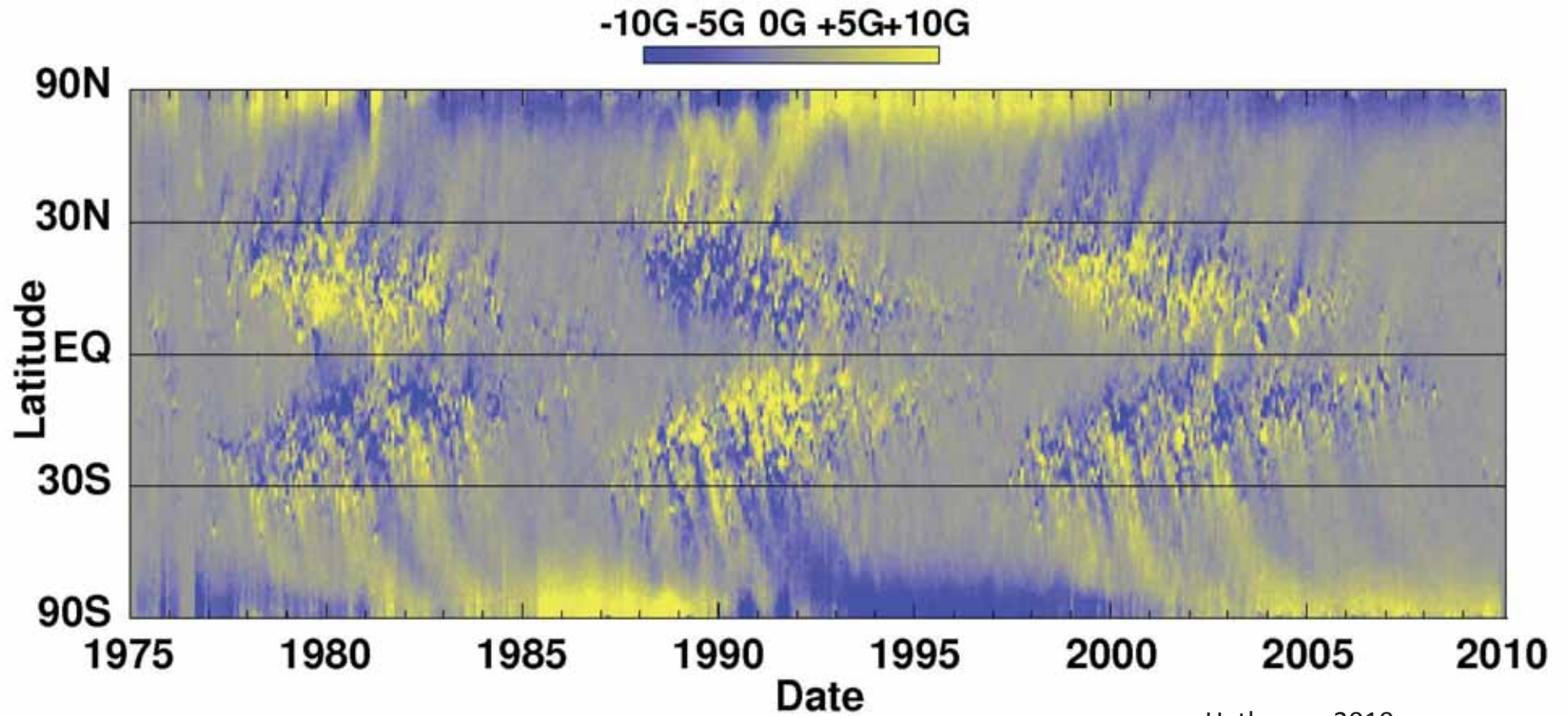


## Stellar Convection, Dynamos, & Intrigue

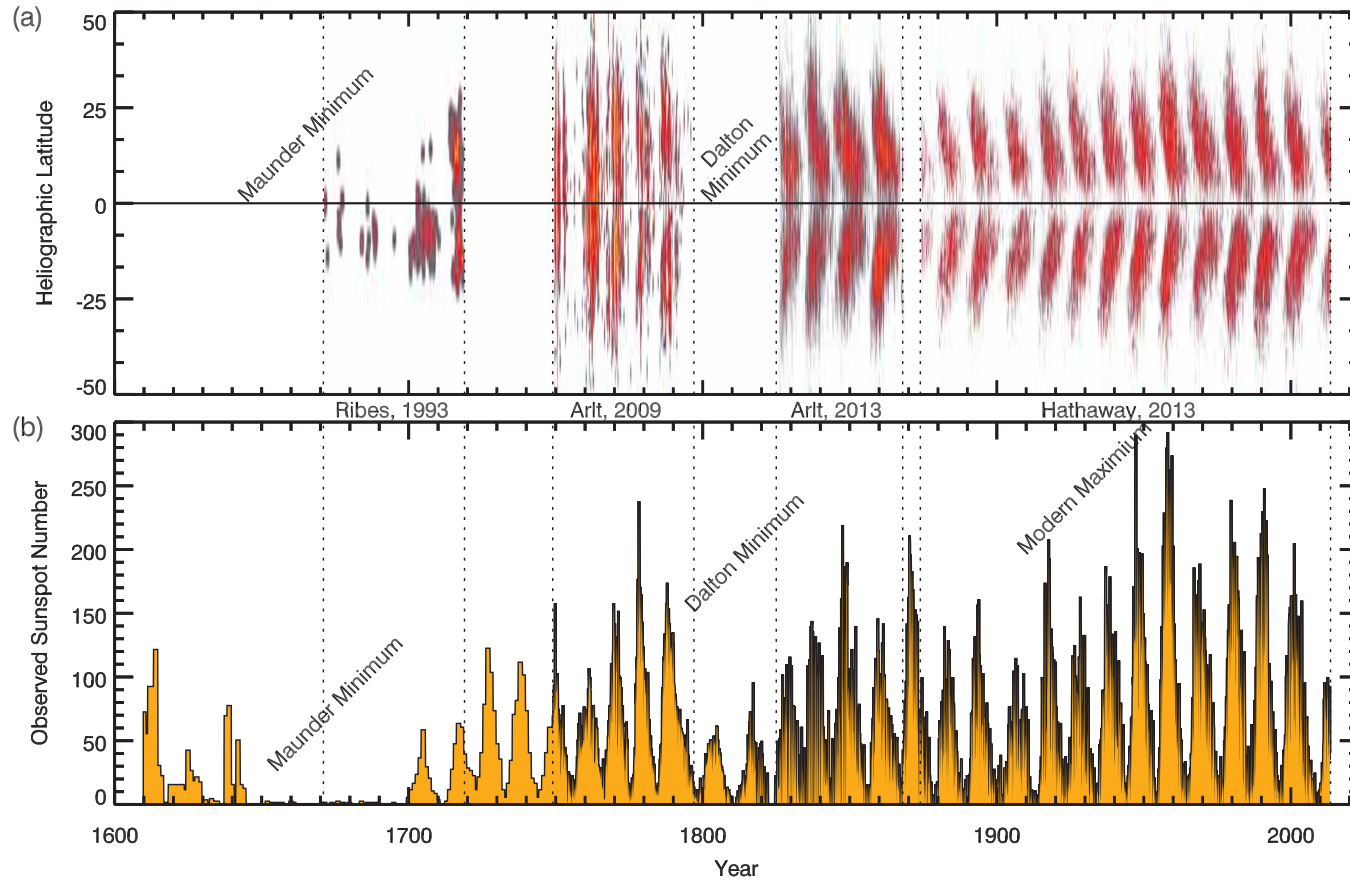
Kyle Augustson - NCAR ASP @ HAO  
Space Weather & Young Suns Workshop  
20 October 2014.

