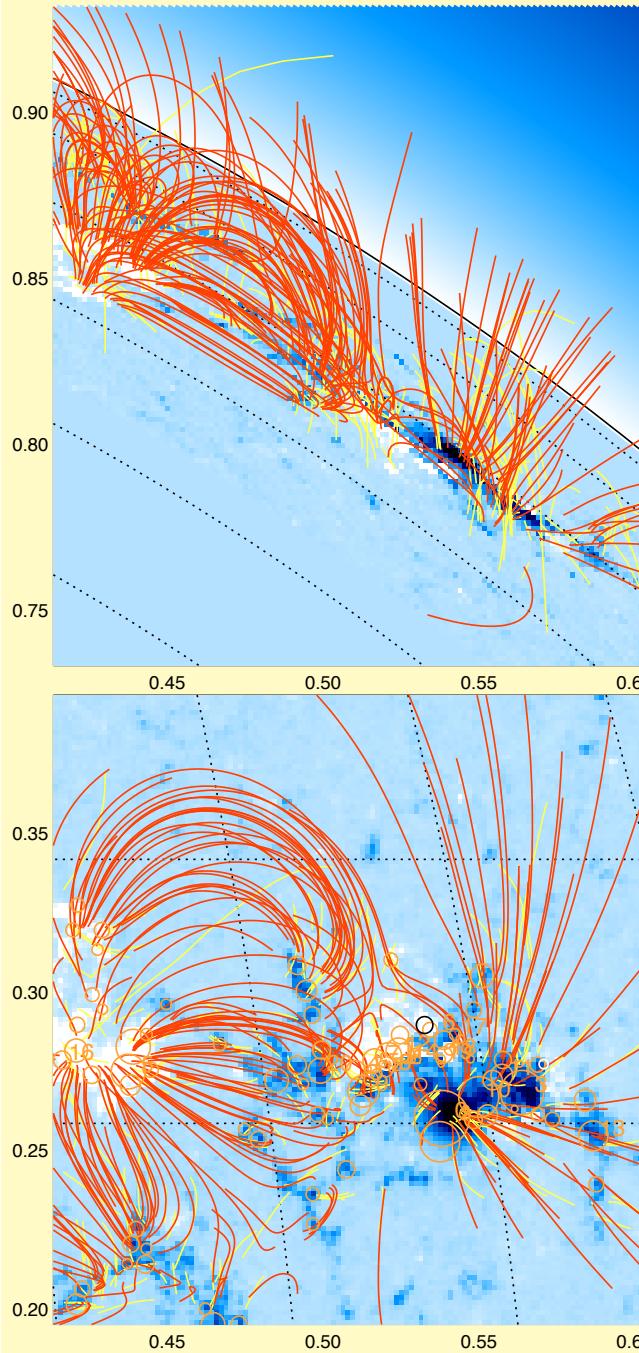


20140329_170500, EVENT=592, FRAME=



Tracing the Chromospheric & Coronal Magnetic Field with AIA, IRIS, IBIS & ROSA

Markus J. Aschwanden (LMSAL)

Bart De Pontieu (LMSAL)

Kevin Reardon (NSO)

Dave Jess (QUB)

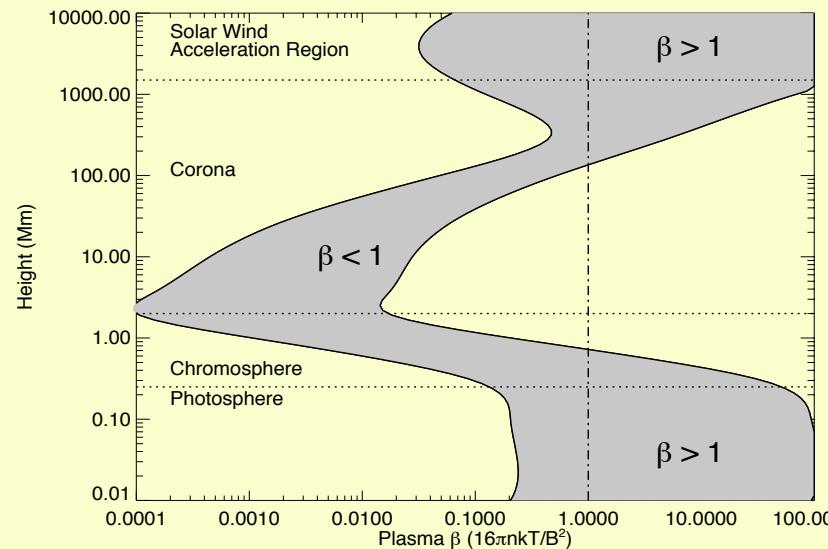
*ALMA-IRIS-DKIST Workshop, March 15, 2016
NSO, Boulder, Colorado*

[http://www.lmsal.com/~aschwand/
2016_chromo_aschwanden.ppt](http://www.lmsal.com/~aschwand/2016_chromo_aschwanden.ppt)

Outline of Talk:

- 1) Previous work on chromospheric magnetic fields
- 2) The VCA-NLFFF method to compute magnetic fields:
 - 2.1 Potential field from buried magnetic sources
 - 2.2 Automated tracing of curvi-linear features
 - 2.3 Forward-fitting of nonpotential magnetic field
- 3) Data Analysis:
 - AIA/SDO, HMI/SDO
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- 4) Discussion and conclusions:
 - Suitability of chromospheric field tracing
 - Altitudes of chromospheric magnetic field tracers
 - Coronal vs. chromospheric free energy

