ &= B_{ij} \bar{J};\end{aligned}\quad \bar{J} \equiv \frac{1}{4\pi} \int d\Omega \int d\nu I_\nu \phi_\nu$$

## Radiative de-excitation

$$\begin{aligned}R_{ij} &= A_{ji} + B_{ji} \frac{h\nu}{4\pi} \int d\Omega \int \frac{d\nu}{h\nu} I_\nu \phi_\nu \\ &= A_{ji} + B_{ji} \bar{J}\end{aligned}$$

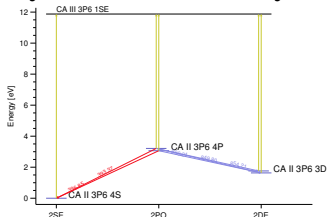


# Basic Equation: Statistical Equilibrium

Consider an atom (or molecule) with levels  $i = 0, \dots, N - 1$ .

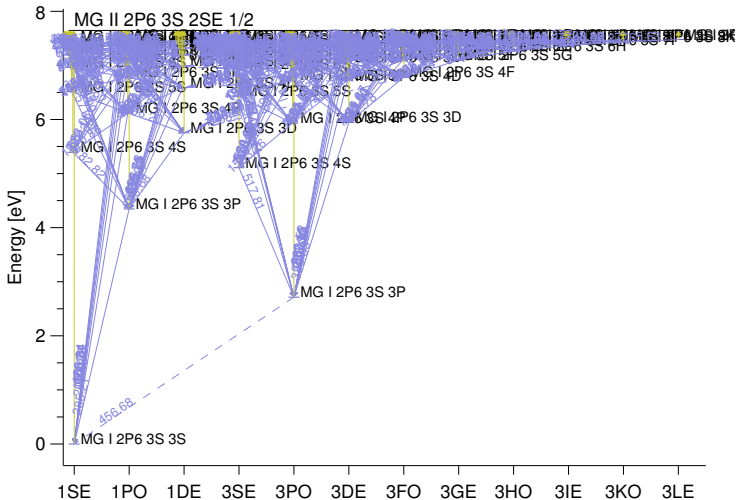
**Statistical equilibrium for level  $i$ :**

$$\sum_{j=0}^{N-1} n_j (C_{ji} + R_{ji}) = \sum_{j=0}^{N-1} n_i (C_{ij} + R_{ij})$$

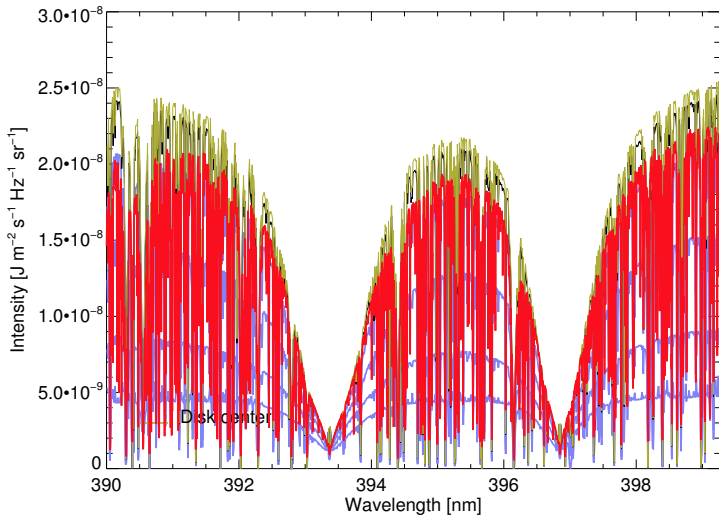


The set of equations for all levels forms a, generally **non-linear**, and **non-local**, set of equations for the population numbers  $n_i$

# Complicated Termdiagram for Magnesium



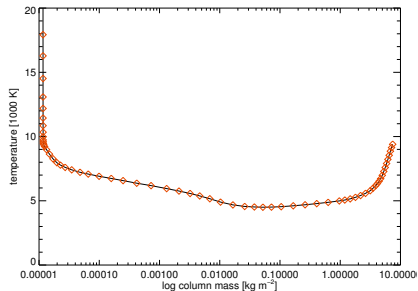
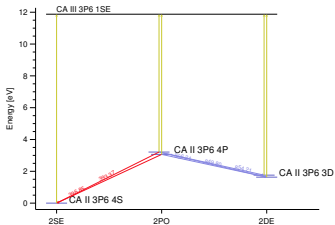
# We want to Reproduce the Spectrum of the Ca II H&K