# Basic Aspects of Solar Magnetism

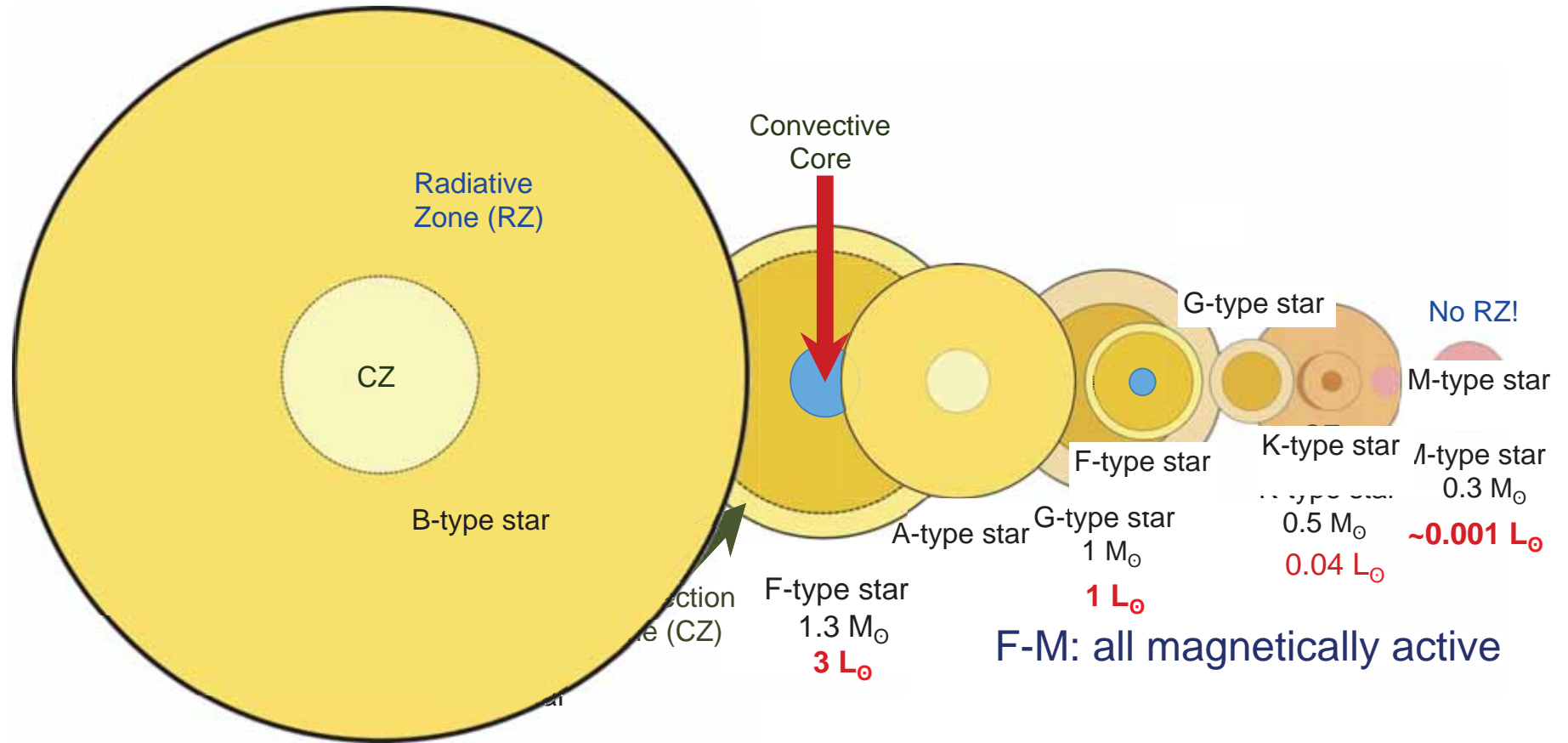


Hathaway 2010

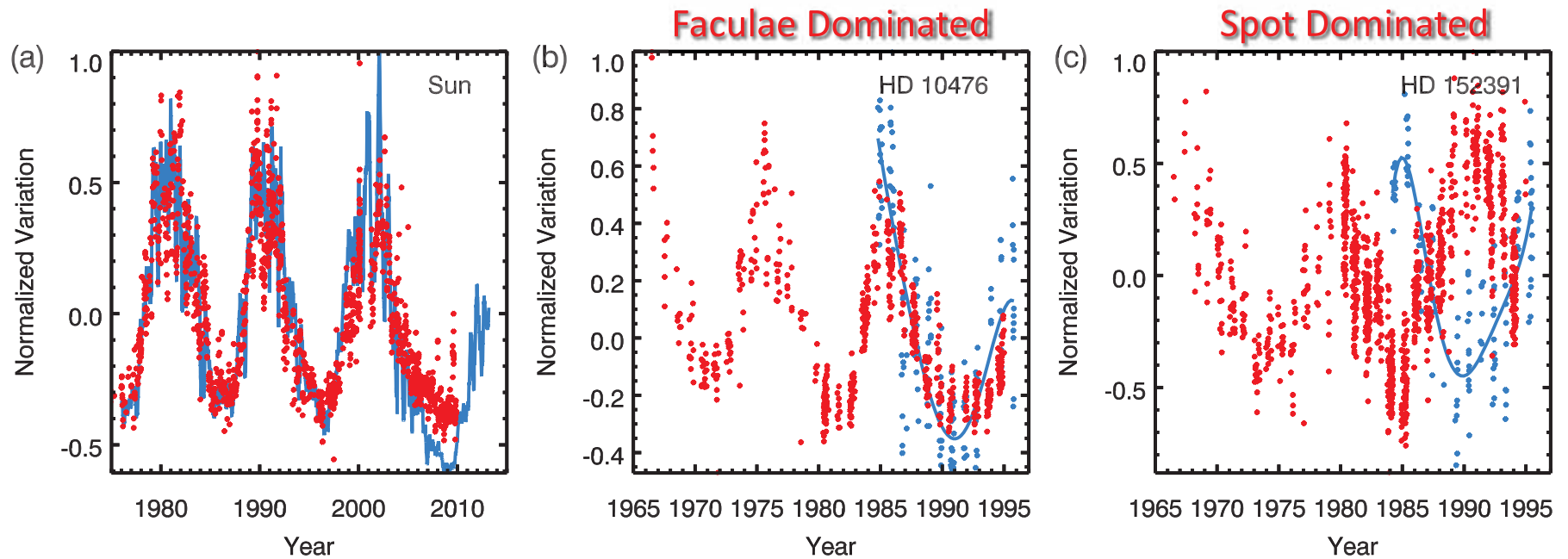
# Basic Aspects of Solar Magnetism



# Stellar Convection Zones



# Stellar Cycles & Magnetism



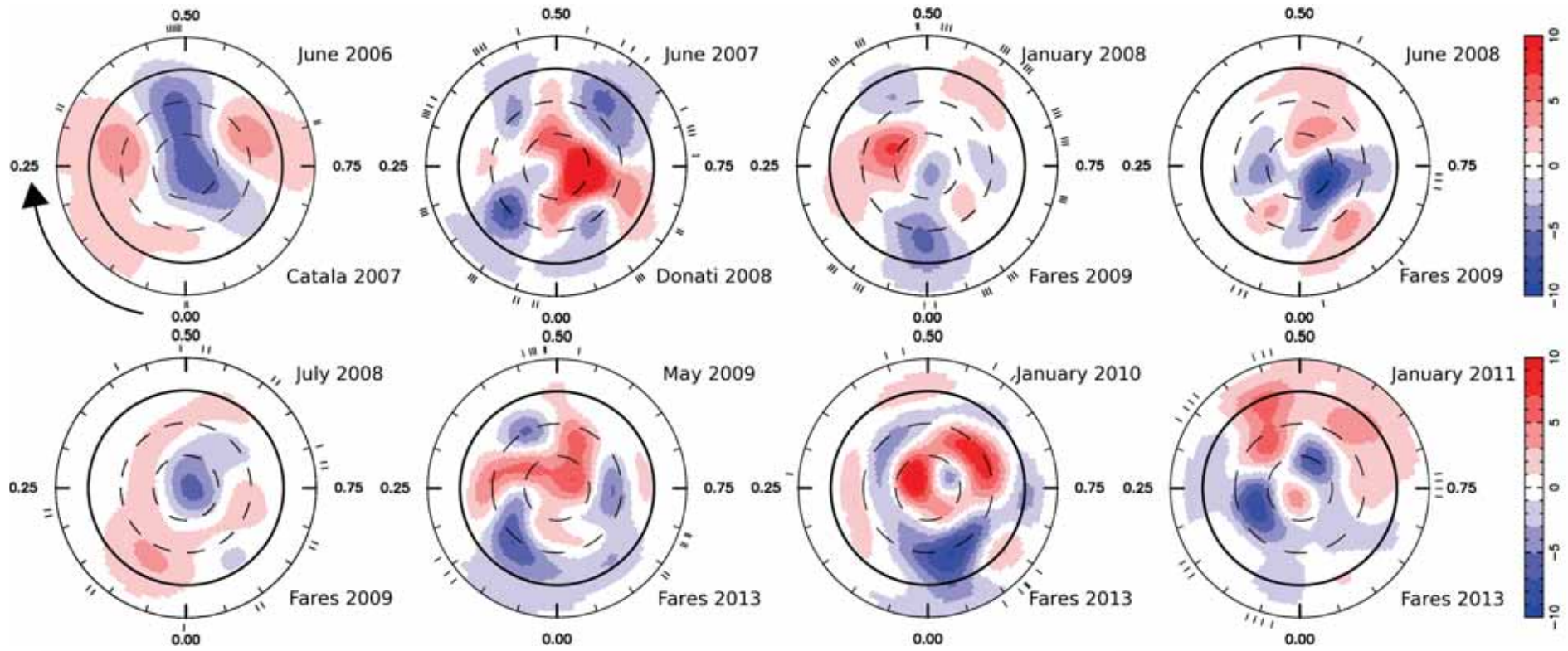
Froehlich 2013,  
Livingston 2007

Radick 1998

Ca H & K Emission

Long-term Activity Cycles

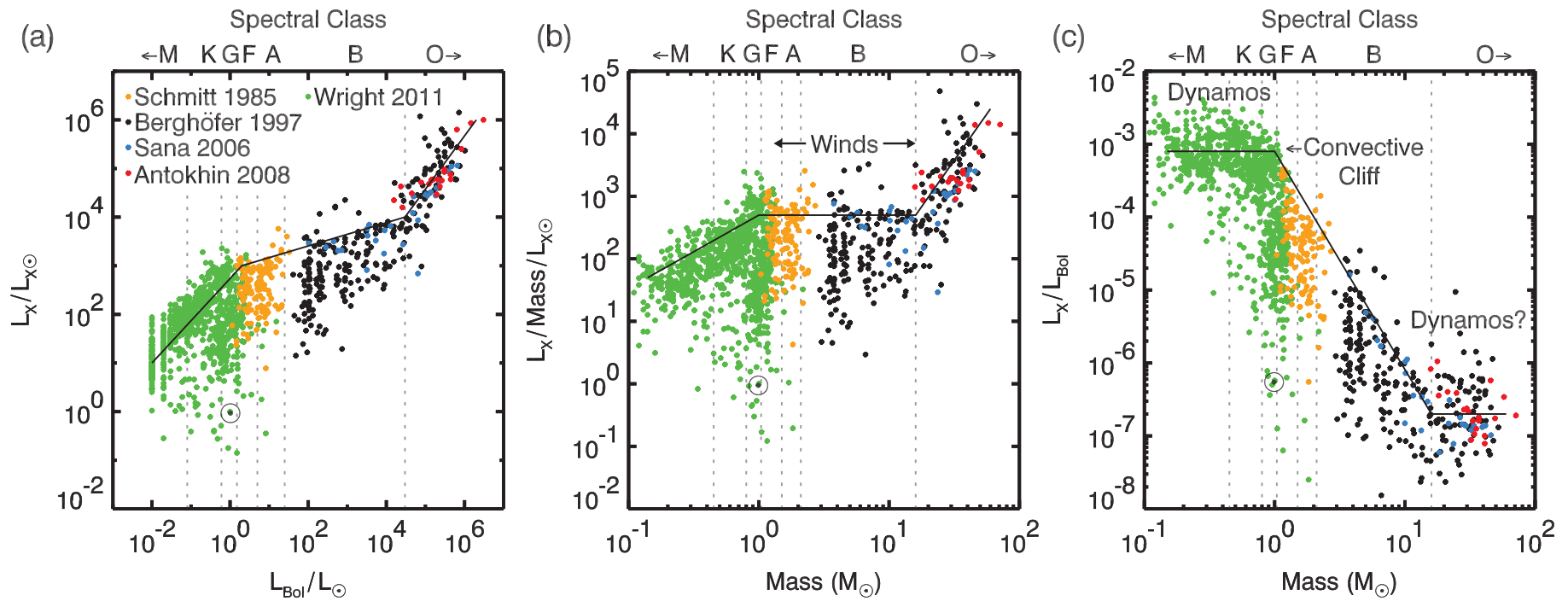
# Stellar Cycles & Magnetism



Spectropolarimetry

Tau-Bootis F-type Star

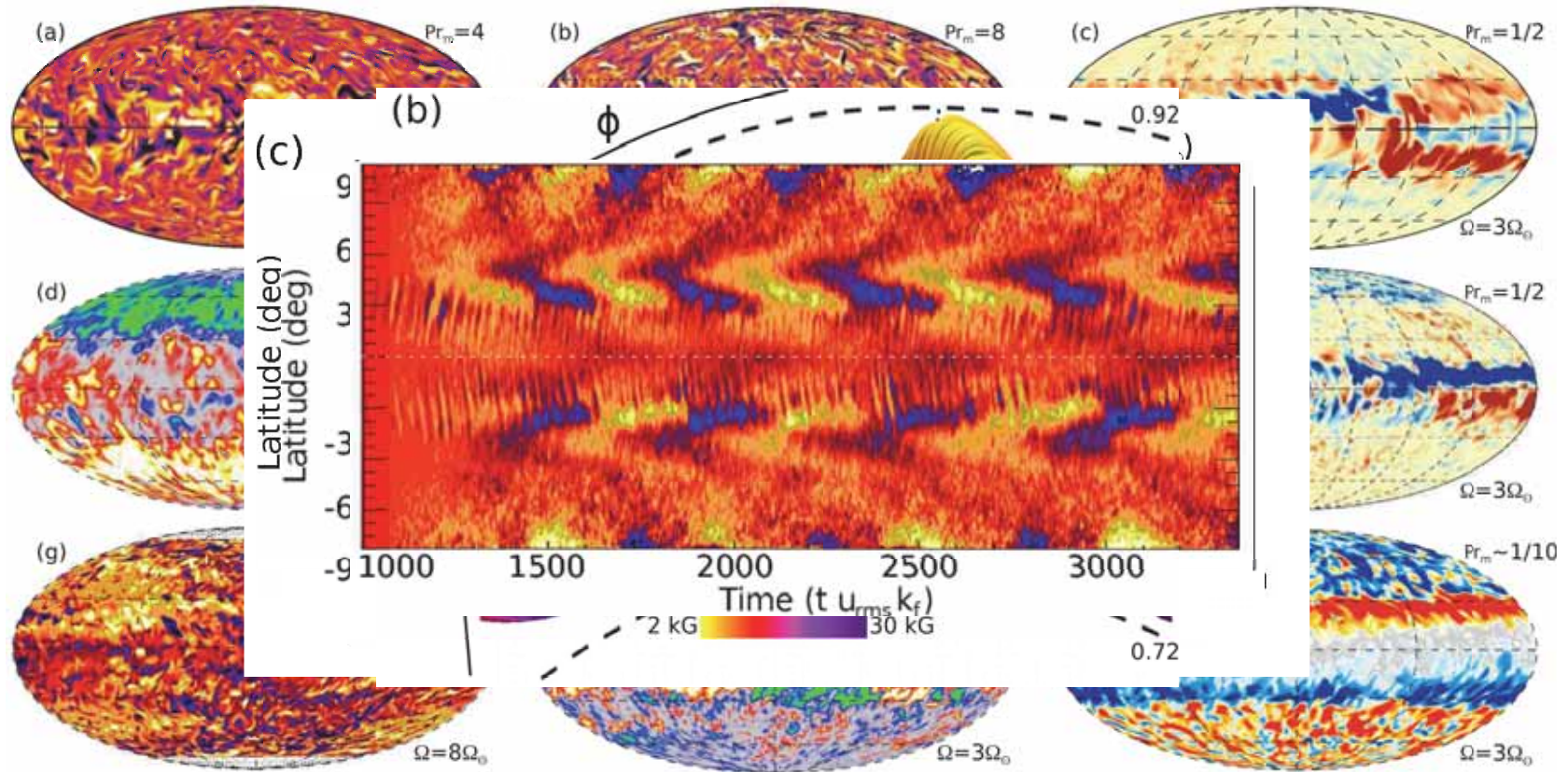
# Stellar Cycles & Magnetism



X-Ray Emission

Convection Transition Regions

# Progress in Stellar Dynamo Theory



Too many sources to list!

$B_\phi$



# Essential Dynamo Processes

Evolution of Mean Magnetic Fields

$$\begin{aligned}
 \frac{\partial A}{\partial t} &= \underbrace{\eta \left( \nabla^2 - \frac{1}{\lambda^2} \right) A}_{\text{magnetic diffusion}} - \underbrace{\frac{1}{\lambda} \mathbf{u}_m \cdot \nabla (\lambda A)}_{\text{meridional advection}} + \underbrace{\hat{\phi} \cdot \overline{\mathbf{u}' \times \mathbf{B}'}}_{\text{poloidal generation}} \\
 \frac{\partial B}{\partial t} &= \underbrace{\eta \left( \nabla^2 - \frac{1}{\lambda^2} \right) B}_{\text{magnetic diffusion}} + \underbrace{\frac{1}{\lambda} \frac{\partial \eta}{\partial r} \frac{\partial \lambda B}{\partial r}}_{\text{diffusive transport}} - \underbrace{\lambda \mathbf{u}_m \cdot \nabla \frac{B}{\lambda}}_{\text{meridional advection}} \\
 &\quad - \underbrace{B \nabla \cdot \mathbf{u}_m}_{\text{compression}} + \underbrace{\lambda \nabla \Omega \cdot \nabla \times A \hat{\phi}}_{\text{stretching}} + \underbrace{\hat{\phi} \cdot \nabla \times \overline{\mathbf{u}' \times \mathbf{B}'}}_{\text{toroidal generation}}
 \end{aligned}$$

Turbulent Correlations

Rotation

- Fully resolved nonlocal 3D MHD  
**Self-consistent flow and field**
- Flux-transport dynamo (e.g., BL)  
**Prescribed flows & model EMF**
- Delta-correlated turbulence (MFT)  
**Prescribed flows & model EMF**

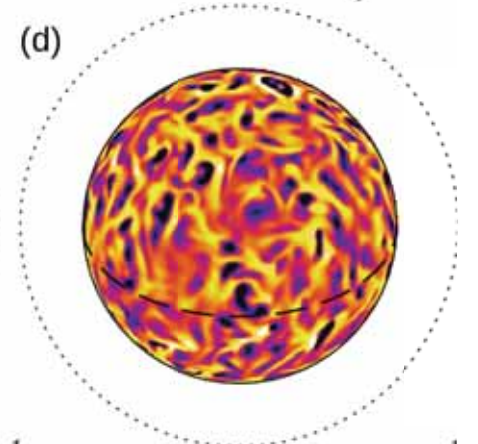
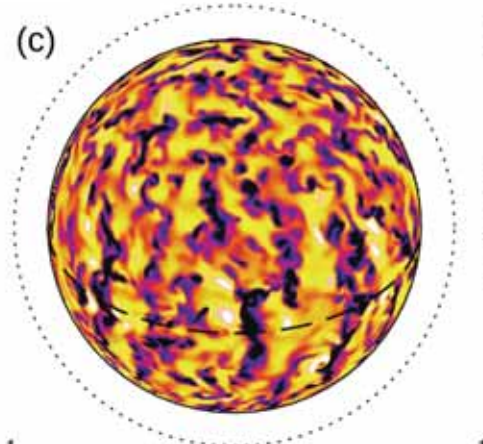
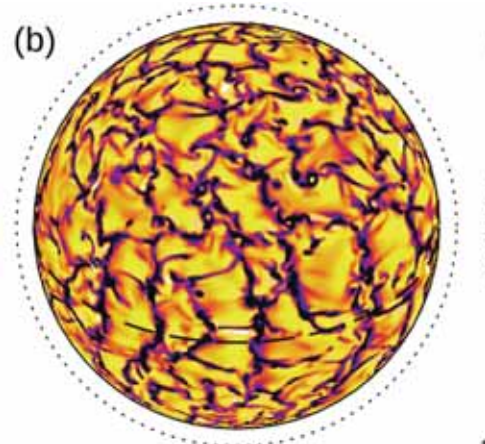
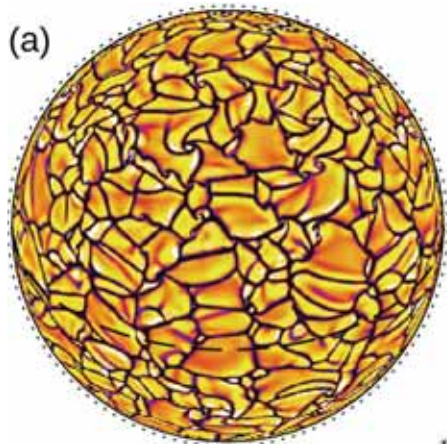
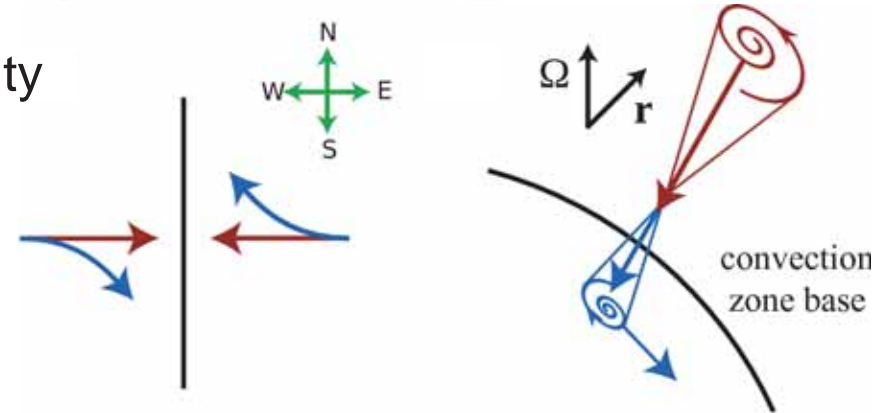
# Elements of Stellar Magnetic Variability

Observations of stellar magnetic variability

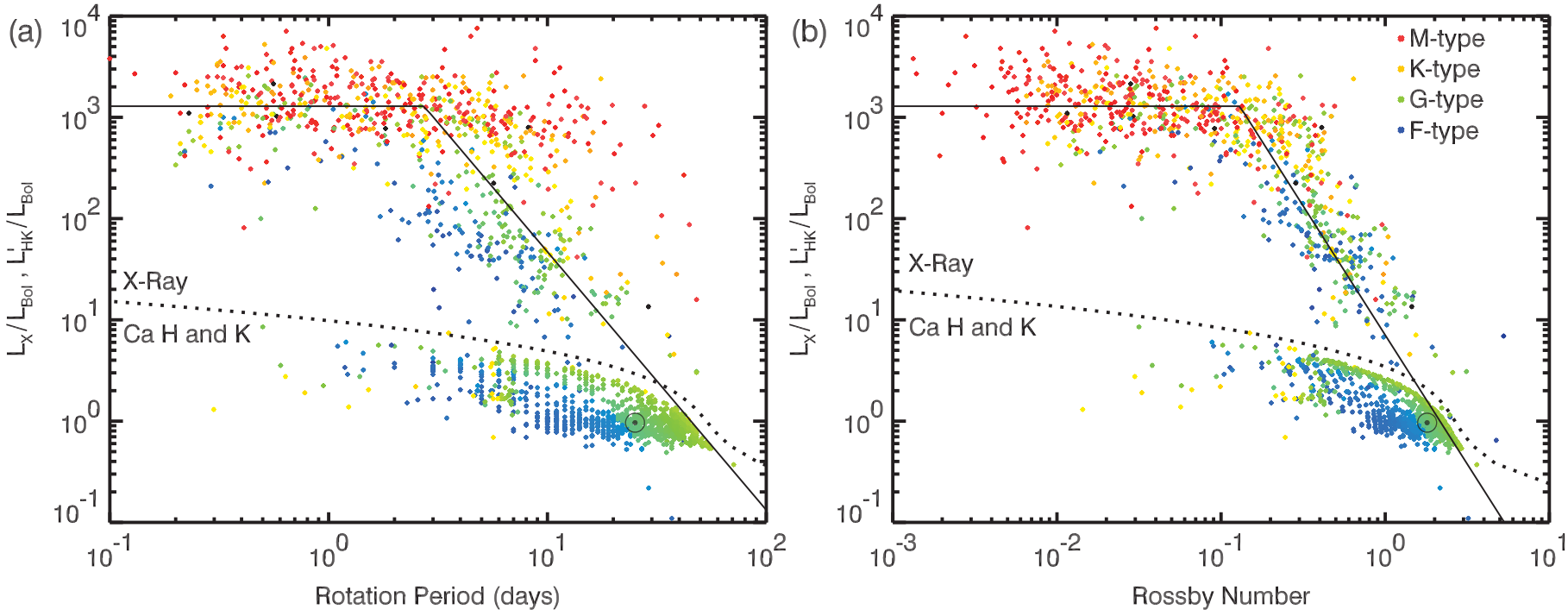
- Largely detects atmospheric phenomenon