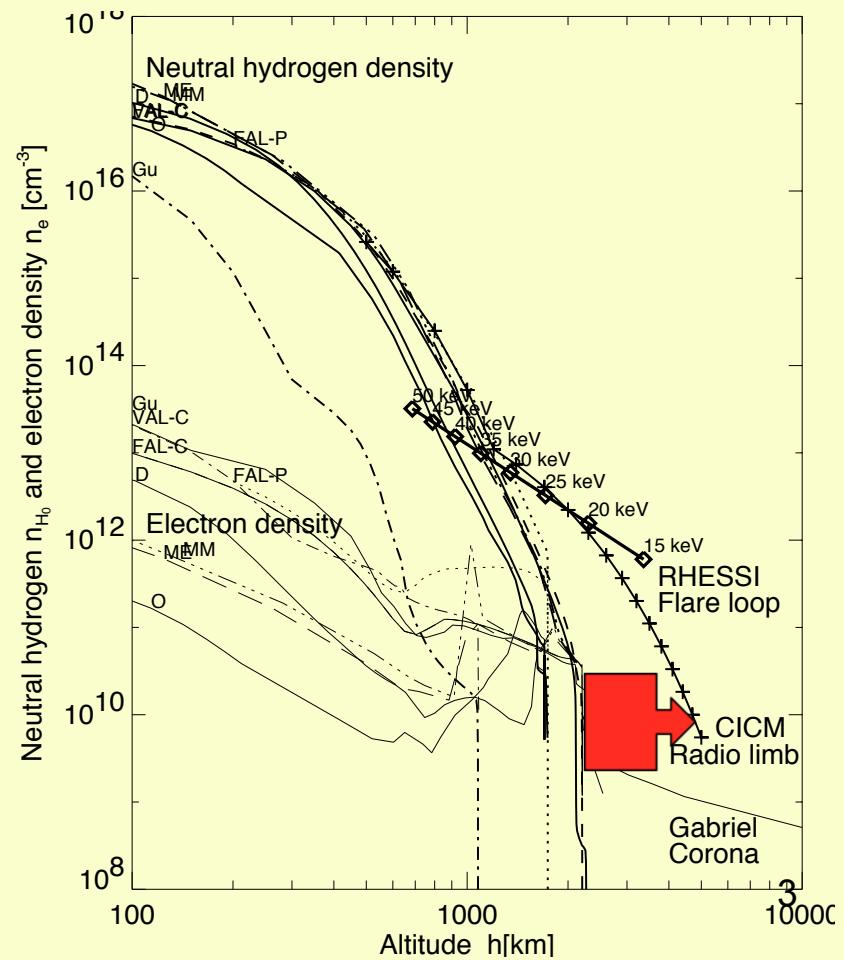
Static and Dynamic Chromospheric Models



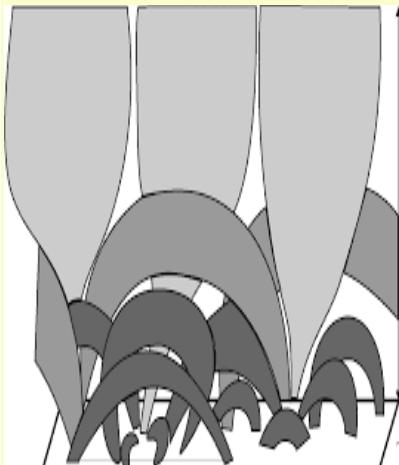
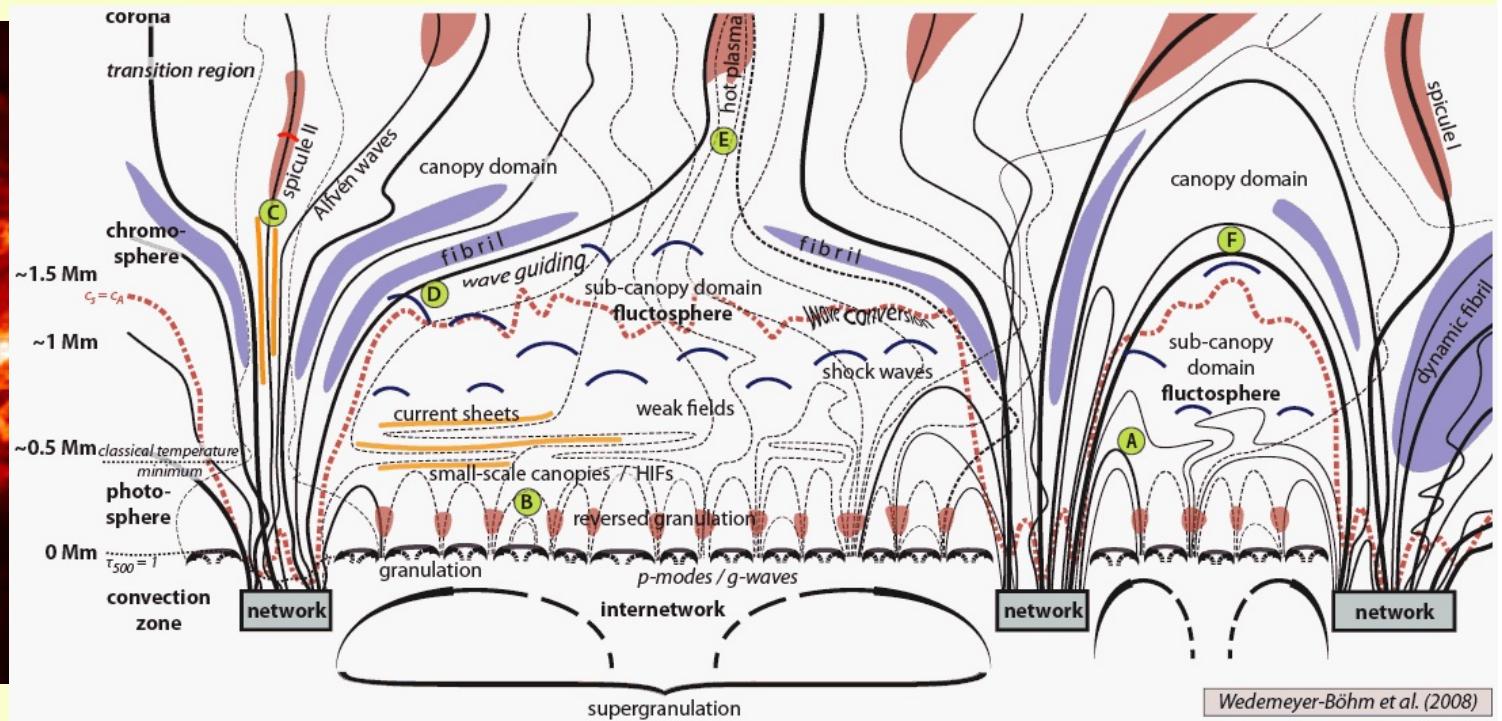
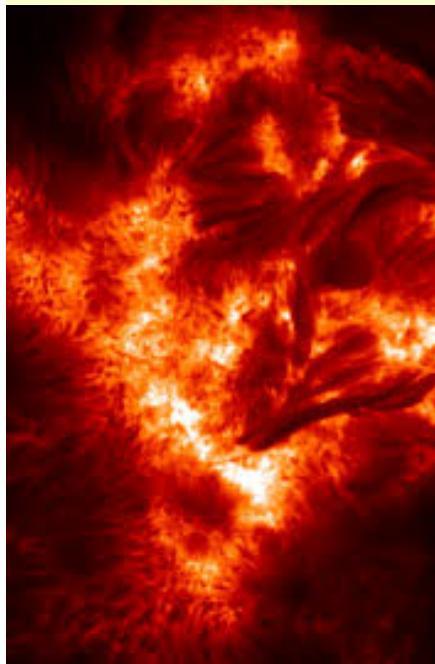
Chromospheric density models:

- VAL-C (Vernazza, Avrett, & Loeser 1981)
- FAL-C (Fontentla, Avrett & Loeser 1990)
- Gu et al. 1997, Maltby et al. 1986,
- Ding & Fang 1989; Obridko & Staude 1988
- Gabriel 1976 (canopy model),
- CICM Caltech Irreference Chromospheric model
- radio sub-millimeter limb observations
(Ewell et al. 1993);
- RHESSI thick-target model, energy-dependent height centroids → chromospheric density model
(Aschwanden, Brown & Kontar 2002)
- Dynamic chromosphere extends up to ~5000 km

The plasma β -parameter is < 1 in most coronal and upper chromospheric regions. Gary 2001



Nomenclature of chromospheric structures



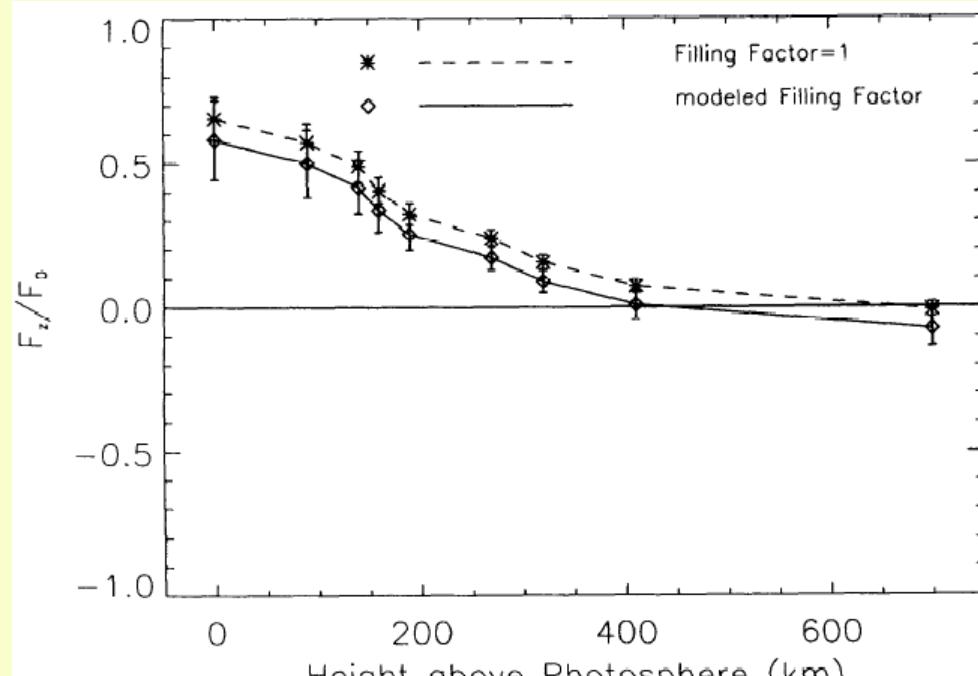
Chromospheric structures:

- Footpoints of field-aligned coronal loops
- Fibrils in active regions and sunspot penumbra
- Spicules (when observed near and above limb)
- Mottles (when observed in Quiet Sun)

(DePontieu et al. 2007; Pietrarila et al. 2009)



The lower chromosphere is not force-free



Metcalf et al. 1995

At what height is the transition between plasma β -parameter >1 to < 1 ?

Setting the total Lorentz force equal to the magnetic pressure force,

Metcalf et al. (1995) found that chromosphere is not force-free for $h < 400$ km.
The implication is that magnetic field extrapolation from photospheric
data violates the force-free assumption

→ Tracers in the upper chromosphere and corona are needed

Link between chromospheric network and corona

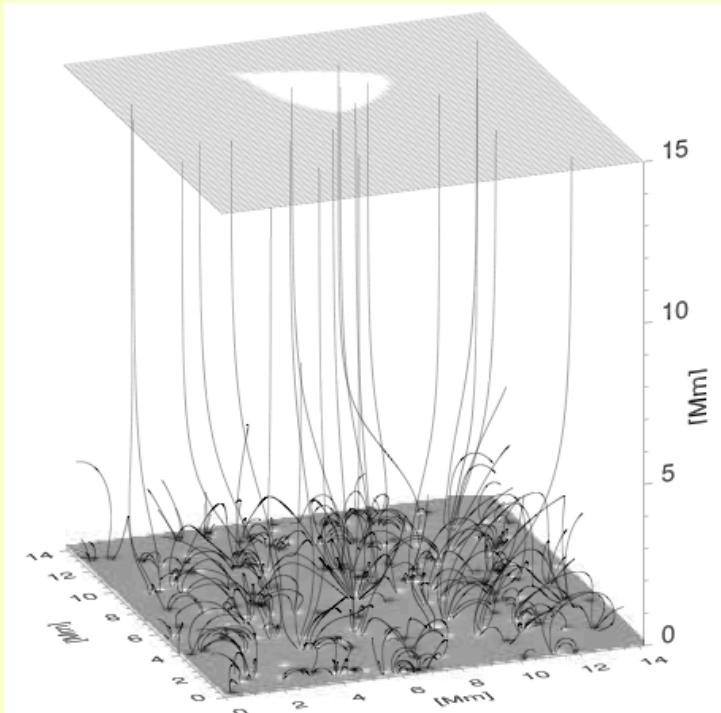


Fig. 1. Composite plot of the magnetic field at the bottom (lower BC), field lines of the extrapolated magnetic field, and a mask of the area at 15 Mm height that is magnetically connected to the central strong network magnetic patch (white).