# Ingredients for Reproducing the Ca II H&K spectrum

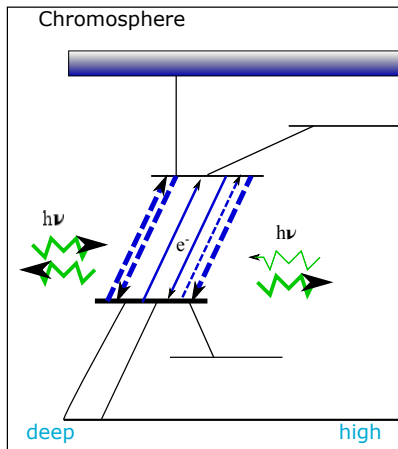
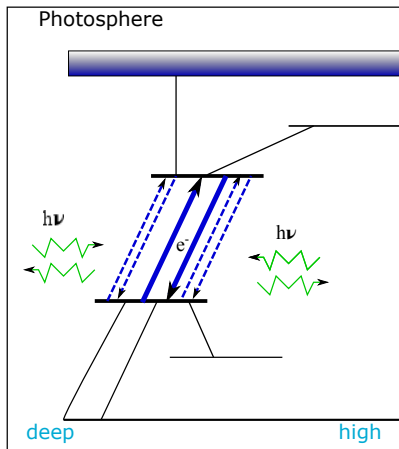
## Atmospheric Model:

## Atomic Model:

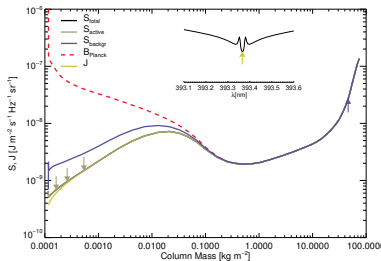
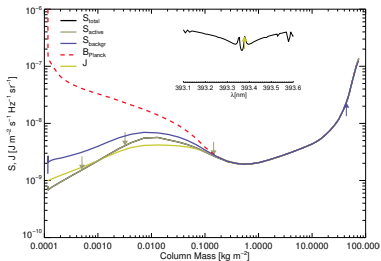
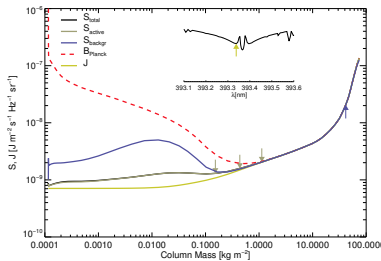
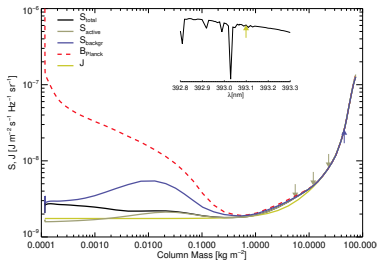


Solve Equations for **radiative transfer** and **statistical equilibrium** simultaneously.

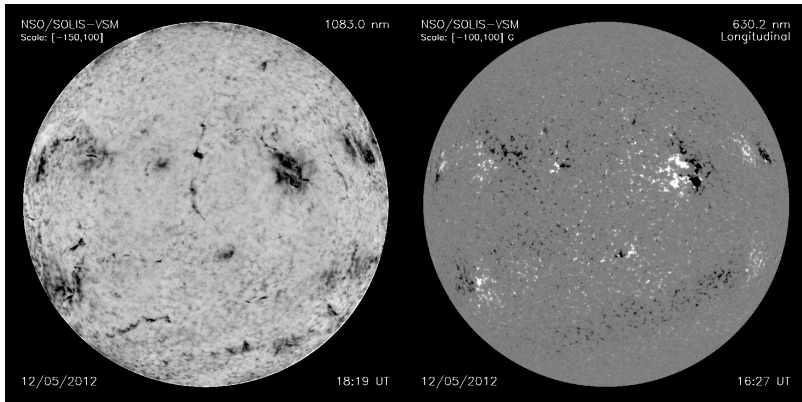
# Collisional and Radiative Excitation in a realistic Case