Basic building blocks of stellar dynamos

- Helical convection
- Rotation



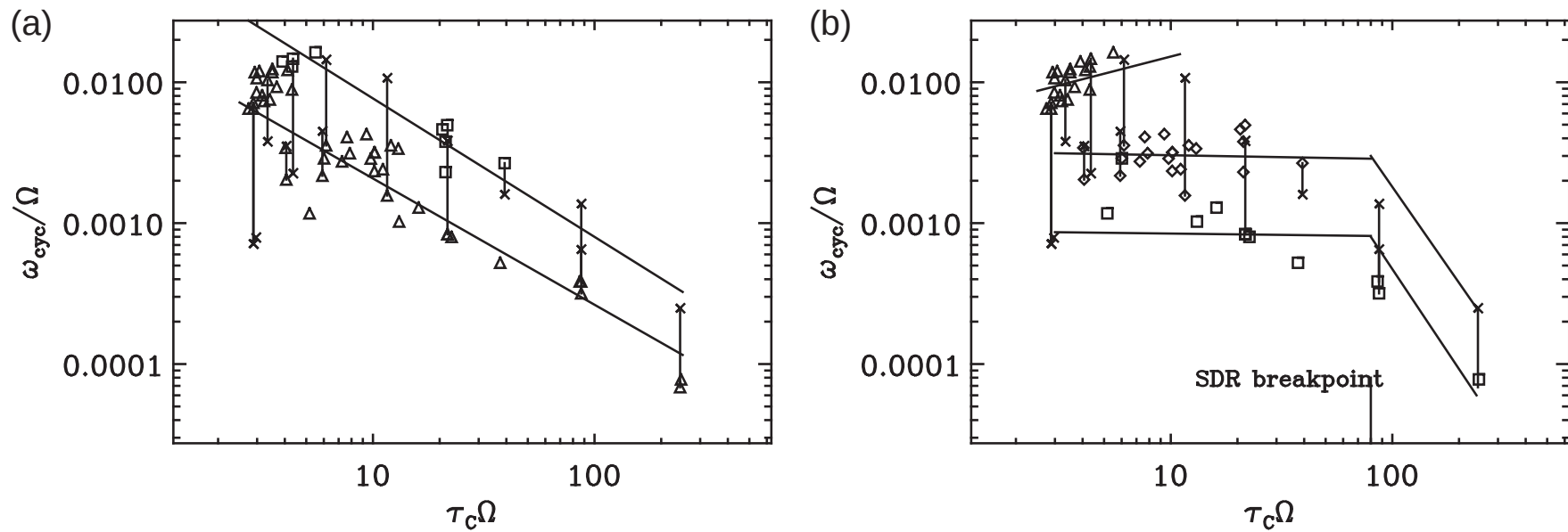
# Rotation-Activity Correlation



Soderblum 1993, Wright 2004, Wright 2011

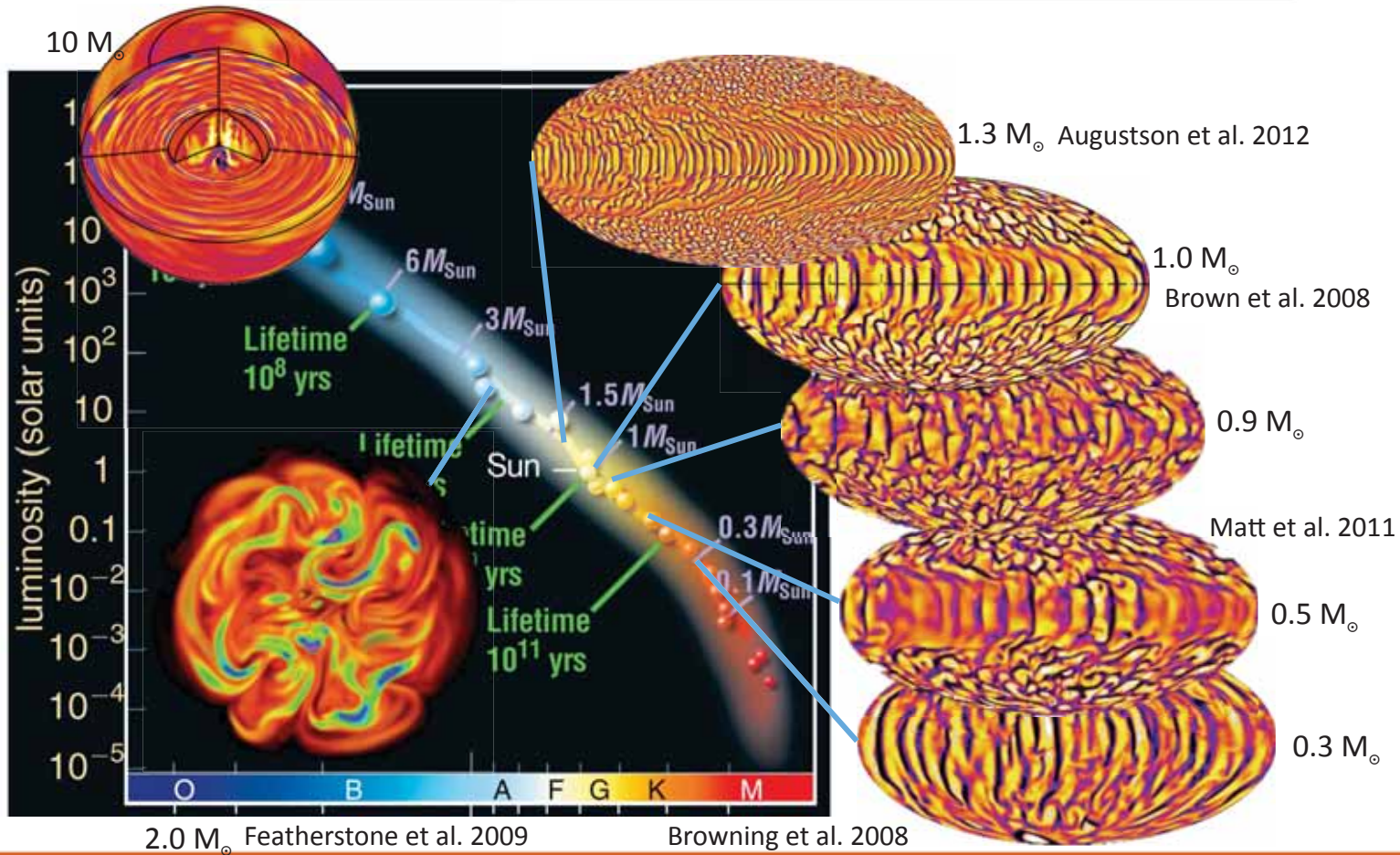


# Rotation-Cycle Period Correlation



Saar 2009

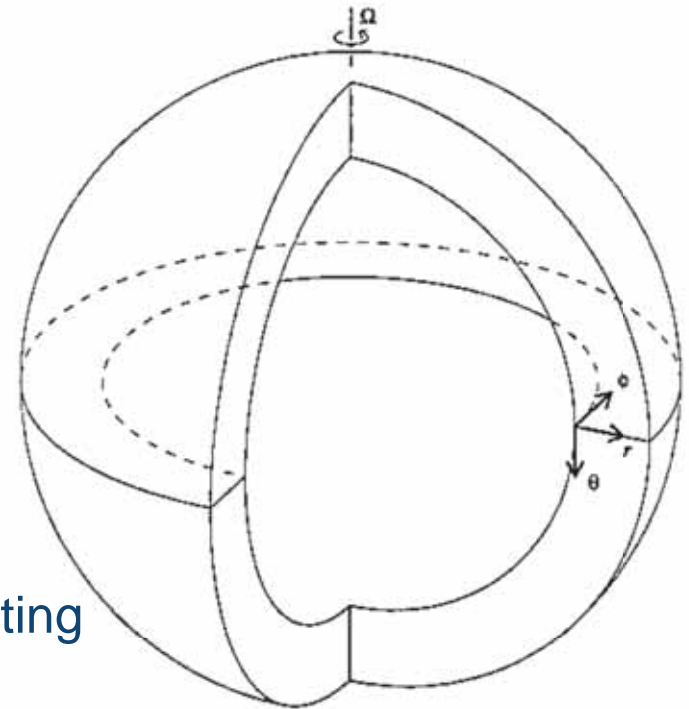
# Simulating the Main-Sequence with ASH



## Features of the ASH Code

### The ASH (Anelastic Spherical Harmonic) code

- Parallel pseudospectral code
- Spherical harmonic & Chebyshev or Finite-difference decomposition
- Spherical shell geometry
- Semi-implicit time-stepping
- Realistic stratification
- Including a stiffly stratified stable layer
- Self-consistent evolution of mean and fluctuating flows and thermodynamics
- Magnetism



Clune et al. 1999; Miesch et al. 2000;  
Brun et al. 2004

## A Few Case Studies

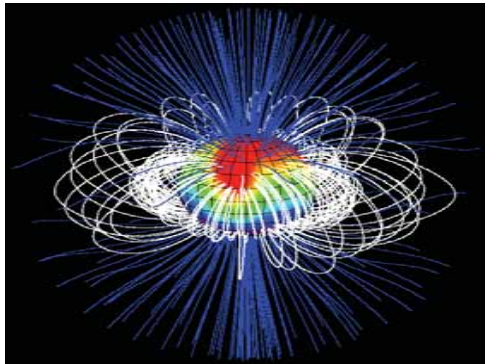
- M dwarfs – Tiny Stars, Strong Fields
- A Young Sun – Faster Cycles & Intermittency
- Massive Stars – Core Convection & Hyper-equipartition



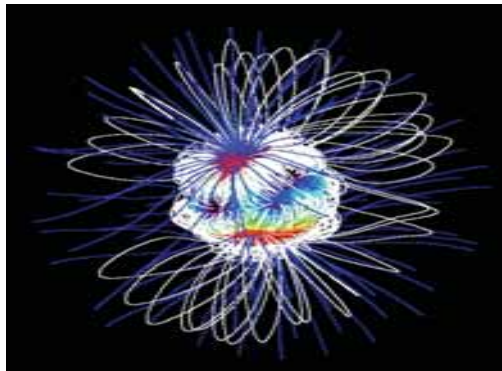
# Tiny Stars and Strong Fields



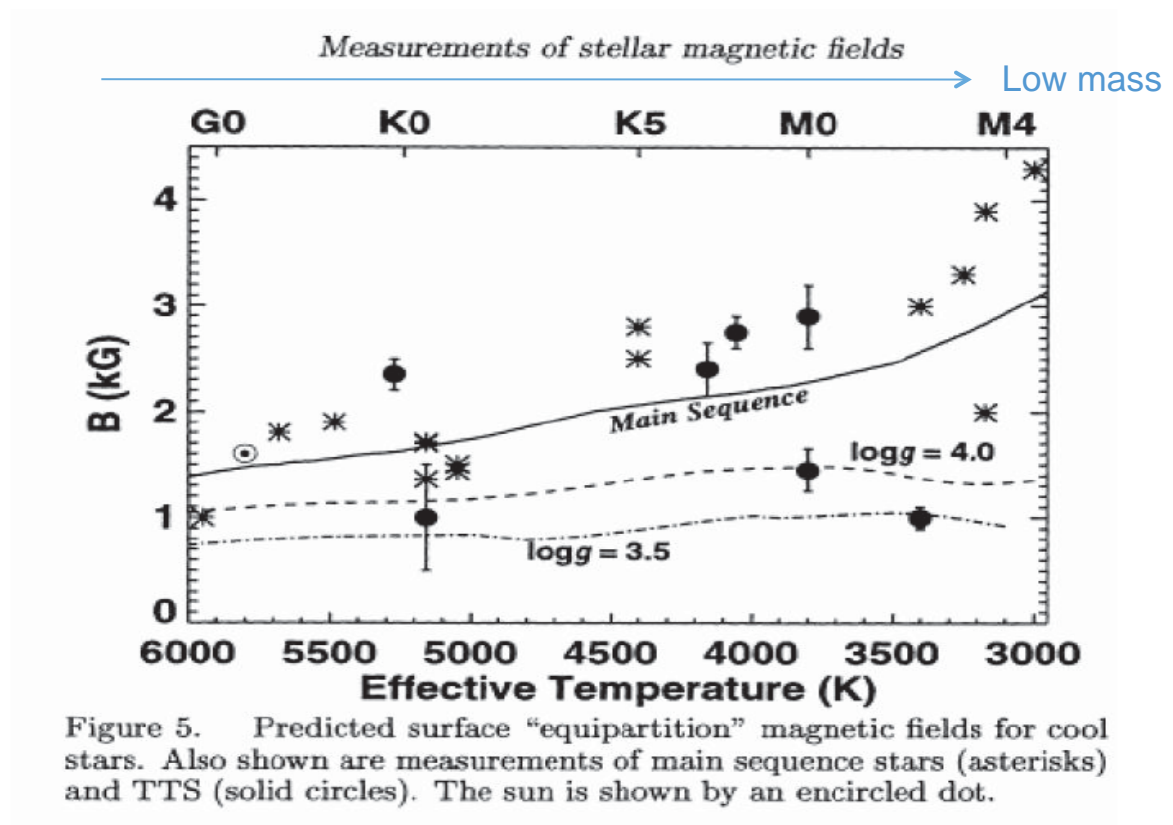




ultra-cool star V374 Pegasi  
(Donati et al.)

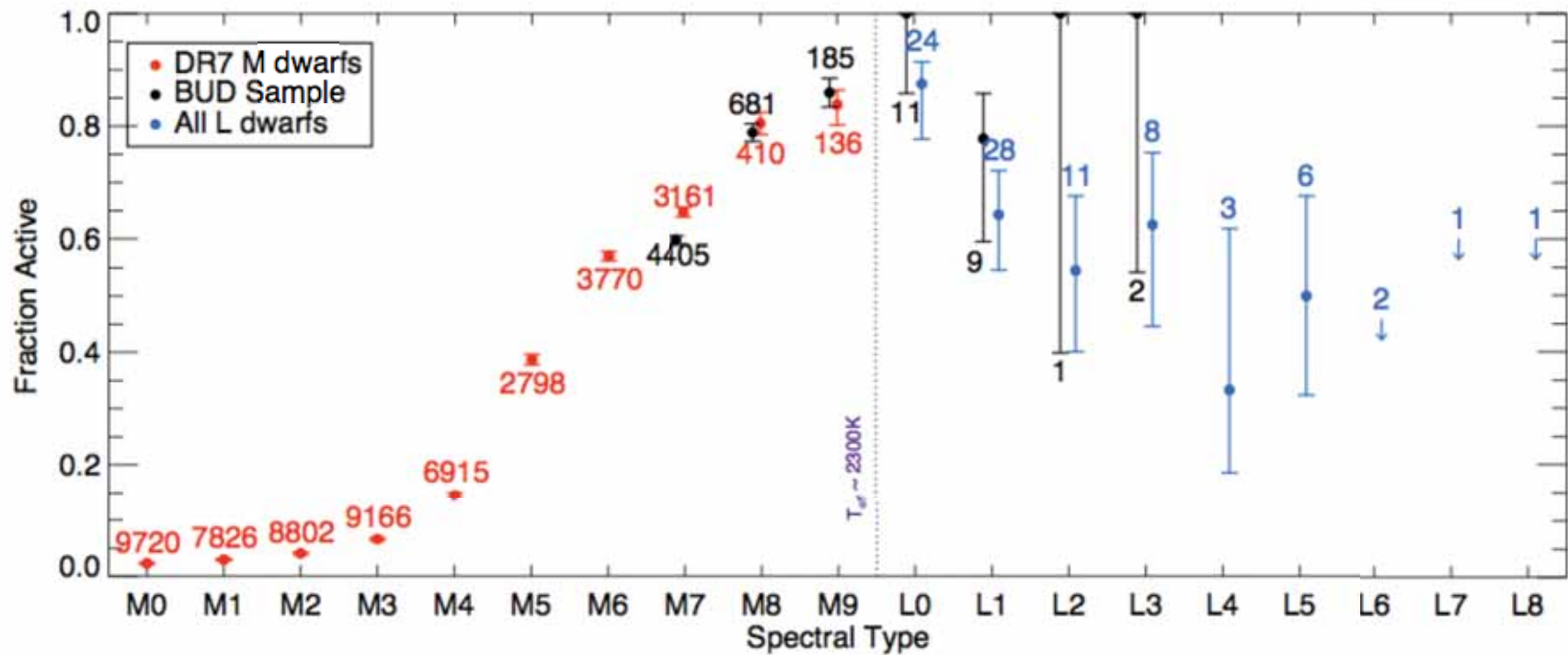


Young star V2129 Oph  
(Donati et al.)



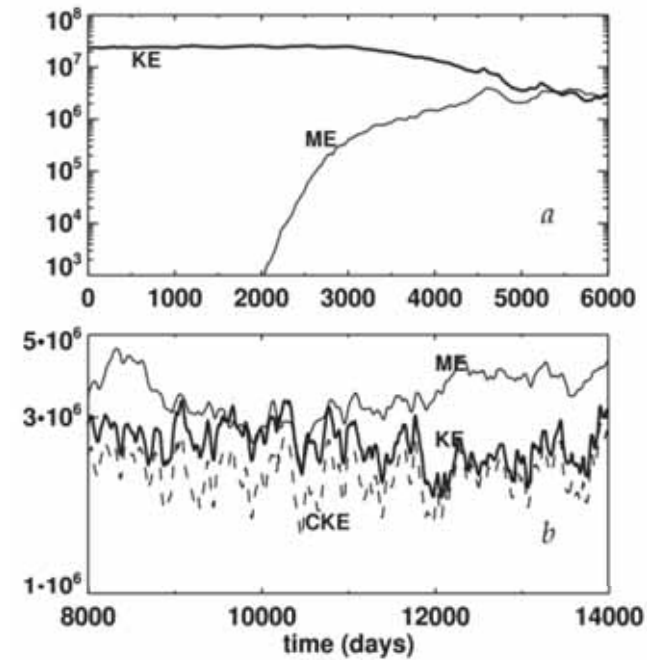
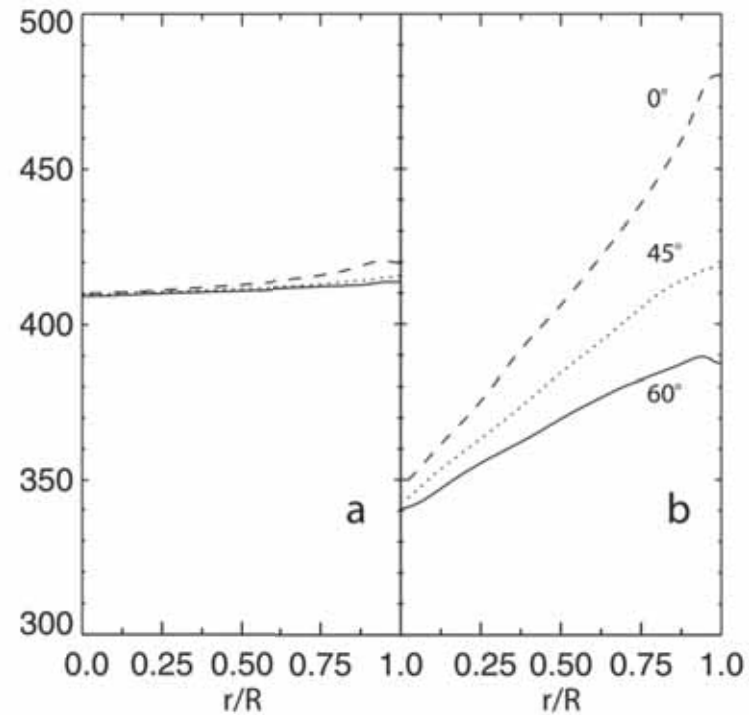
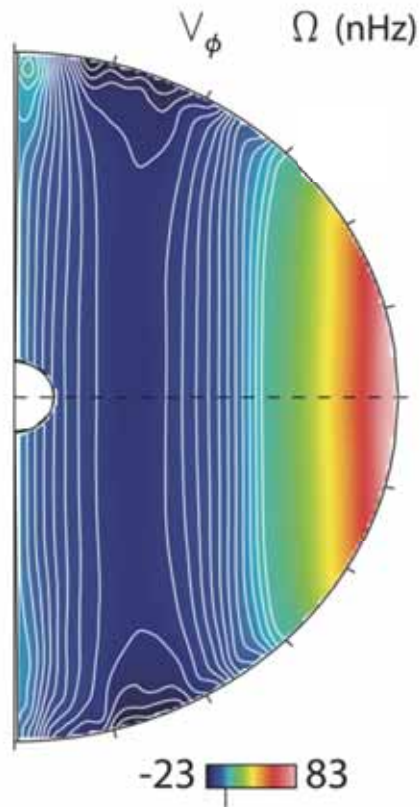
From Johns-Krull & Valenti