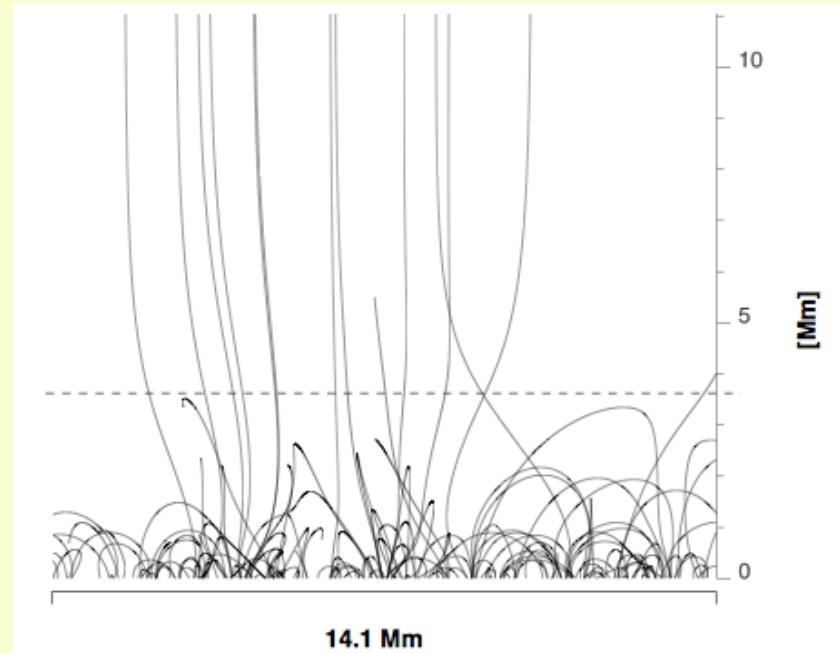


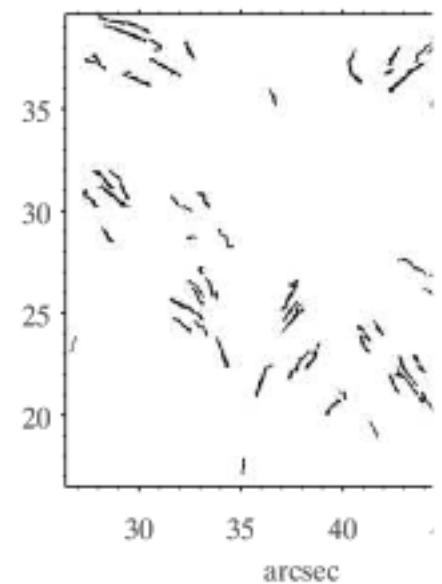
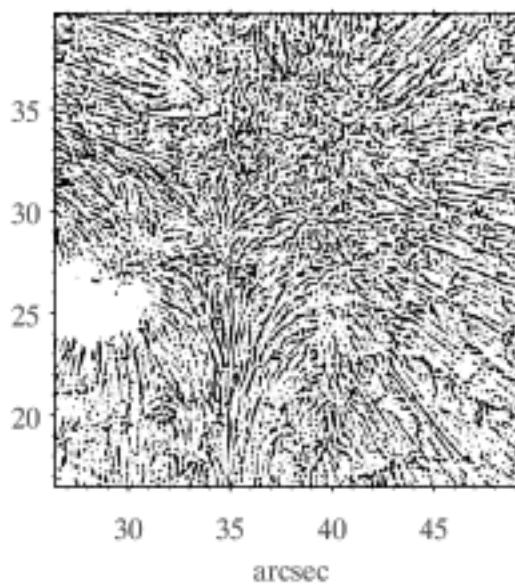
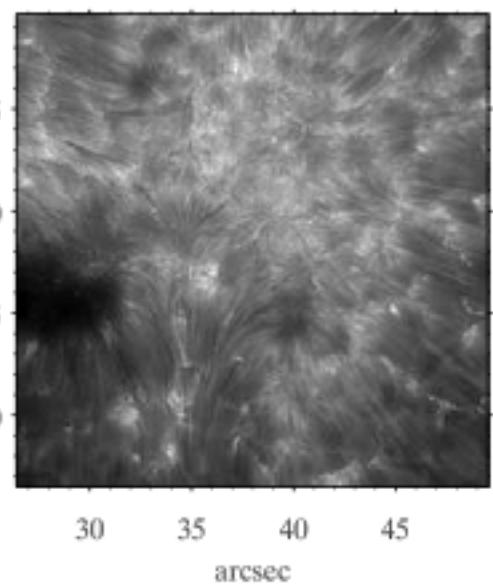
Fig. 3. A selection of field lines starting from the internetwork are drawn for an unsigned mean internetwork flux density of 60 Mx/cm². Here the computational domain is viewed from the side. The dashed line indicates the maximum height of the highest-reaching closed field line from this selection. See Sect. 3.2.

Schrijver & Title 2002; Jendersie & Peter 2006

Many magnetic field lines rooted in small-scale network (salt & pepper) field concentrations close inside the lower chromosphere and do not extend up into the corona, which hampers magnetic field extrapolation methods
→ tracing of upper chromospheric and coronal structures is needed.

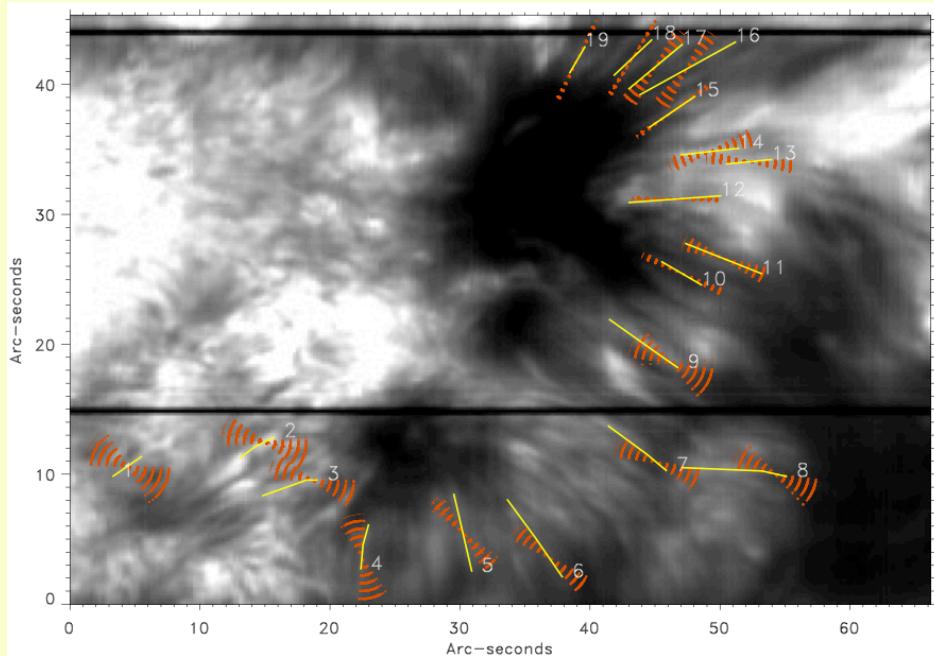
Chromospheric magnetic field

- 137 solar active regions observed with NSO/KP in Ca II 8542 Å (most sensitive at $h=800$ km) reveal non-potentiality of magnetic field when comparing extrapolated with measured field.
(Harvey et al. 1999; Choudhary et al. 2001)
- The Ca II 8542 Å line is particularly suited to observe the fine structure of fibril-like features, to measure their geometry and orientation, and to determine their magnetic field alignment and non-potentiality.