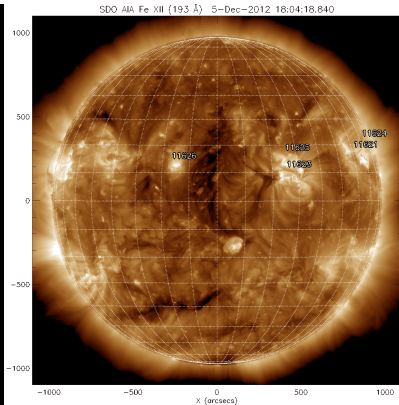
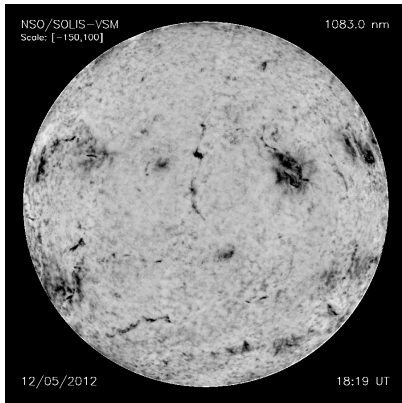
# Source function Ca II K line (Non-LTE)



# Full disk images of He I equivalent width and $B_{\parallel}$

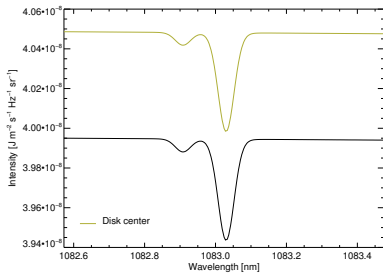
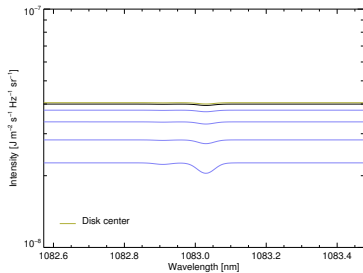