# Interface Dynamo Transition?



Schmidt 2014

# Hydrodynamics versus MHD

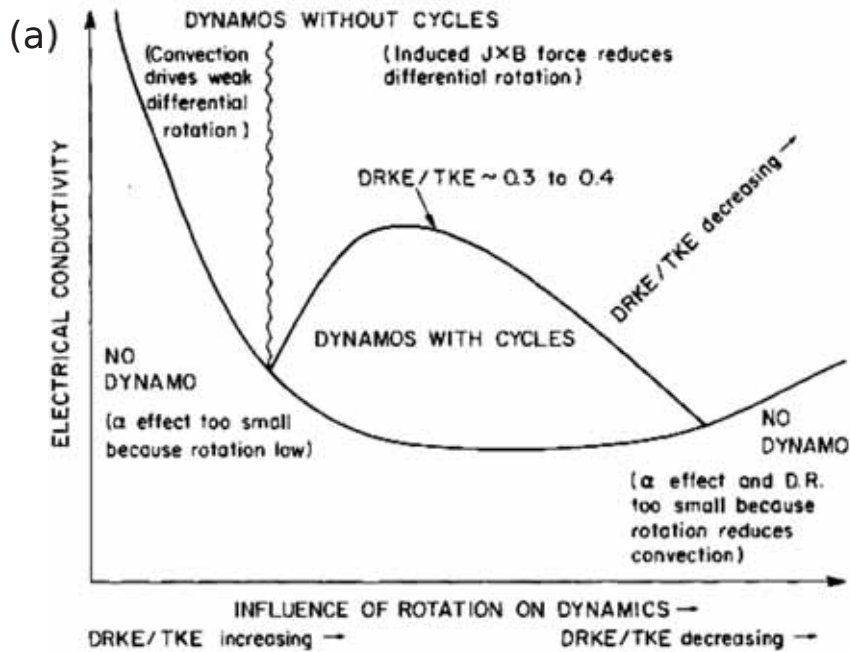


Browning 2008

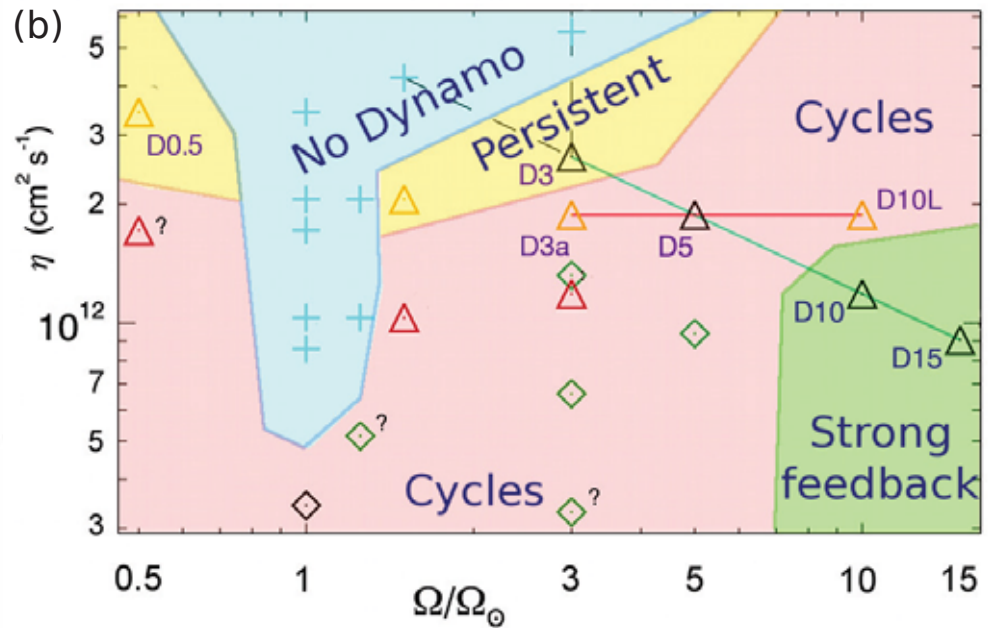
# A Young Sun



# Dynamo Parameter Space Rapidly Rotating Stars

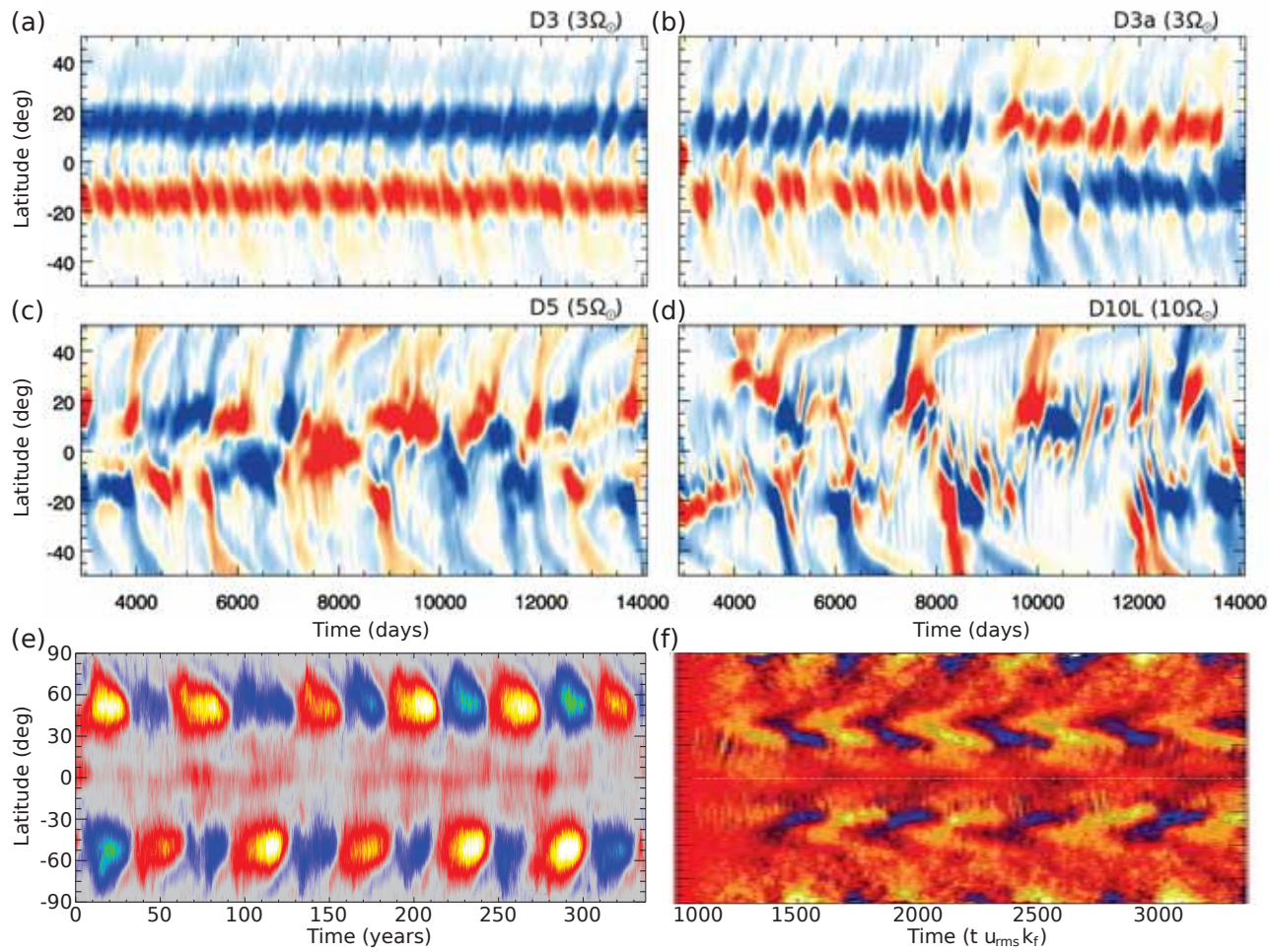


Gilman 1984

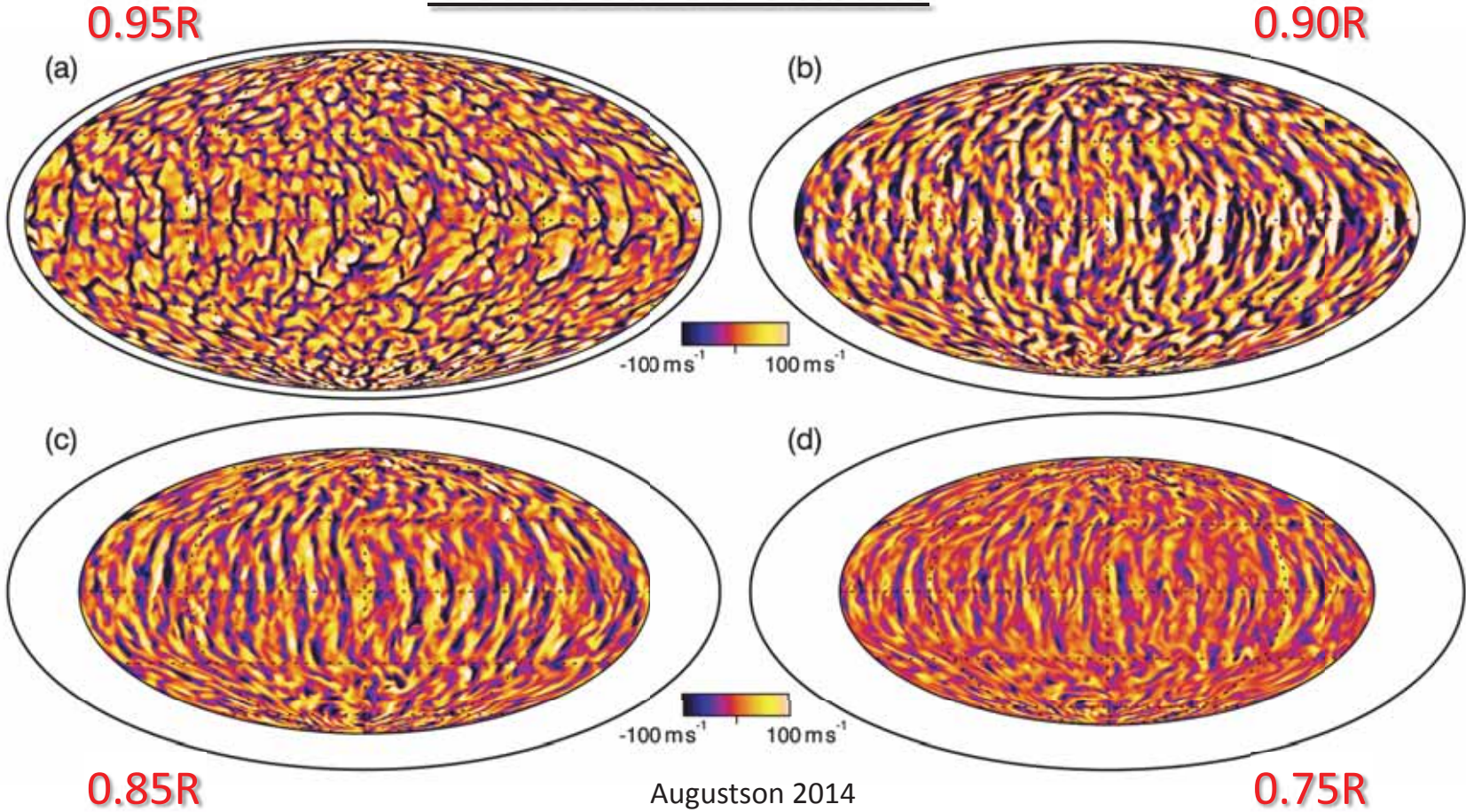


Brown 2011

# Dynamo Parameter Space

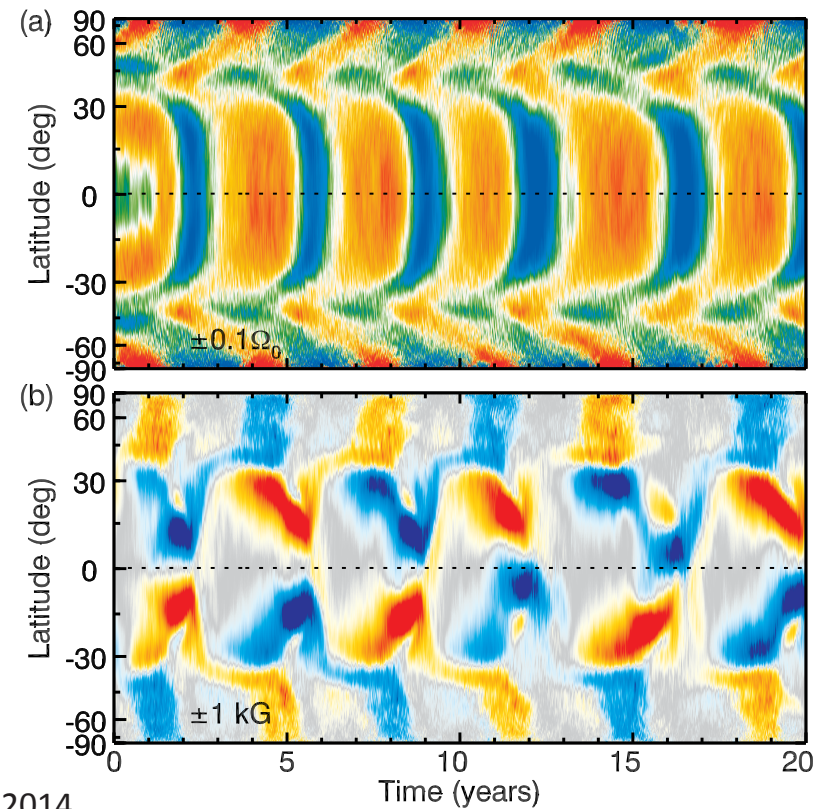
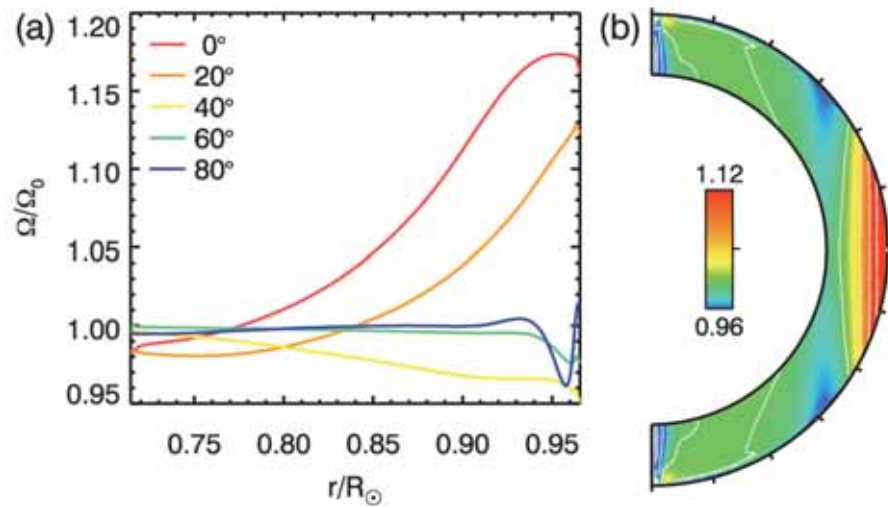


# Convective Patterns



Augustson 2014

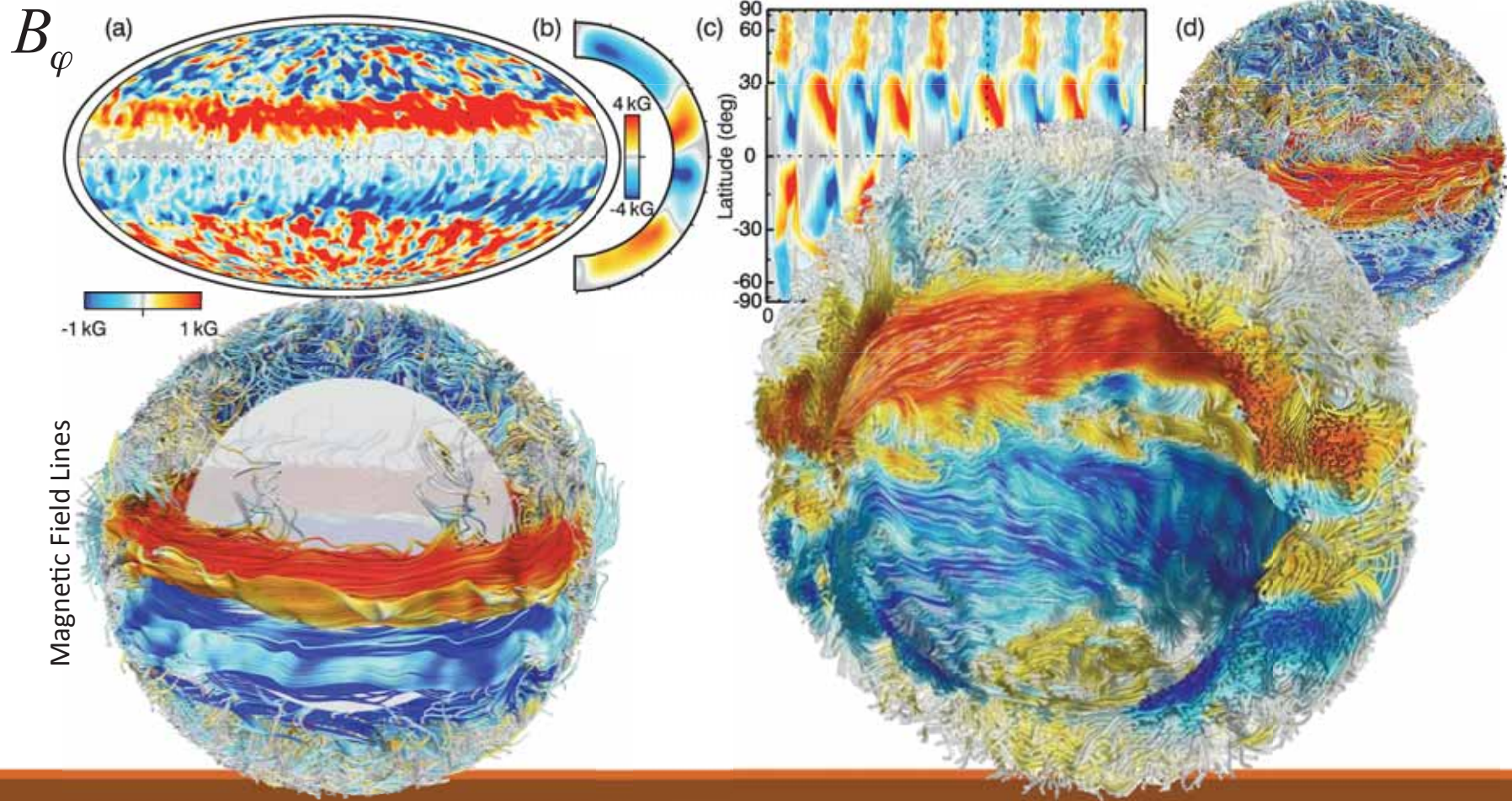
# Differential rotation and its Evolution