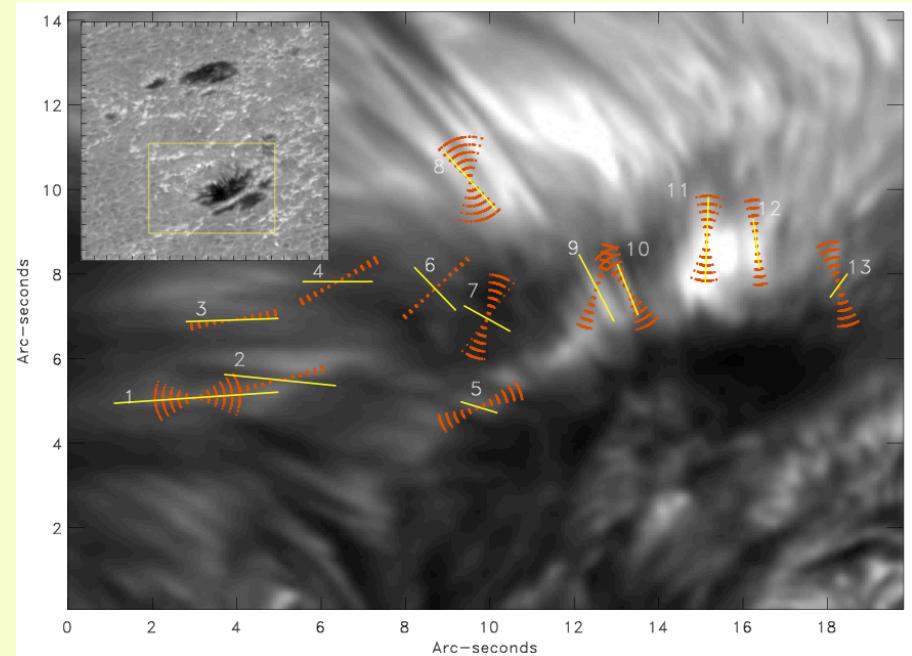


Pietarila et al. 2009

Do chromospheric fibrils trace the magnetic field ?



Ca II 8542 Å, SPINOR, Stokes Q and U profile
De la Cruz Rodriguez & Socas-Navarro (2011)

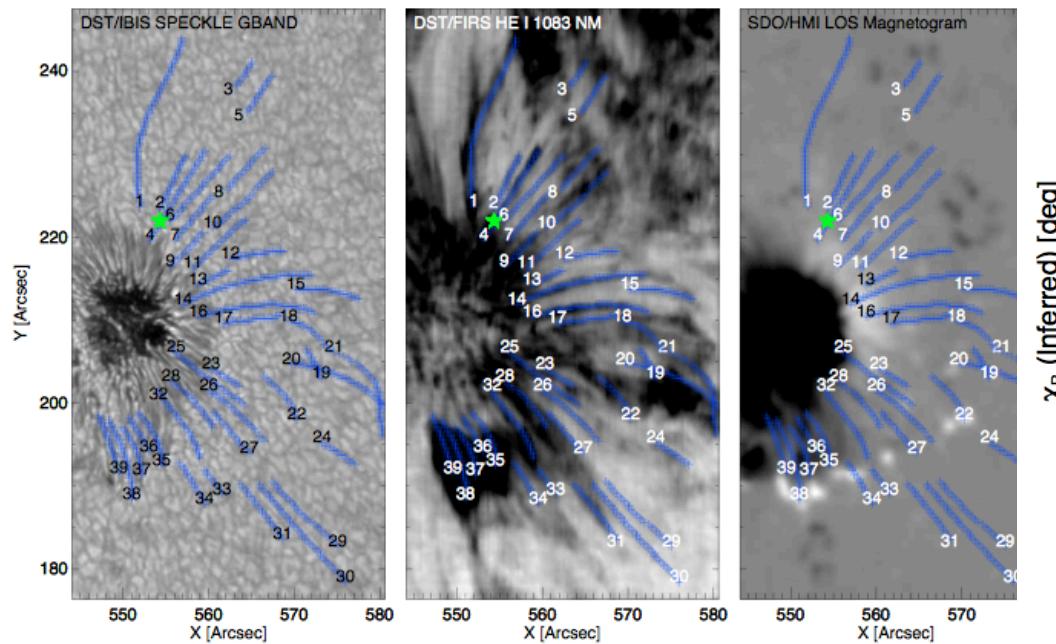


wing of Ca II 8542, CRISP
De la Cruz Rodriguez & Socas-Navarro (2011)

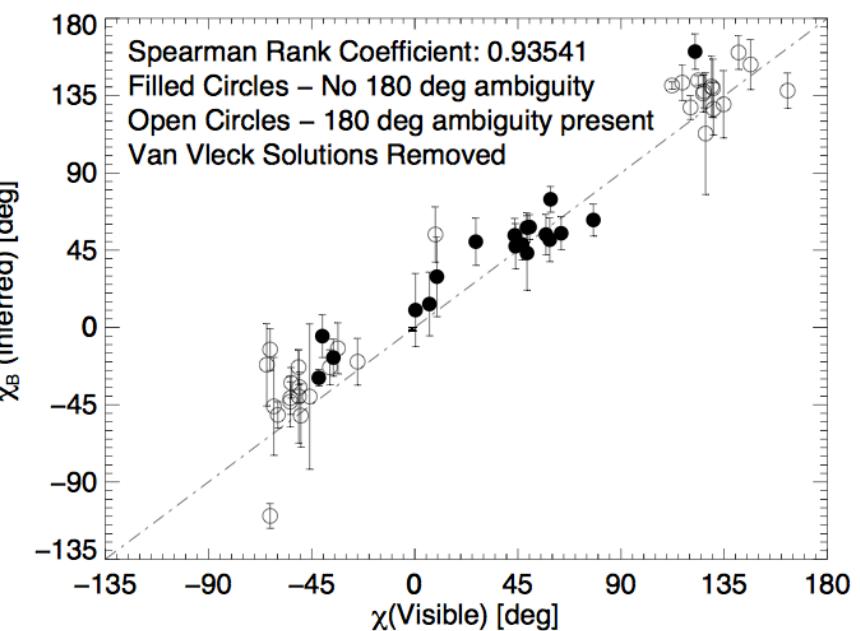
Spectropolarimetric observations of Ca II lines

Indicate the chromospheric fibrils trace the field mostly, but not always

Do chromospheric fibrils trace the magnetic field ?