# Full disk images of He I EQW and Fe XII 19.3 nm

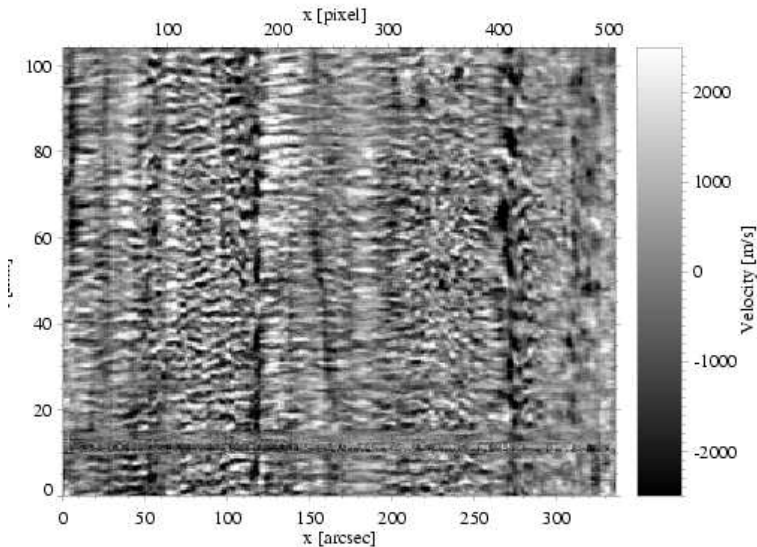




# Line profiles of the He I 1083 nm triplet

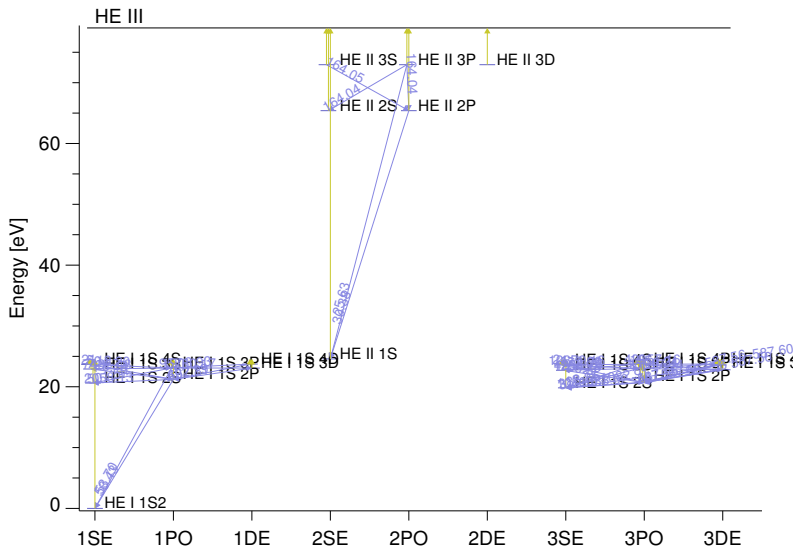


# The He I 1083.0 nm line: chromospheric?

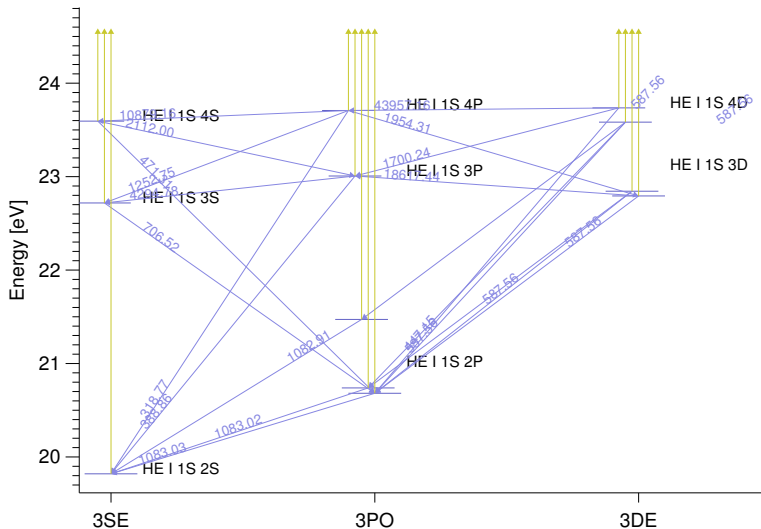


Courtesy Bernhard Fleck

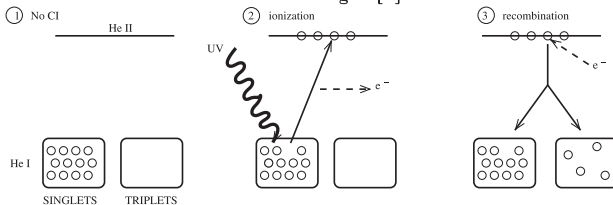
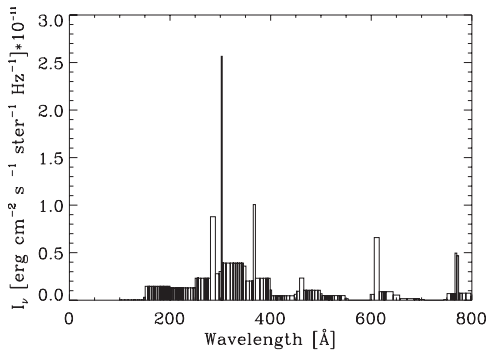
# The He I 1083.0 nm term diagram



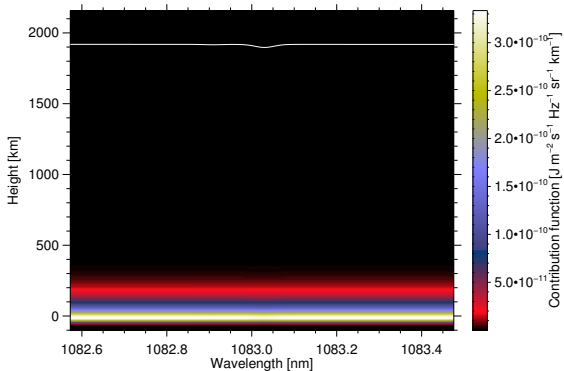
# The He I 1083.0 nm term diagram, triplet system