Augustson 2014

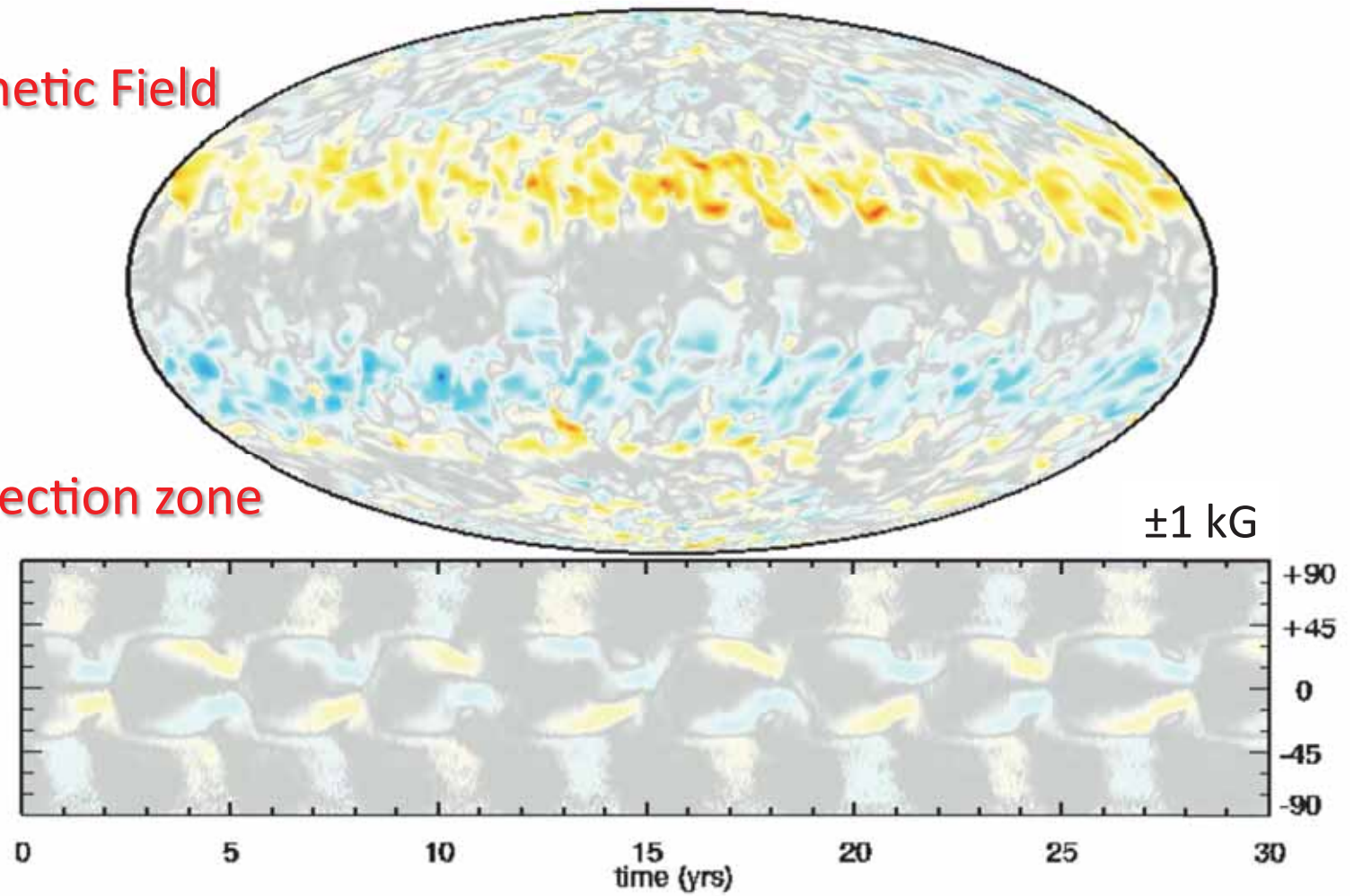


# Wreaths and Magnetic Fields

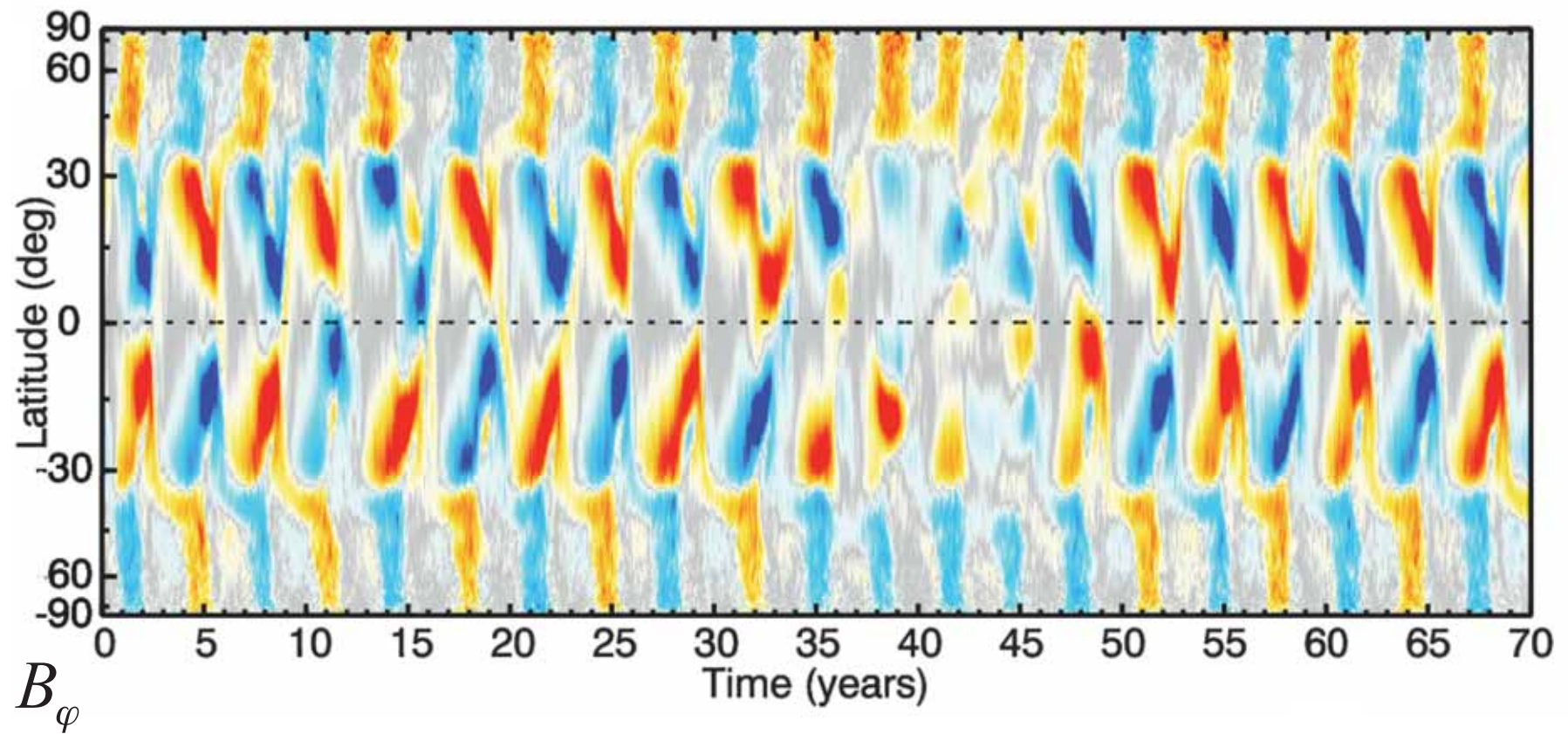


## Toroidal Magnetic Field Evolution

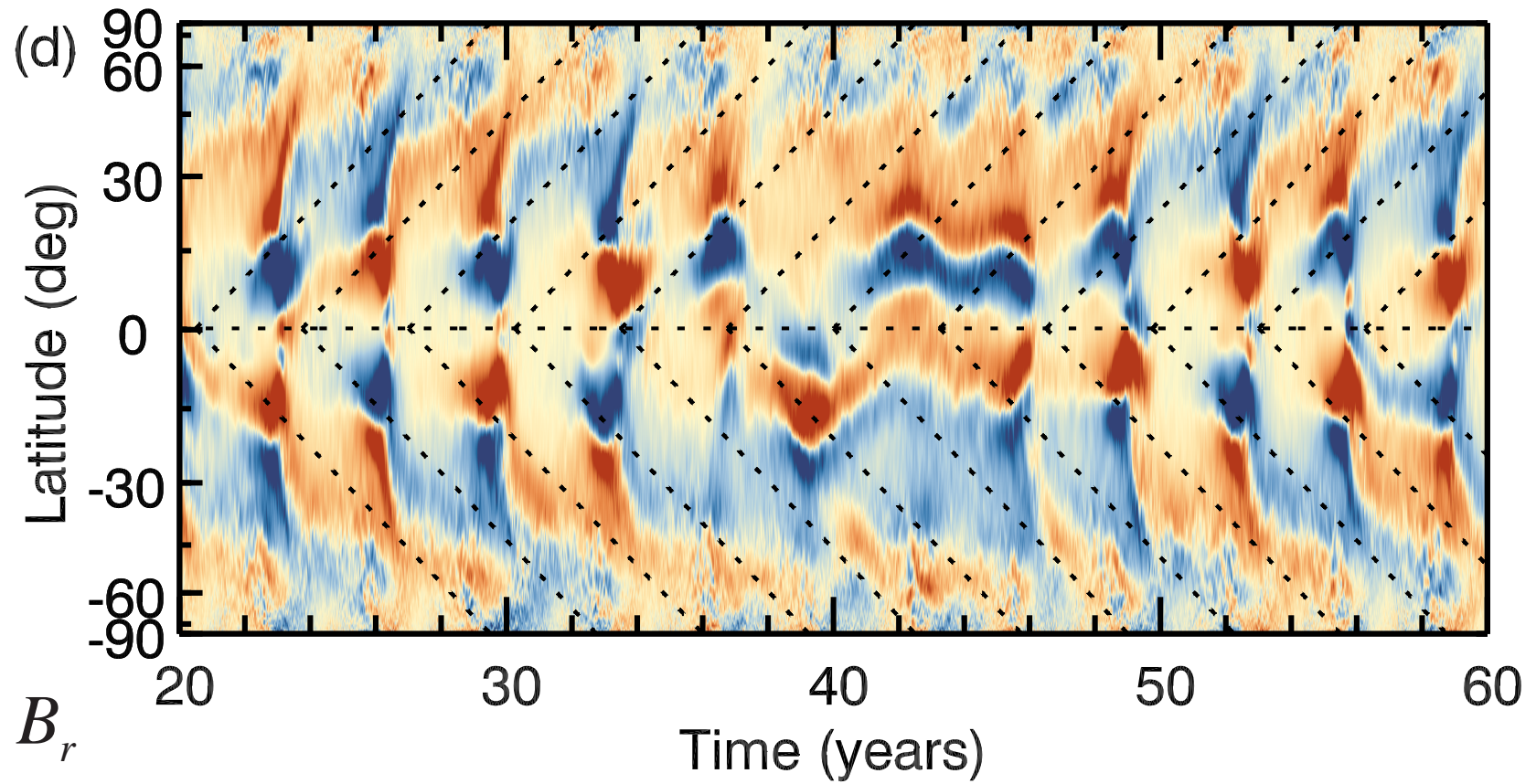
In upper convection zone



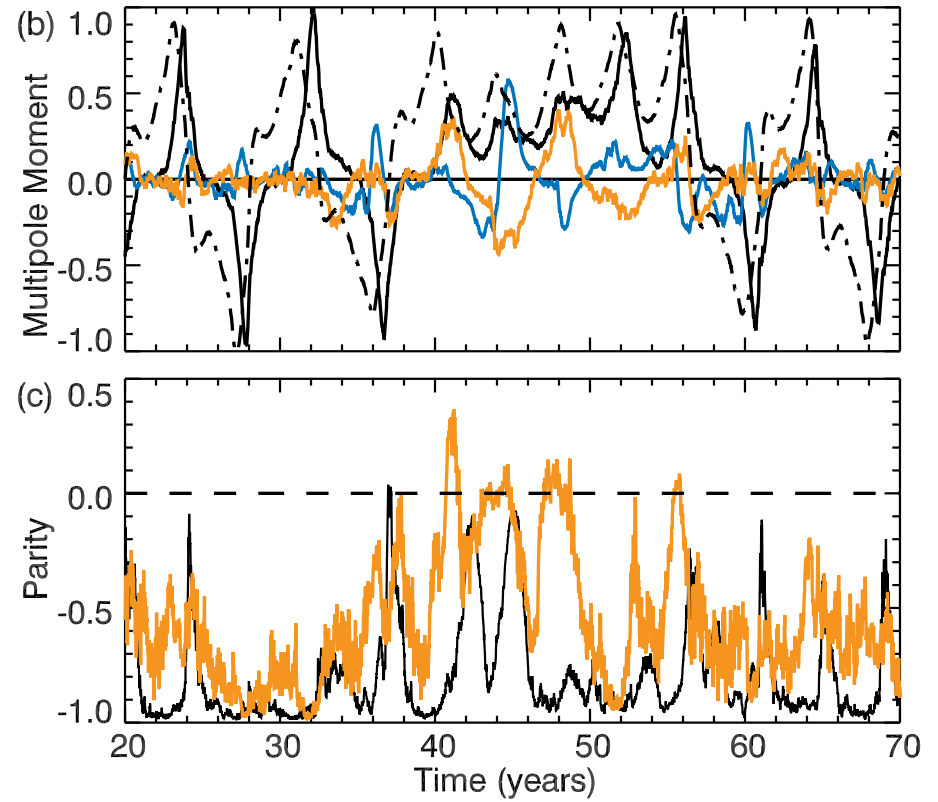
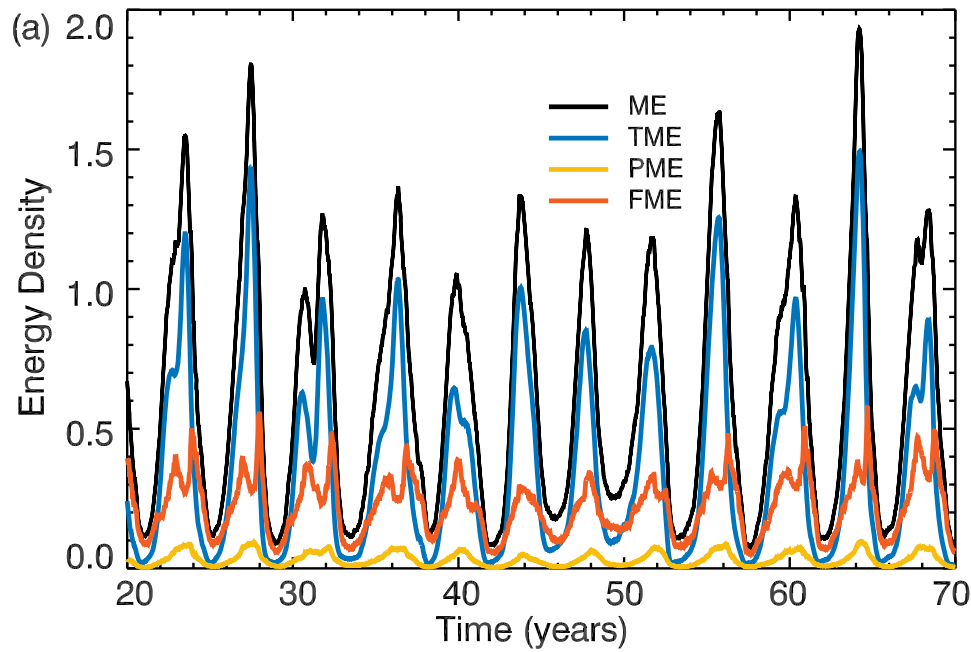
## Long Running Cycles Punctuated with Grand Minimum



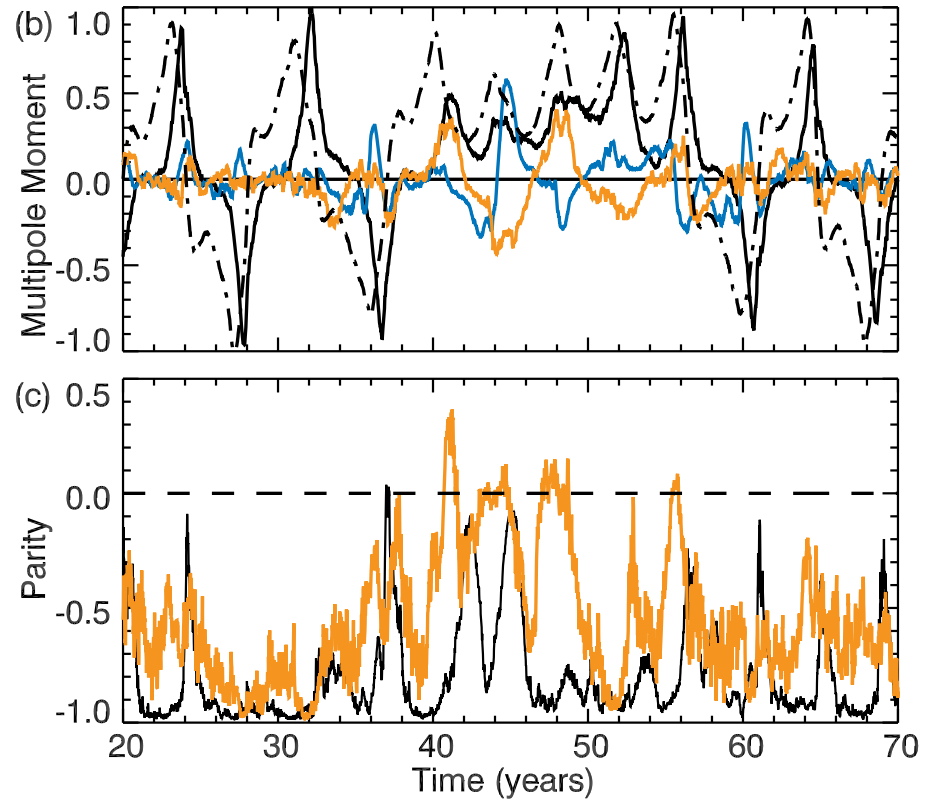
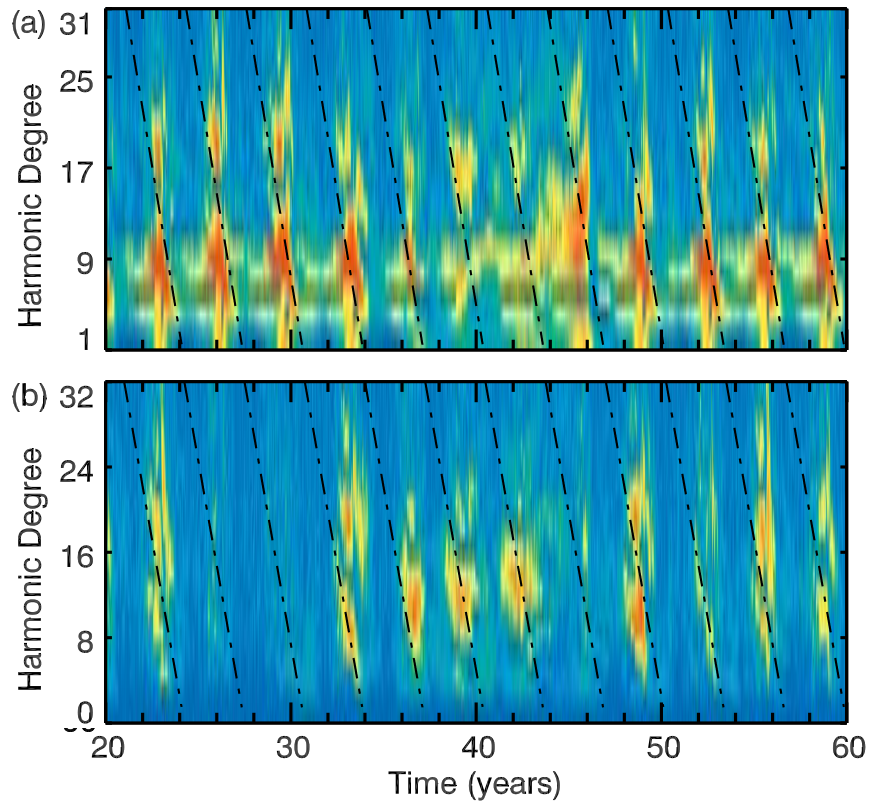
## Long Running Cycles Punctuated with Grand Minimum