39 manually traced fibrils, He I, CRISPEX,
Schad, Penn, & Lin (2013)



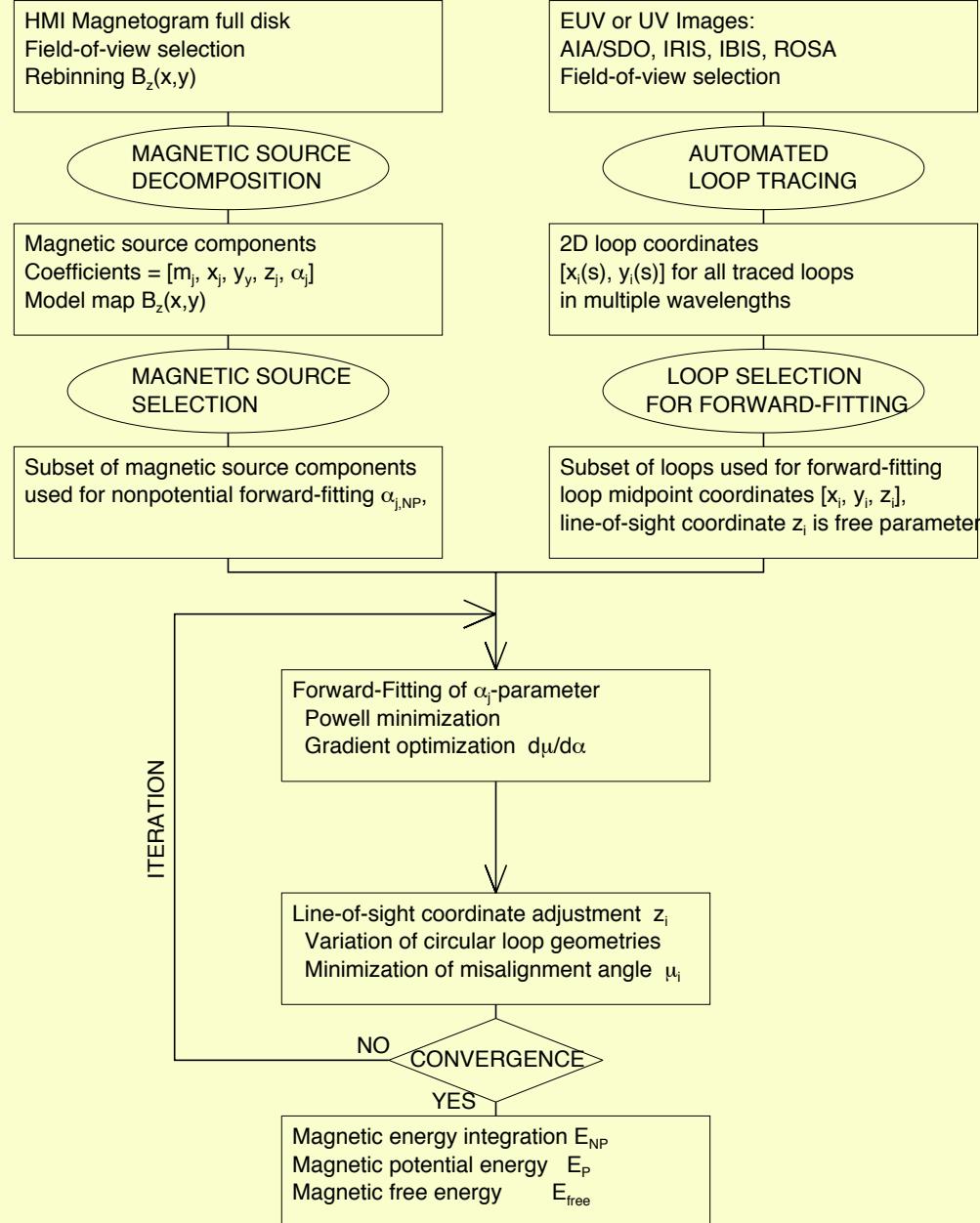
Magnetic field direction vs. projected angle of fibrils
Schad, Penn, & Lin (2013)

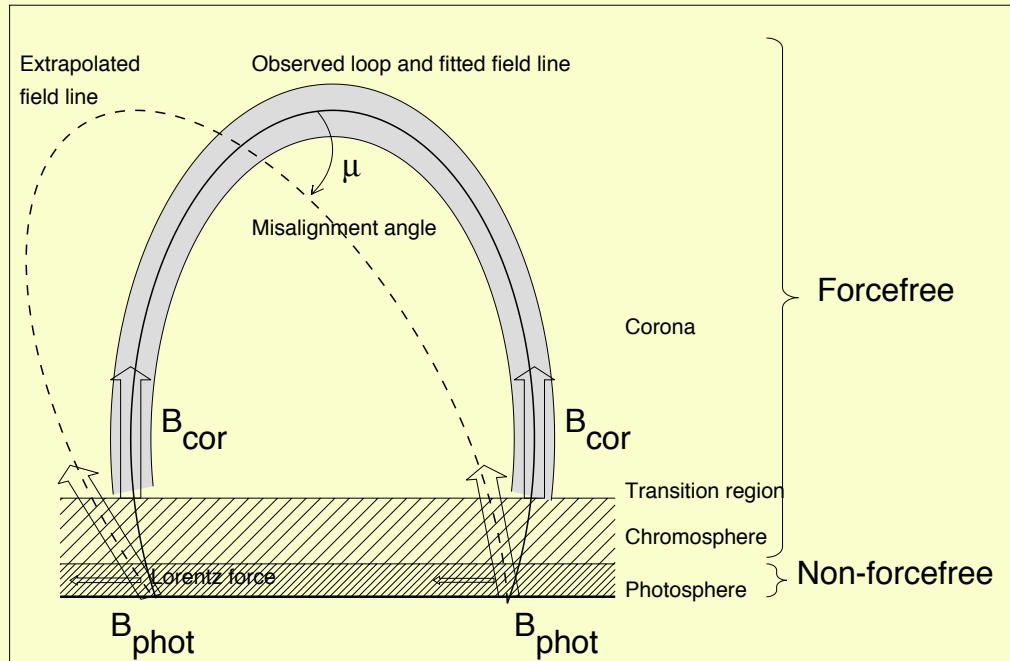
Full vector magnetometry of super-penumbral fibrils observed in He I 10830 Å, H-alpha 6563 Å, and Ca II 8542 Å (at DST) show that the Projected angle of the fibrils is aligned with the magnetic field within ± 10 deg.