# EUV irradiation from Corona populates triplet levels



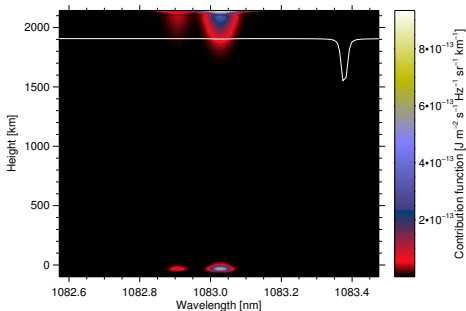
# The He I 1083.0 nm contribution function



Contribution function:

$$C \equiv S(\tau) e^{-\tau} \frac{d\tau}{dh}$$

# He I Line contribution function



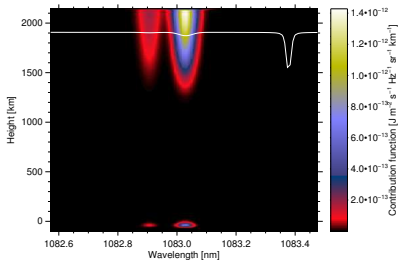
Line contribution function:

$$S_{\text{tot}} = \frac{(\eta_l + \eta_c)}{(\chi_l + \chi_c)}$$

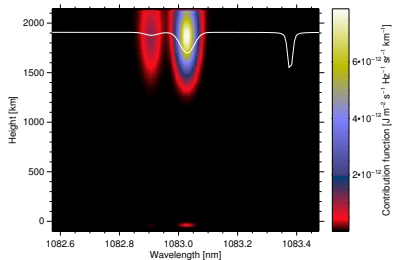
$$C = \left[ \frac{\eta_l}{(\chi_l + \chi_c)} + \frac{\eta_c}{(\chi_l + \chi_c)} \right] e^{-\tau} \frac{d\tau}{dh}$$

# He I Line contribution function with irradiation

1x



10x

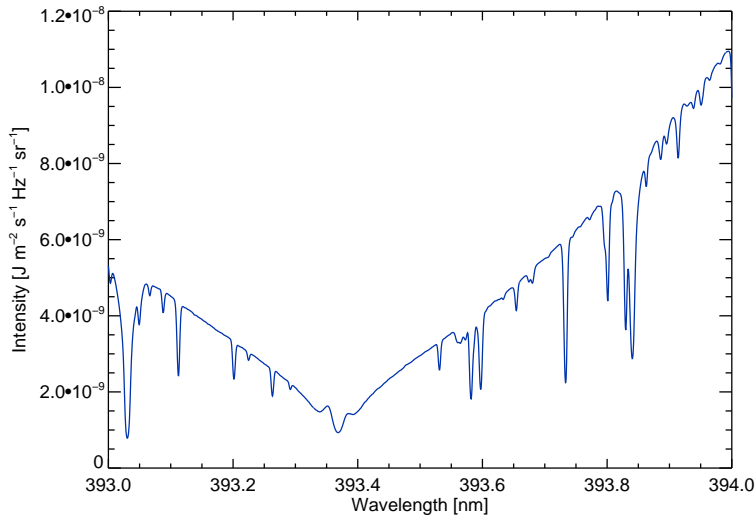




# Next lecture:

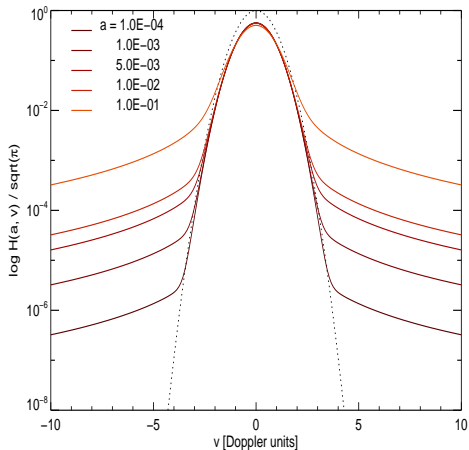
- Molecular line formation

# Details of the Call K line



Back

# Voigt Functions



$$\phi(\nu - \nu_0) = \frac{H(a, \nu)}{\sqrt{\pi} \Delta \nu_D}$$
$$\Delta \nu_D \equiv \frac{\nu_0}{c} \sqrt{\frac{2kT}{m}}$$
$$a = \frac{\Gamma}{4\pi \Delta \nu_D}$$

Back