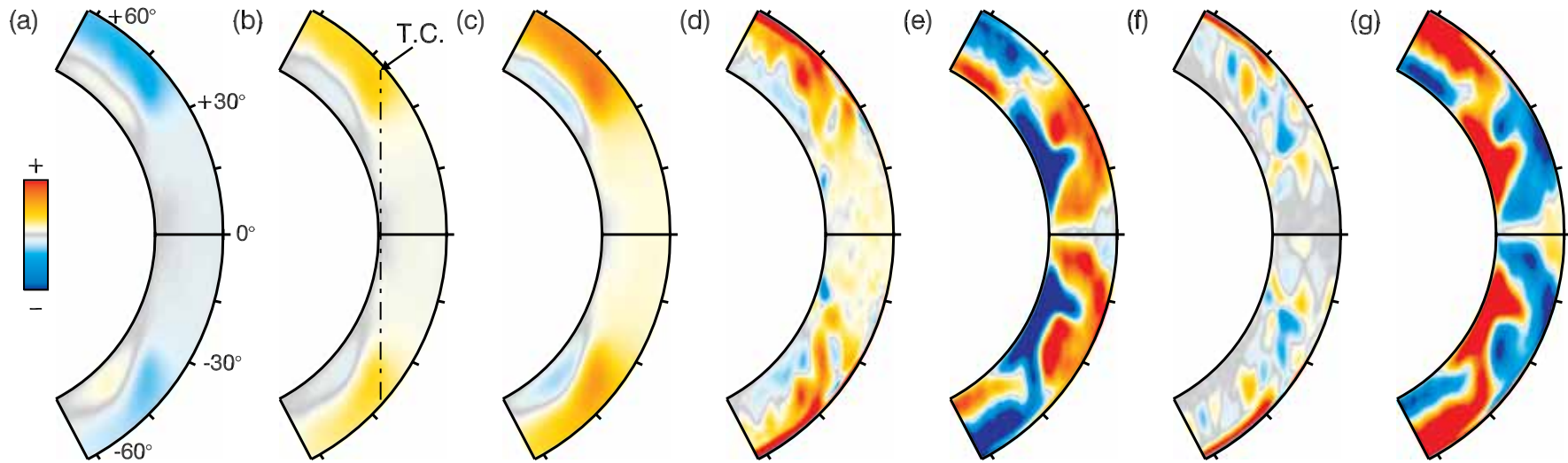
# Long Running Cycles Punctuated with Grand Minimum



# Long Running Cycles Punctuated with Grand Minimum



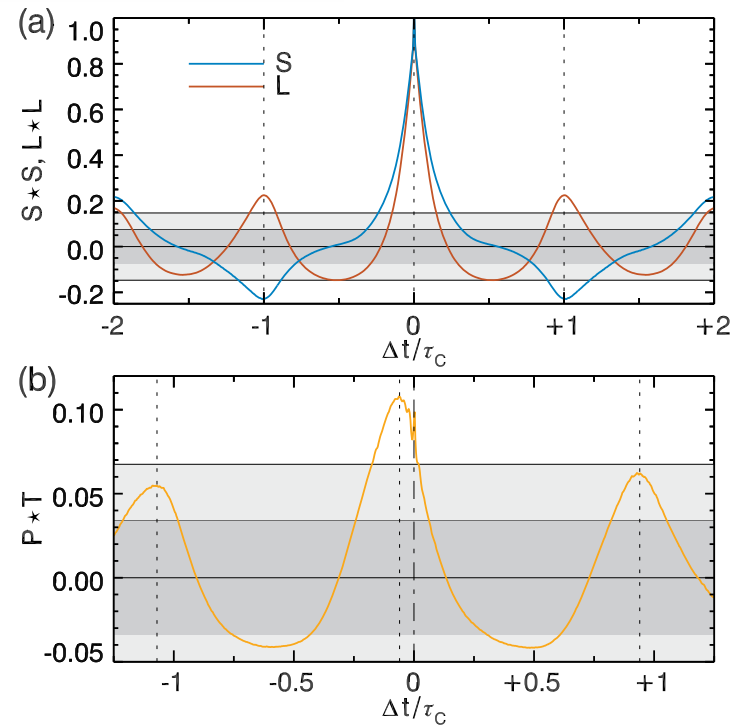
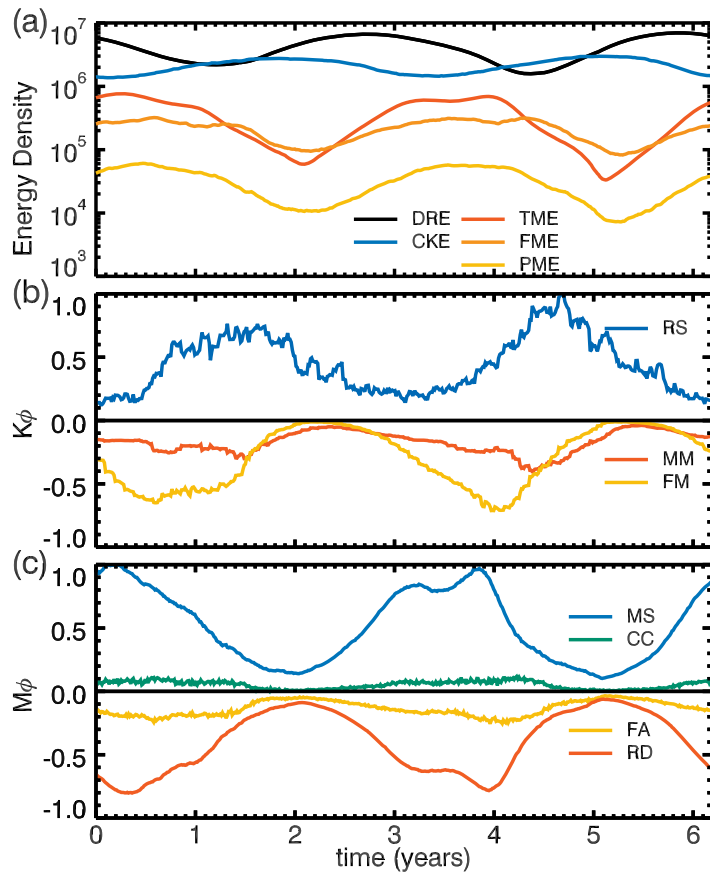
## Time Evolution of Magnetic Energy Generation



$$\Delta \langle A_\varphi \rangle = \langle A_\varphi \rangle_2 - \langle A_\varphi \rangle_1 = \int_{t_1}^{t_2} \hat{\varphi} \cdot \langle \mathbf{v}' \times \mathbf{B}' \rangle dt$$

$$+ \int_{t_1}^{t_2} \hat{\varphi} \cdot (\langle \mathbf{v} \rangle \times \langle \mathbf{B} \rangle) dt - \int_{t_1}^{t_2} \eta \langle J_\varphi \rangle dt.$$

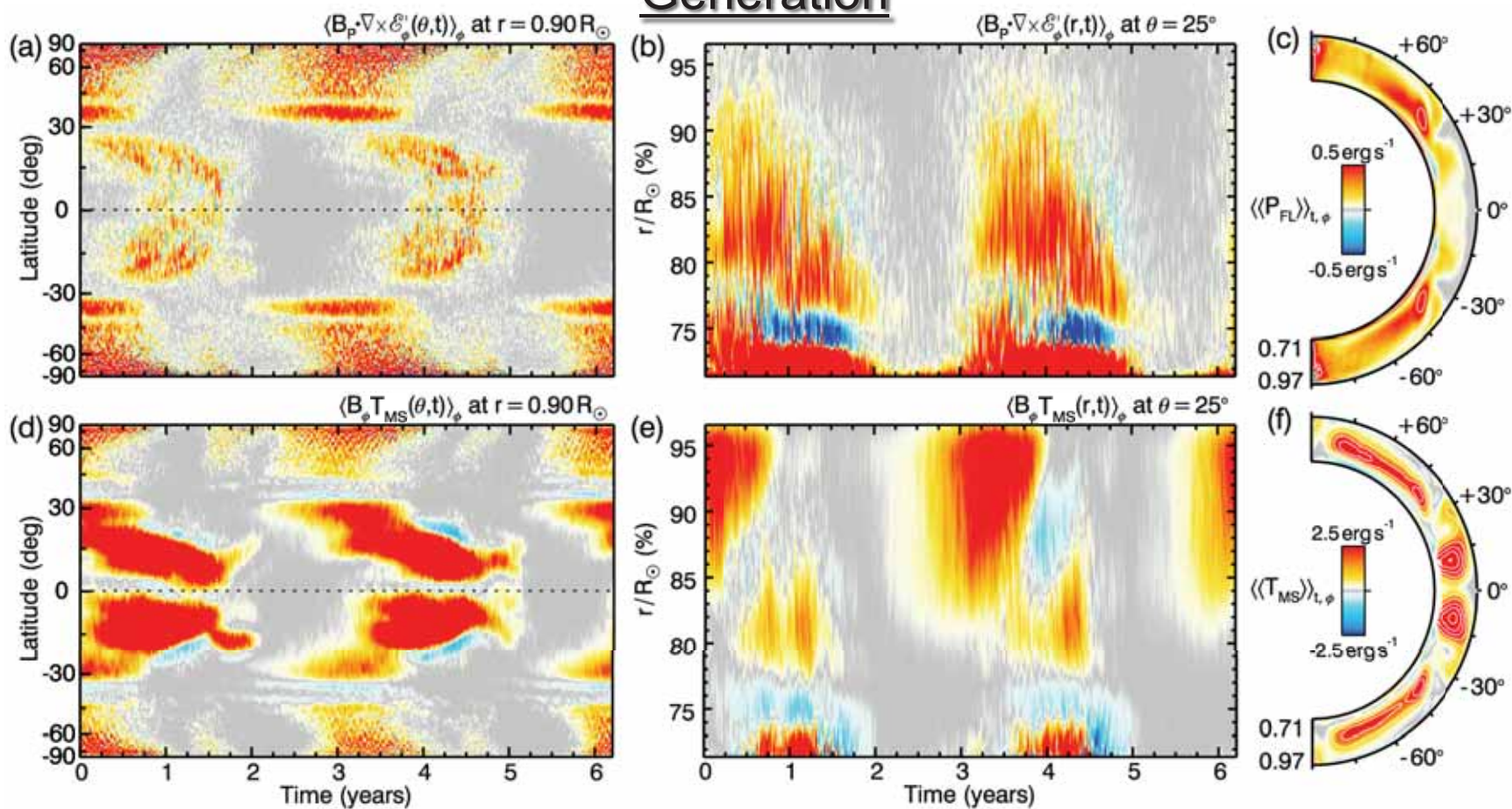
## Time Evolution of Magnetic Energy Generation



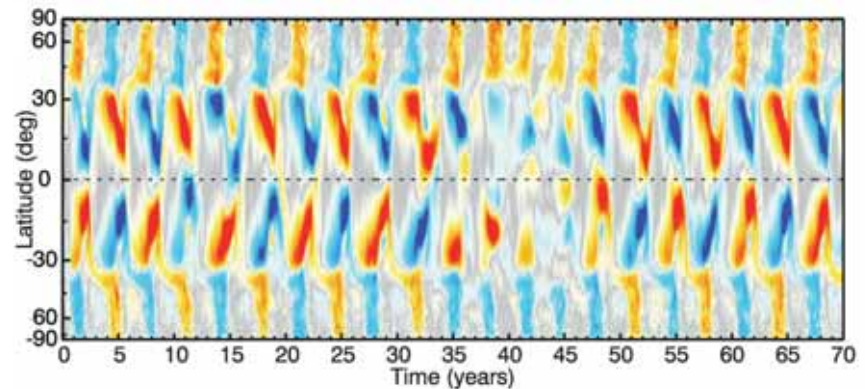
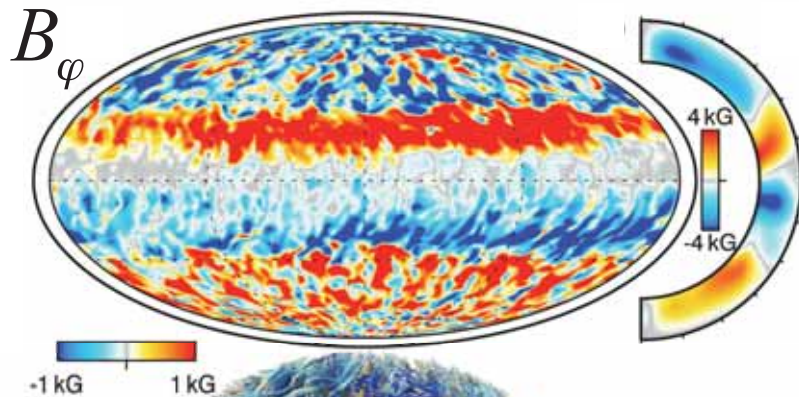
Time evolution of volume averaged kinetic and magnetic energy generation



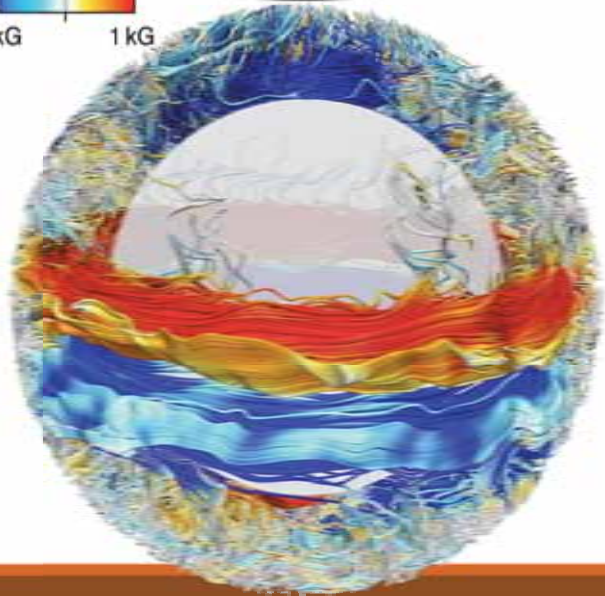
# Time Evolution of Magnetic Energy Generation



## Cycling Wreaths of Magnetism in a Stellar Dynamo Simulation



Magnetic Field Lines



Features similar to the observed solar dynamo:

- Magnetic energy (activity) cycles
- Regular polarity reversals
- Equatorward propagation of magnetic structures
- Grand minimum

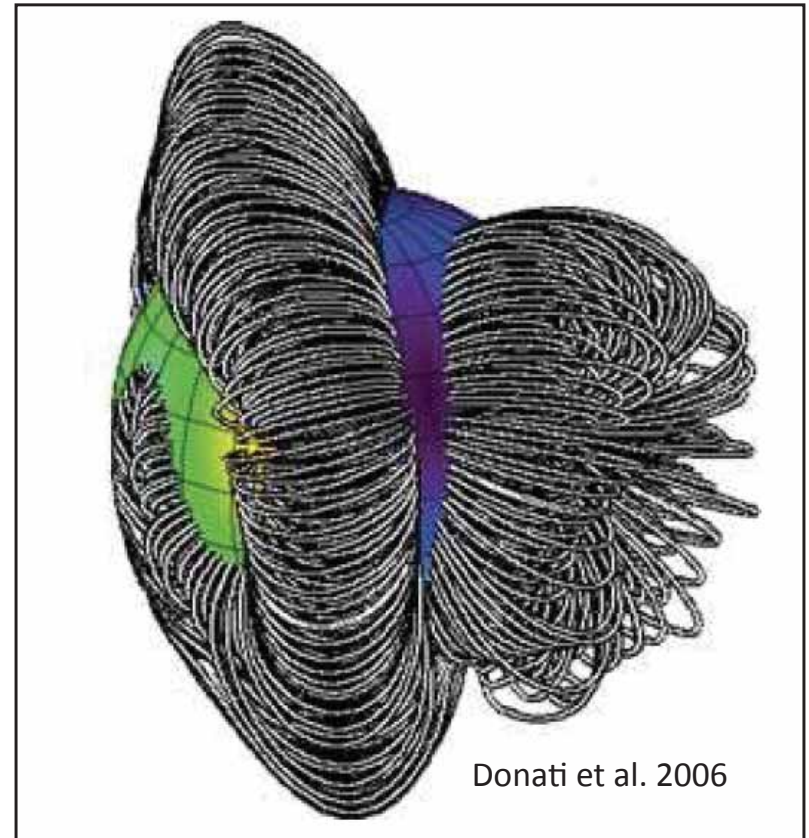
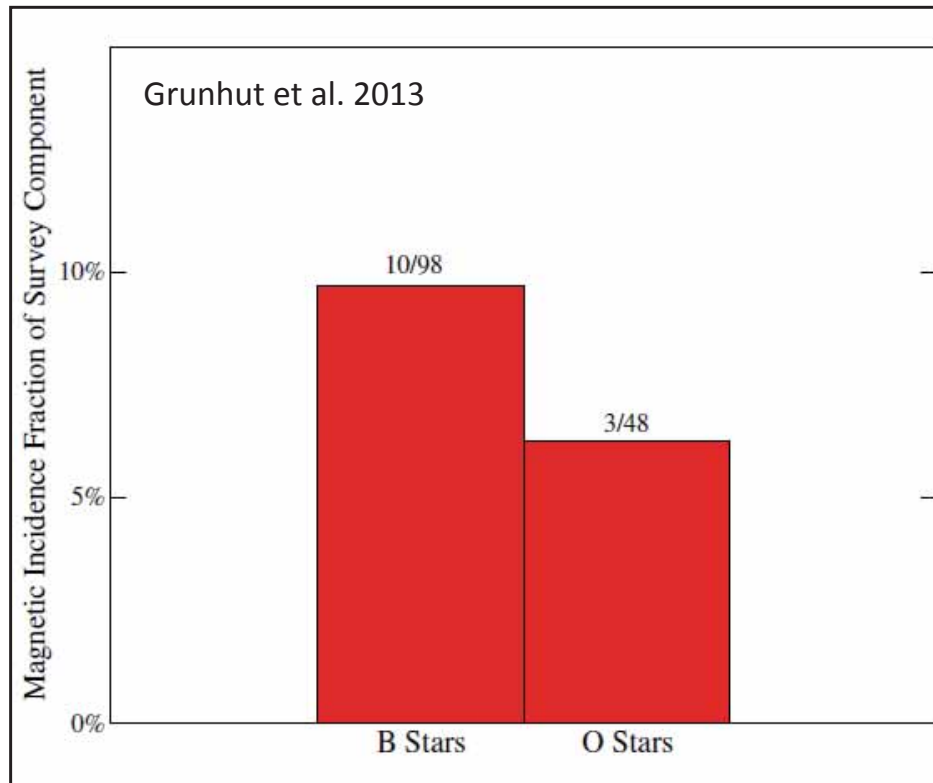
Physical processes at work (Augustson et al., ApJ, 2014):

- Polarity cycle arising from
  - Strong Lorentz-force feedback
  - Low-latitude poloidal field generation
  - Resistive collapse
- Equatorward propagation through a nonlinear dynamo wave
- Grand minimum arising from loss of phase correlation