Outline of Talk:

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Vertical Current Approximation Non-Linear Force-Free Field (VCA-NLFFF) Code





Potential field: PFSS code (no free energy available for flares or coronal heating)

Non-Potential field codes:

(1) Standard-NLFFF codes (extrapolation ignores non-forcefree zones, use vector-magnetograph LOS + transverse field, but are misaligned to geometry of coronal loops)
 (e.g. Wheatland et al. 2000; Wiegmann 2004; Grad & Rubin 1958)

(2) VCA-NLFFF code: Forward-fitting of analytical NLFFF approximation to coronal loops, transverse field is free parameter and can minimize misalignment with coronal loops)
 (Aschwanden 2013, Aschwanden, Sun, & Liu 2014)

Photospheric vs. Coronal Magnetic Field Measurement Methods

Standard NLFFF

(Wiegelmann et al. 2008)

Input: Photospheric 3D vectors
 (B_x, B_y, B_z)

Method: Force-free α -parameter optimization

Problems: Non-forcefree photosphere
 \rightarrow preprocessing
Misalignment of coronal loops

Computation time:
2-12 hrs/run

VCA-NLFFF

(Aschwanden 2013)

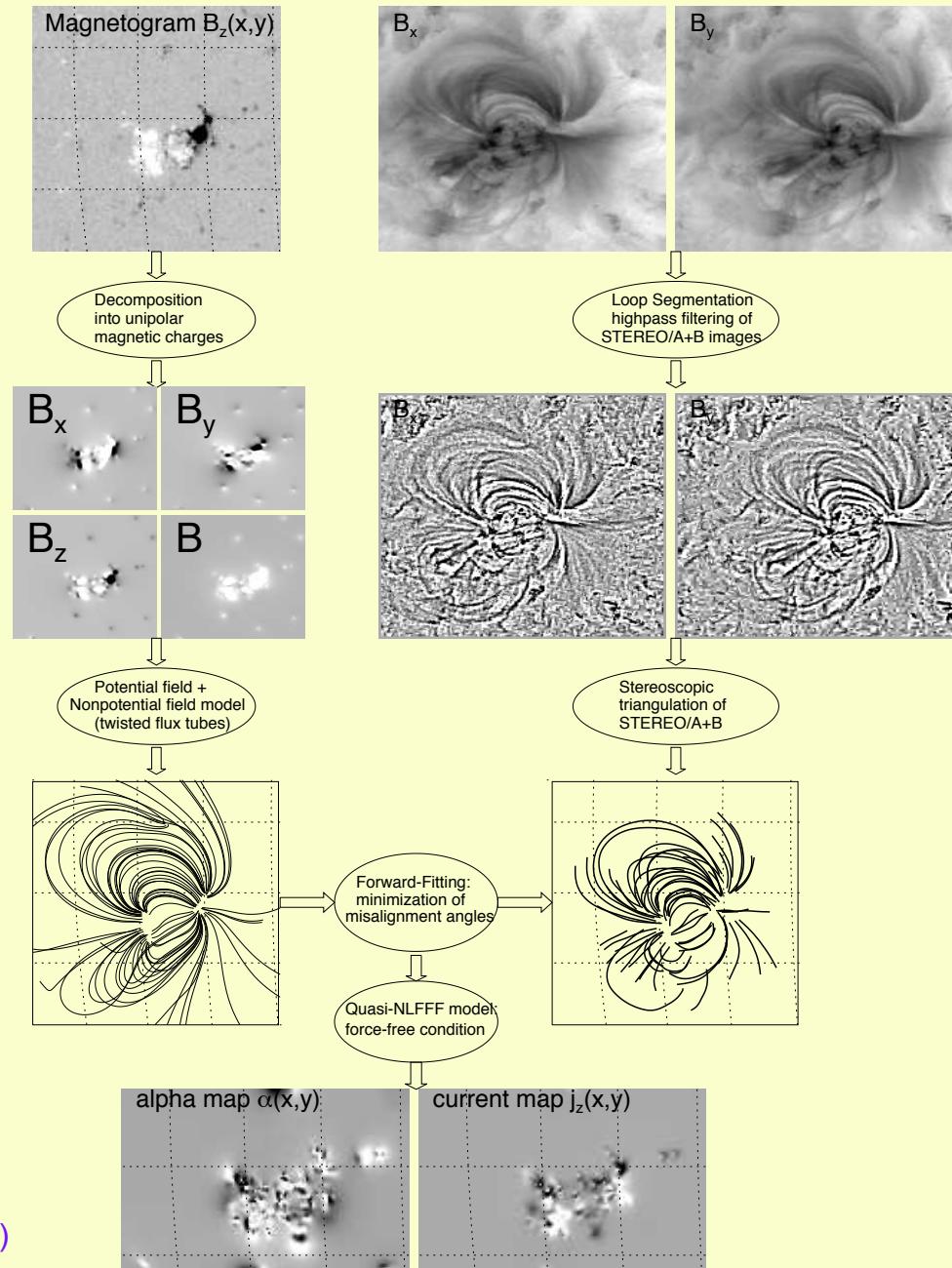
Photospheric B_z magnetogram
Coronal loop coordinates
 $[x(s), y(s)]$ or $[x(s), y(s), z(s)]$