# Massive Stars and Core Convection



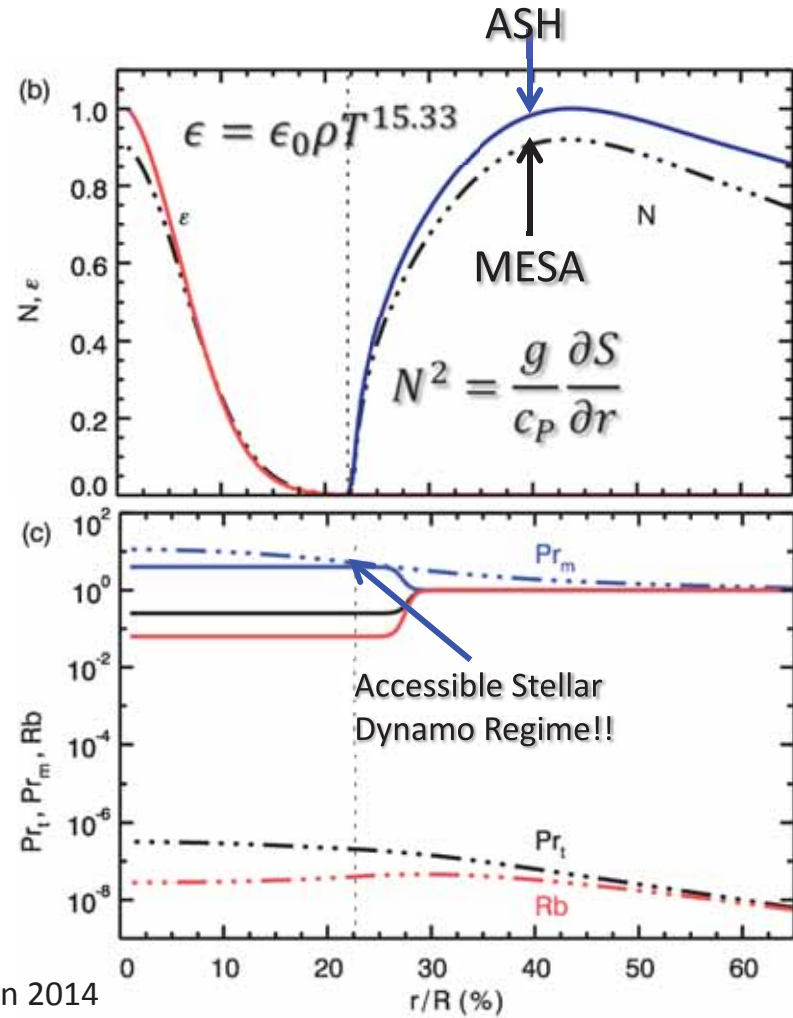
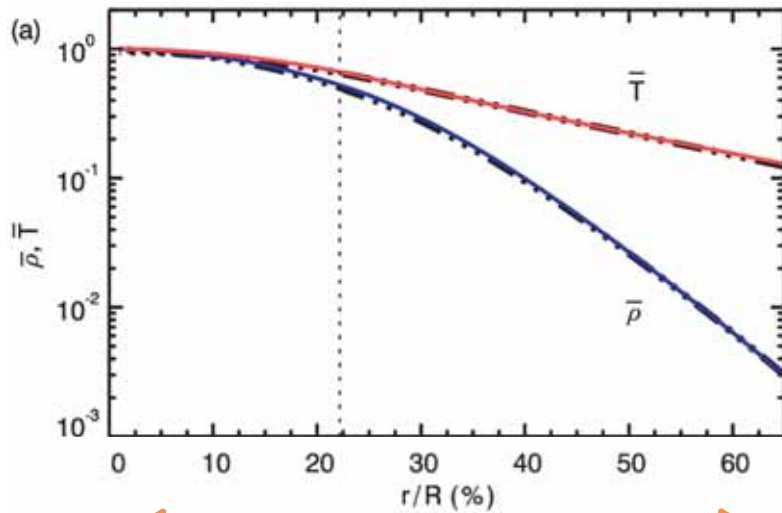
# Massive Star Magnetism



# Problem Setup

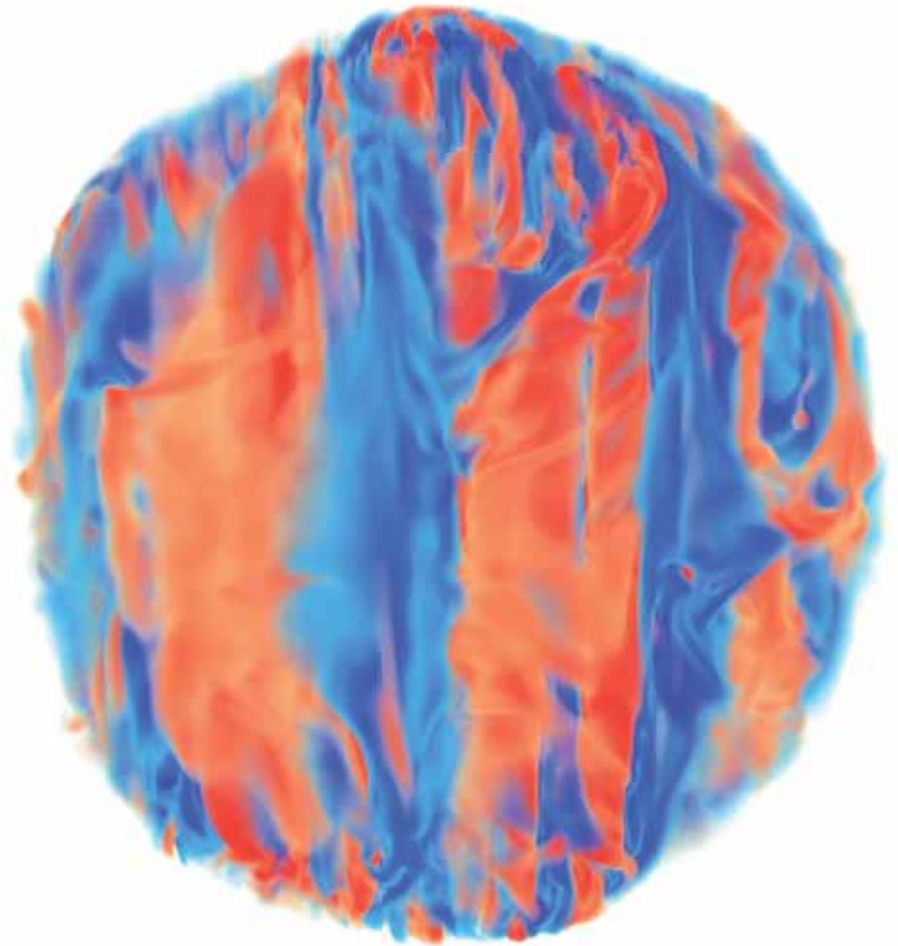
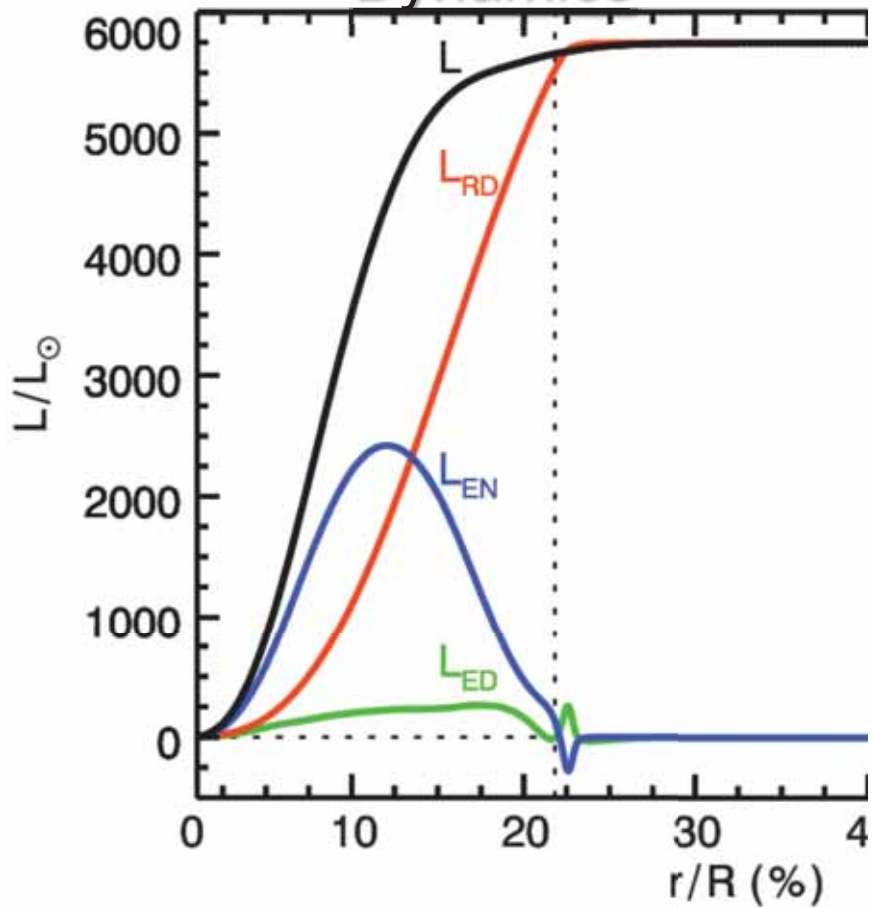
## MS B-type Star Simulations

- 10 Solar Masses (MESA)
- Rotation:  
30 – 480 km/s ( $v_{eq}$ )  
0.1 – 50% of breakup
- Non-uniform FD



Augustson 2014

# Energy Flux and Convective Dynamics

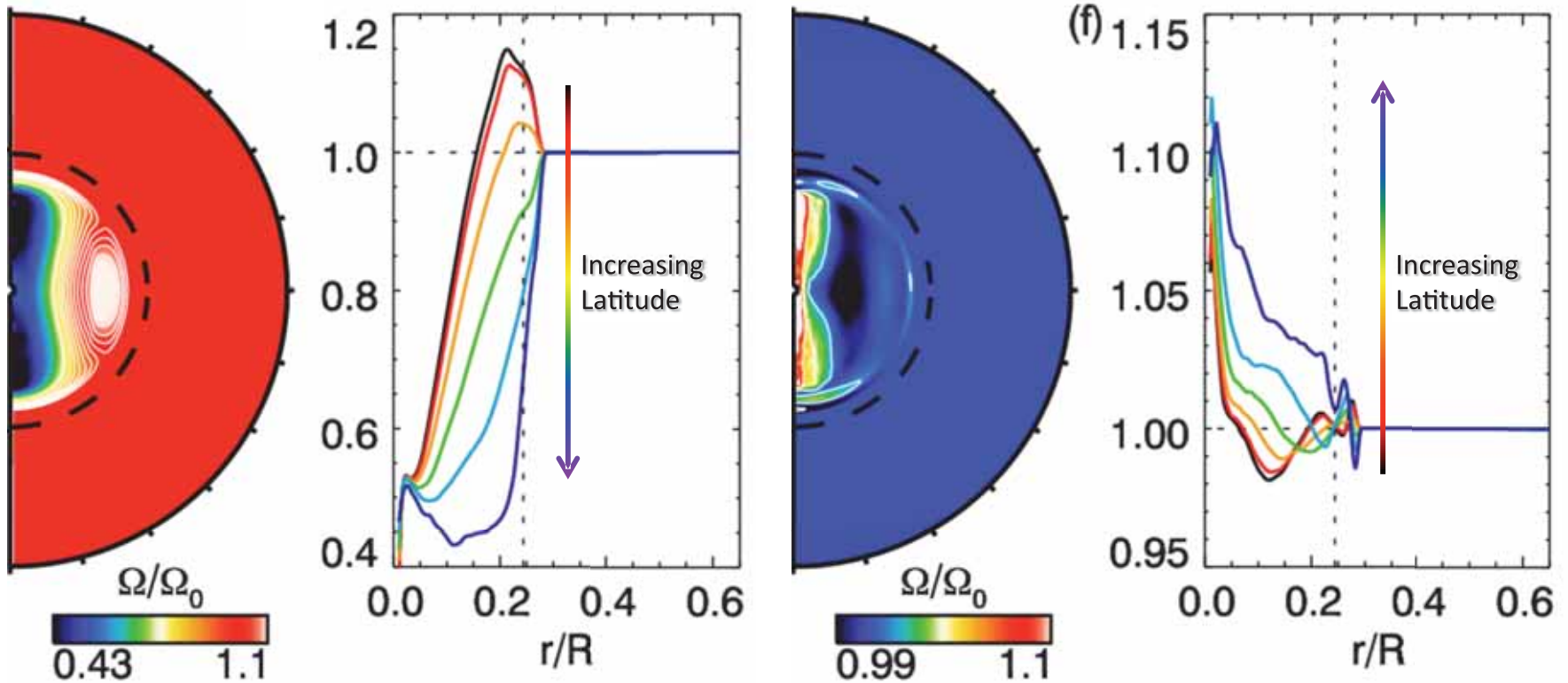


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# Hydrodynamics versus MHD

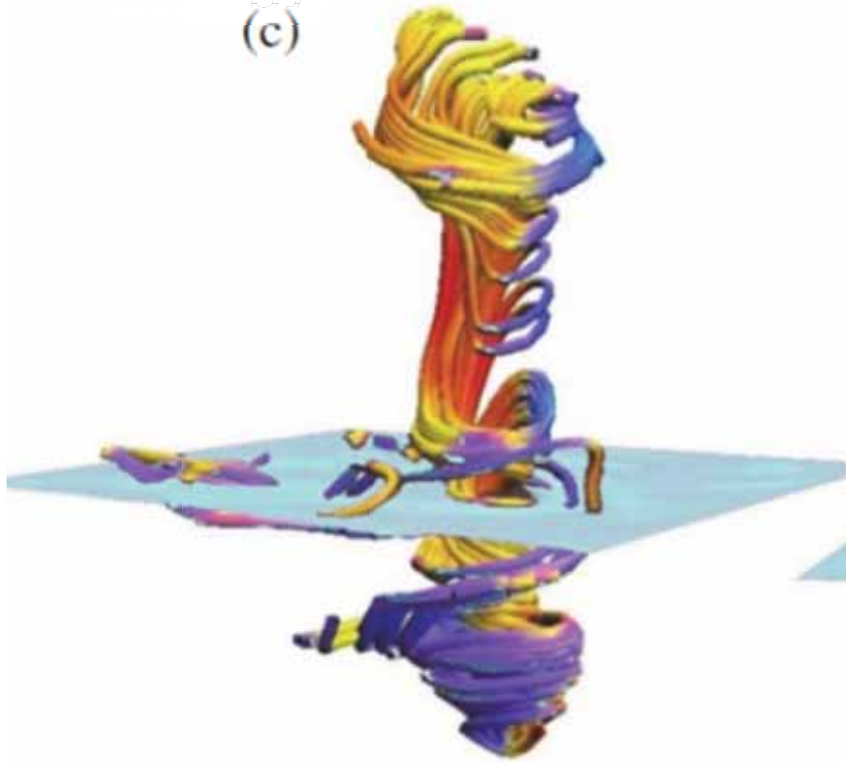
Marked difference in differential rotation

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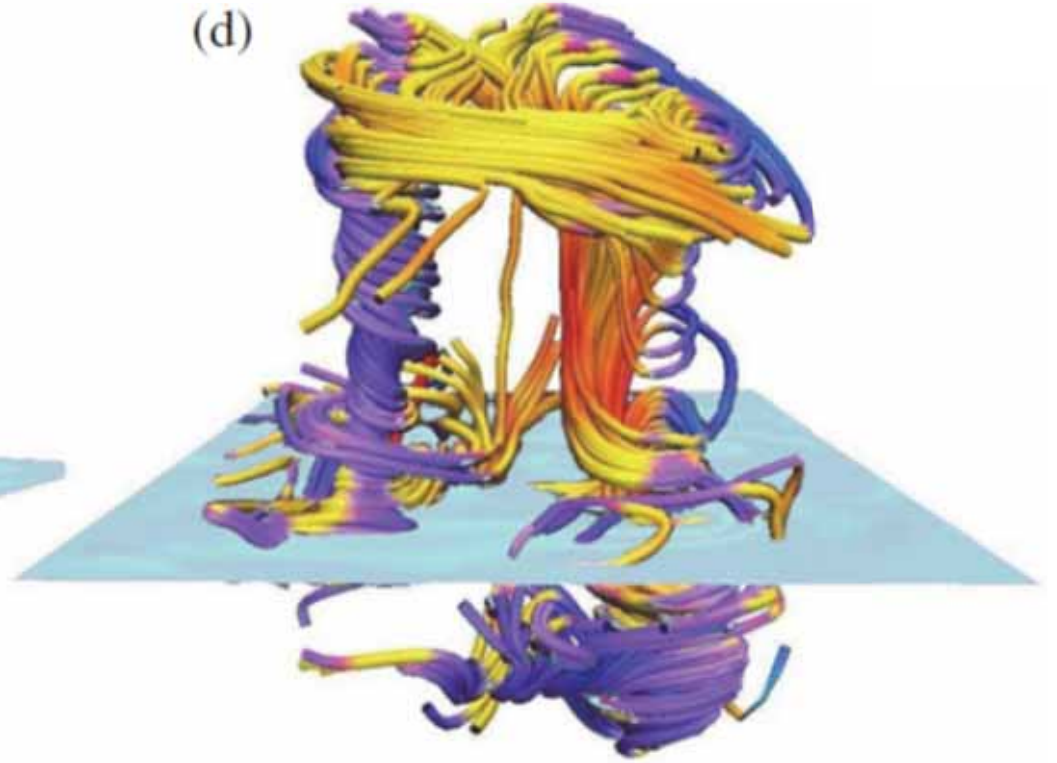


# Magnetic Fields and Their Energy

(c)



(d)



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## Properties of B-type Star Convection and Magnetism

Case	KE	KE <sub>DR</sub>	ME	FME	TME	ME/KE	B <sub>max</sub>	$\Delta\Omega_r/\Omega_0$
<i>H4</i>	73.1	66.4 (91.%)	–	–	–	–	–	0.495
<i>M4</i>	3.91	0.17 (4.5%)	4.08	3.71 (91.%)	0.30 (7.4%)	1.06	0.76	-0.078
<i>M8</i>	2.20	0.14 (6.2%)	4.52	4.19 (93.%)	0.20 (4.5%)	2.07	1.06	-0.017
<i>M16</i>	1.42	0.09 (6.5%)	5.42	5.17 (95.%)	0.15 (2.8%)	3.86	1.17	-0.012
<i>M64</i>	1.22	0.06 (5.9%)	7.33	6.95 (95.%)	0.12 (1.6%)	6.01	1.53	-0.013

KE = Kinetic Energy    ME = Magnetic Energy  
 $10^7 \text{ erg cm}^{-3}$          $10^7 \text{ erg cm}^{-3}$

B<sub>max</sub> in MG

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## Magnetostrophic Balance

Cases	$\Lambda$	$Rm'$	$\Lambda_D$	$Ro$	$Ro^{-1}\Lambda_D$	ME/KE
M4	330	2080	0.15	0.35	0.42	1.06
M8	493	1960	0.25	0.16	1.5	2.07
M16	383	1640	0.23	0.06	3.83	3.86

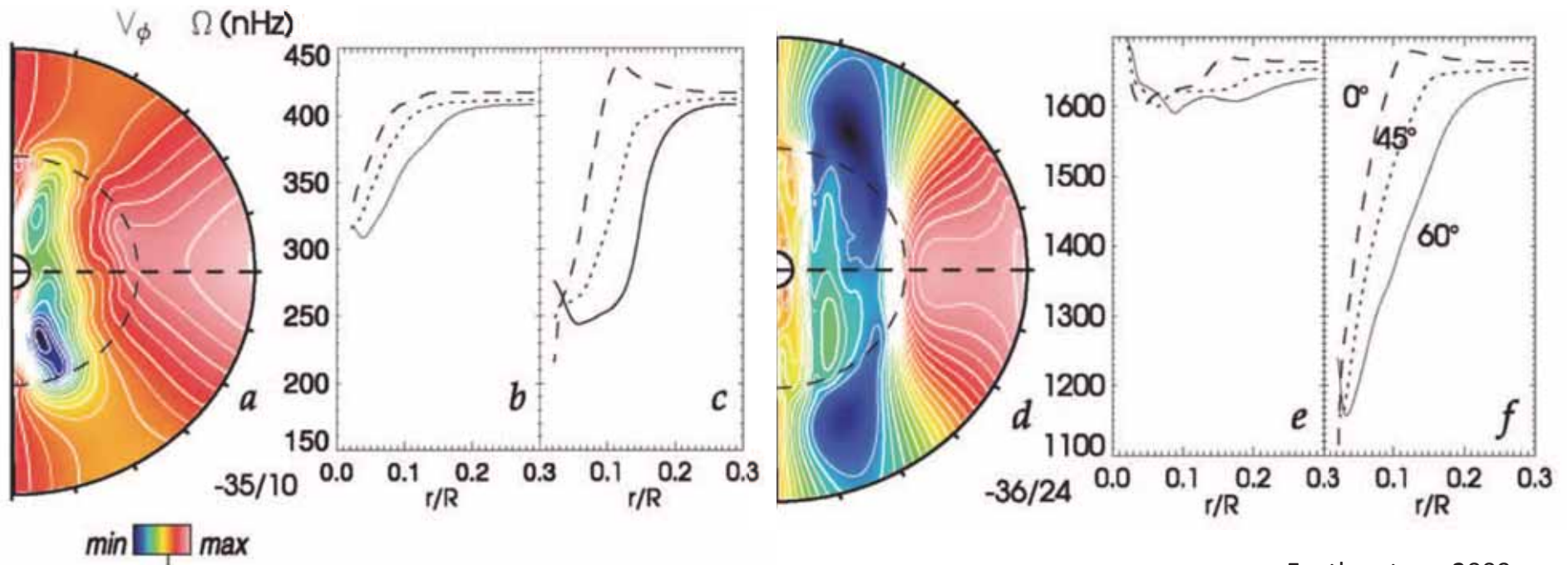
$$\Lambda_D = \frac{(1/4\pi)\nabla \times \mathbf{B} \times \mathbf{B}}{\rho 2\boldsymbol{\Omega} \times \mathbf{u}} = \frac{(1/8\pi)B^2}{\rho\Omega uL}$$

$$\Lambda = \frac{(1/8\pi)B^2}{\rho\Omega\eta} = \Lambda_D Rm$$

$$\Lambda_D = \frac{(1/8\pi)B^2}{\rho\Omega uL} = \frac{(1/8\pi)B^2}{(1/2)\rho(u^2)} Ro \quad \Rightarrow \quad \frac{ME}{KE} = \Lambda_D Ro^{-1}$$

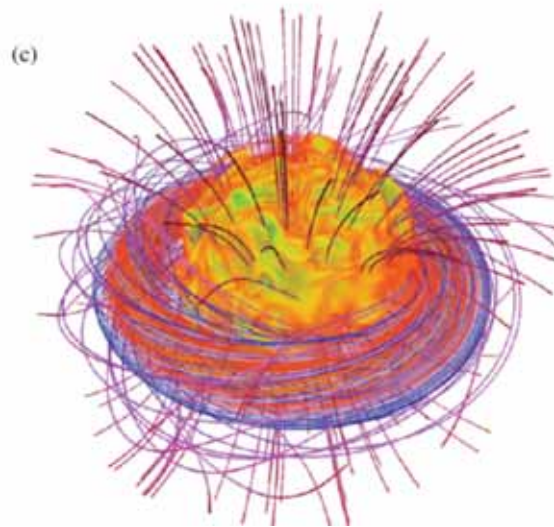
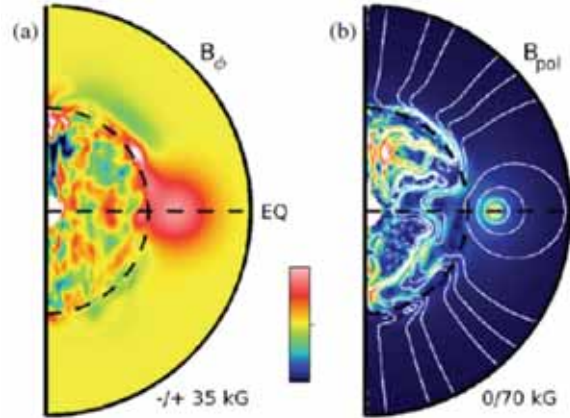
# Hydrodynamics versus MHD

Marked difference in differential rotation

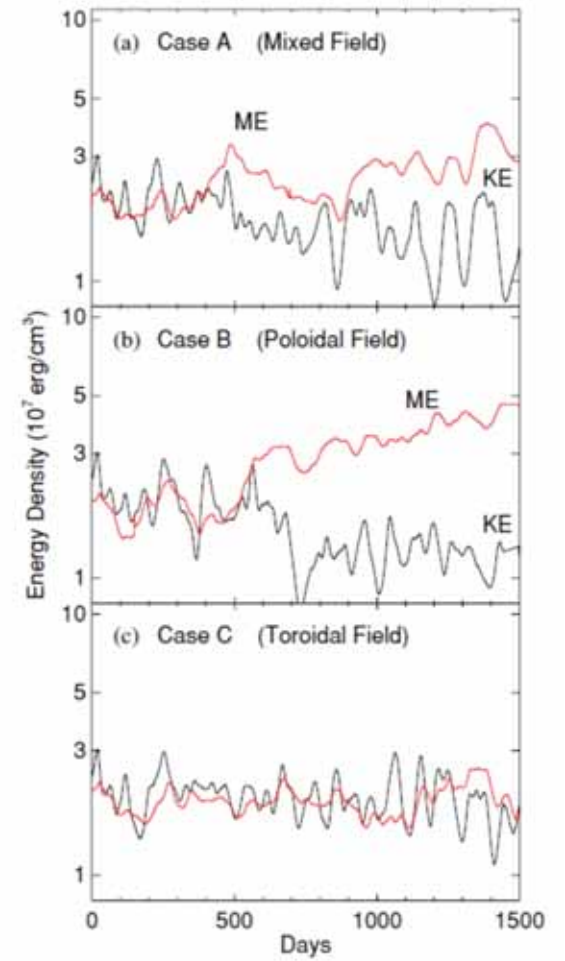


Featherstone 2009

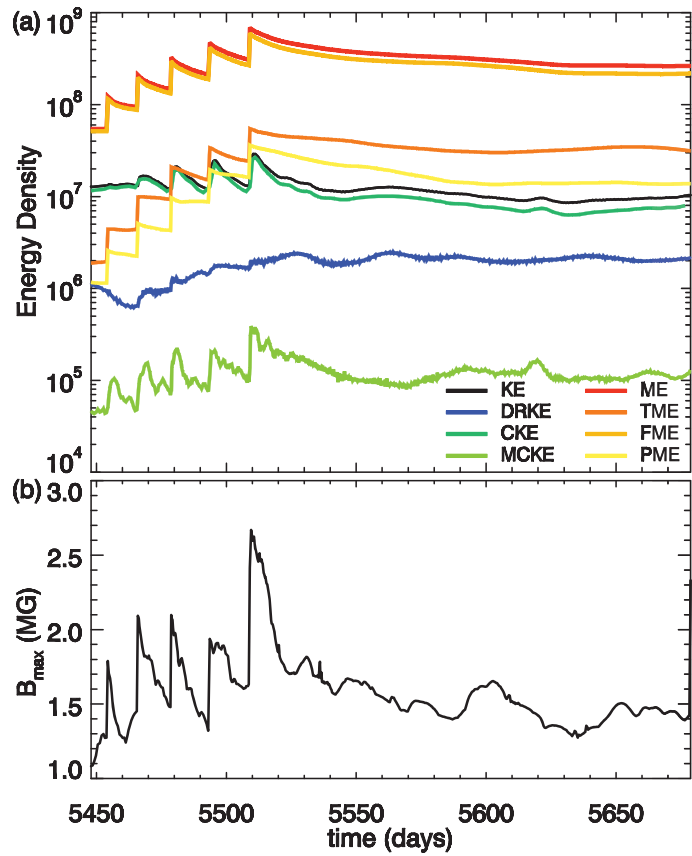
# Impact of Fossil Field Geometry



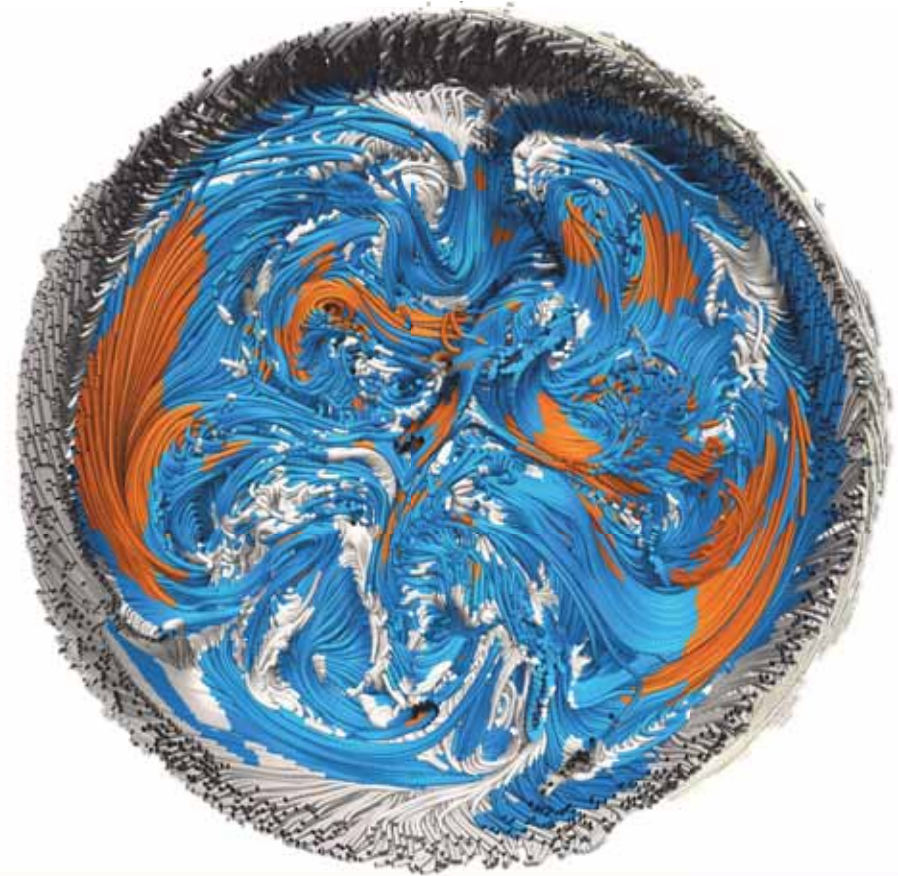
Featherstone 2009



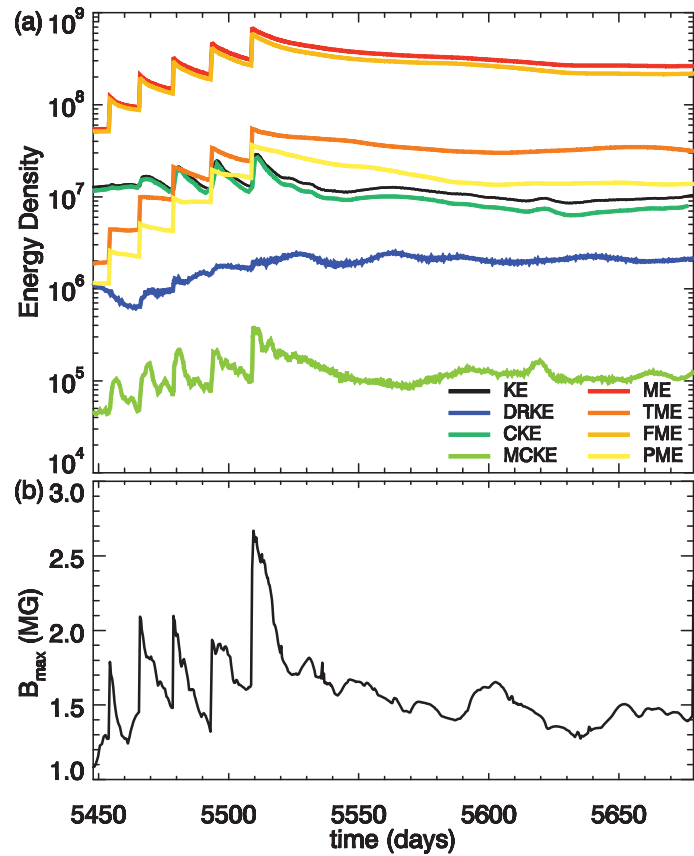
## Impact of Initial Conditions



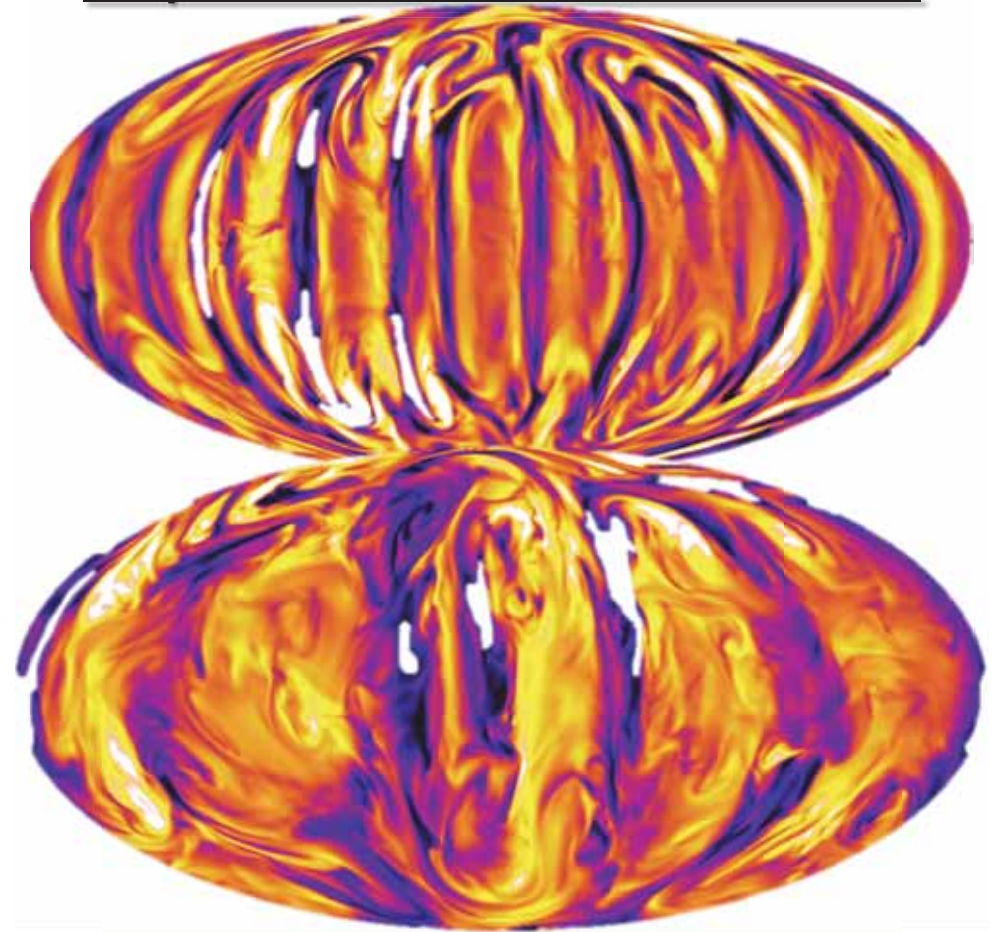
Augustson 2014



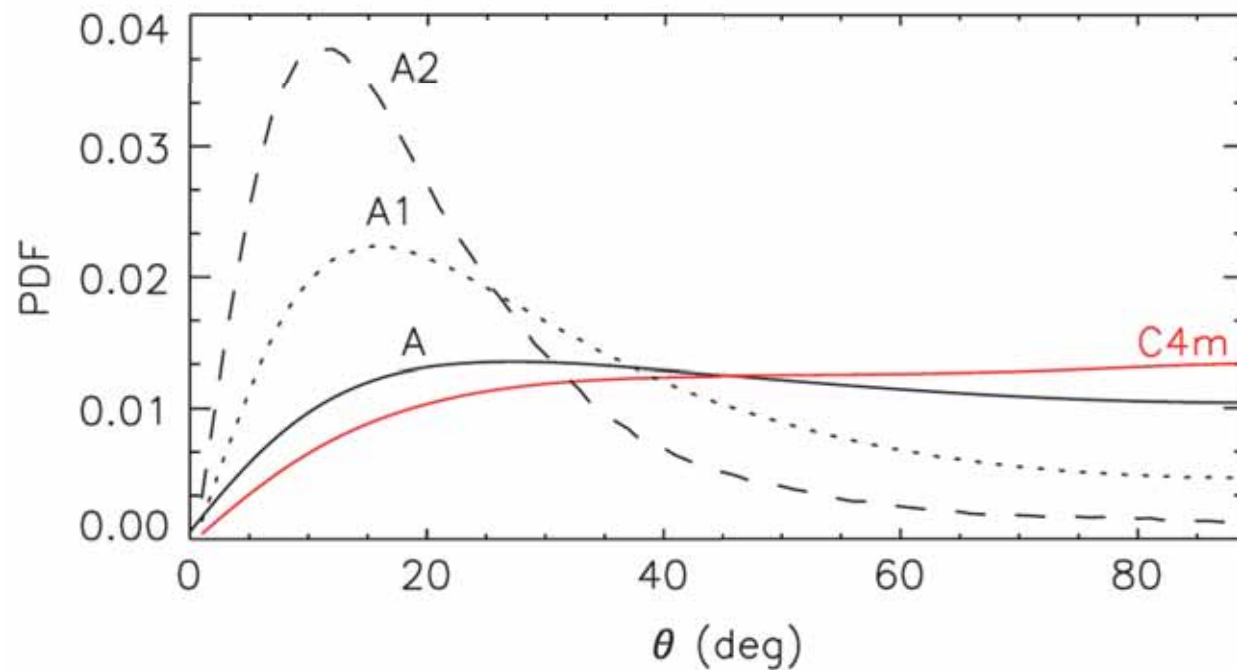
## Impact of Initial Conditions



Augustson 2014



## How can such states exist?



$$\theta = \cos^{-1}(v \cdot B / |v||B|)$$

Increasing  
superequipartition  
levels lead to  
increasing alignment

## Summary and Outlook

- Rossby number

  - Rotational scaling of: cycle period and activity

  - What are appropriate Rossby numbers?

  - Stellar convective amplitudes & energy transport?

- Strong internal magnetic states

  - Impacts upon transport & field morphology

  - How far can super-equipartition be pushed?

- Influence of a stable radiative interior?

- Is there such a thing as a nonmagnetic star?