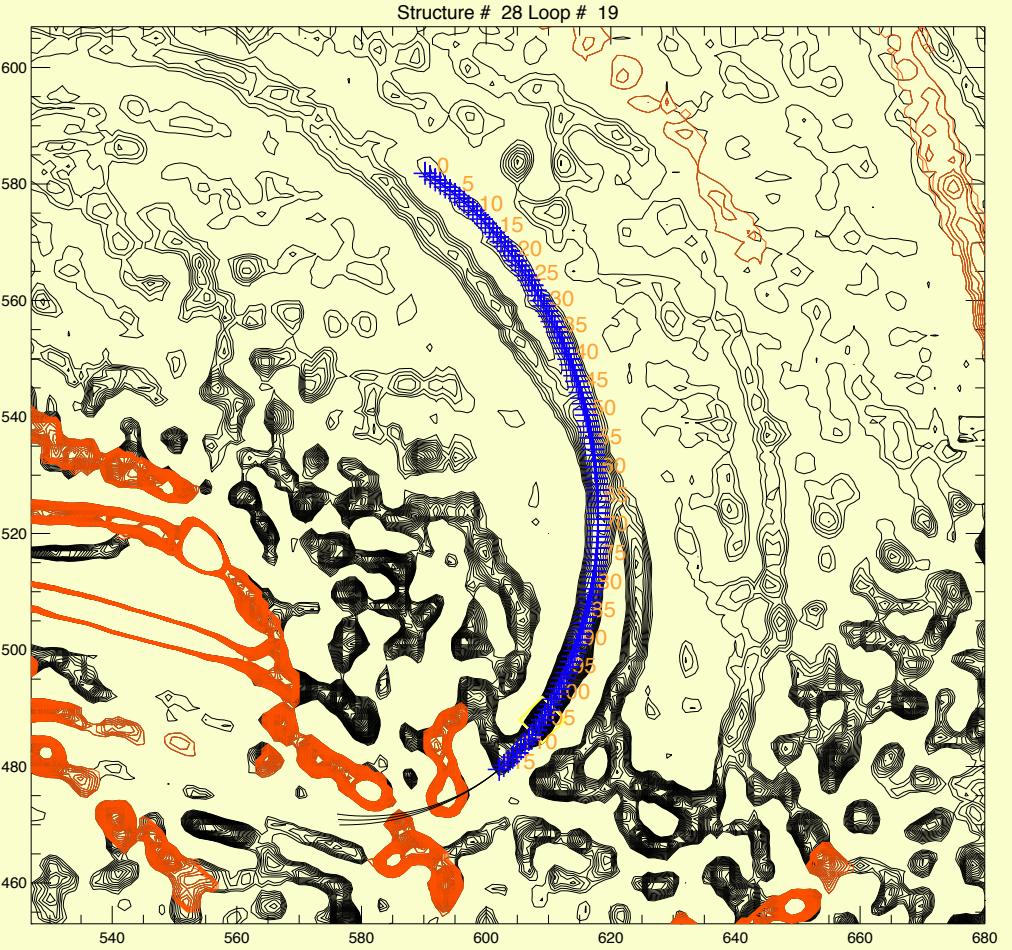
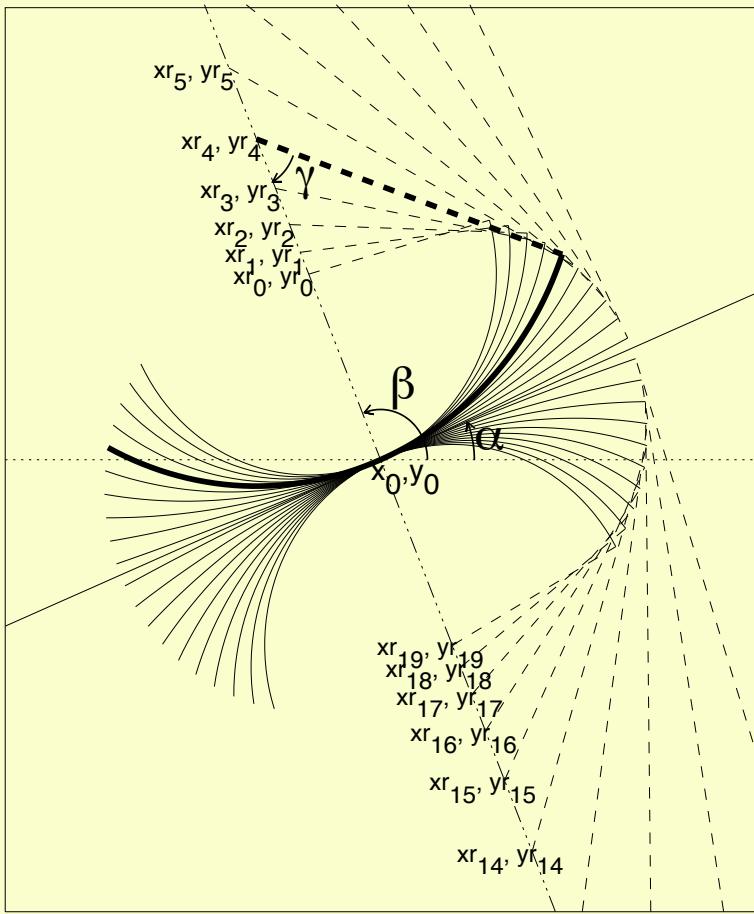
Forward-fitting of analytical
NLFFF solution based on the
Vertical Current Approximation

Sparse loops near sunspots,
false loop detection in moss areas,
neglects horizontal currents

1-3 min/run

VCA-NLFFF with stereoscopy (3D) or without (2D loop coordinates)



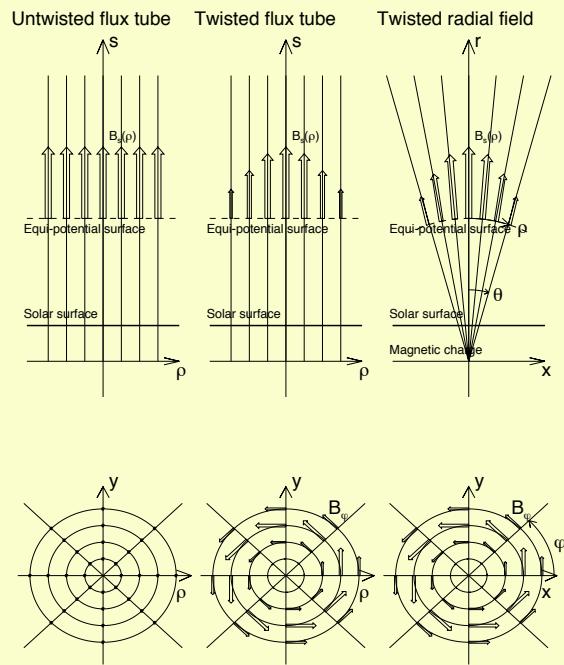


OCCULT-2 Code:
Local curvature radius provides guiding of directional changes in tracing a curvi-linear structure

Challenges:

- crossing loops
- data noise
- background (confusion moss)
- saturation, pixel bleeding
- entrance filter diffraction pattern

The Vertical-Current Approximation Non-Linear Force-Free Field Method



Approximative nonlinear force-free solution (neglecting second-order terms)

$$\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 B_r) \approx 0 , \quad (26)$$

$$\frac{1}{r \sin \theta} \frac{\partial}{\partial \theta} (B_\varphi \sin \theta) = \alpha B_r , \quad (27)$$

$$-\frac{1}{r} \frac{\partial}{\partial r} (r B_\varphi) \approx 0 , \quad (28)$$

$$-\frac{1}{r} \frac{\partial B_r}{\partial \theta} \approx \alpha B_\varphi . \quad (29)$$

Ansatz for azimuthal component

$$B_\varphi = B_r b r \sin \theta , \quad (30)$$

differential equation

$$\frac{\partial}{\partial \theta} [B_r (1 + b^2 r^2 \sin^2 \theta)] = 0 . \quad (31)$$

Solution of differential equation (neglecting second-order terms)

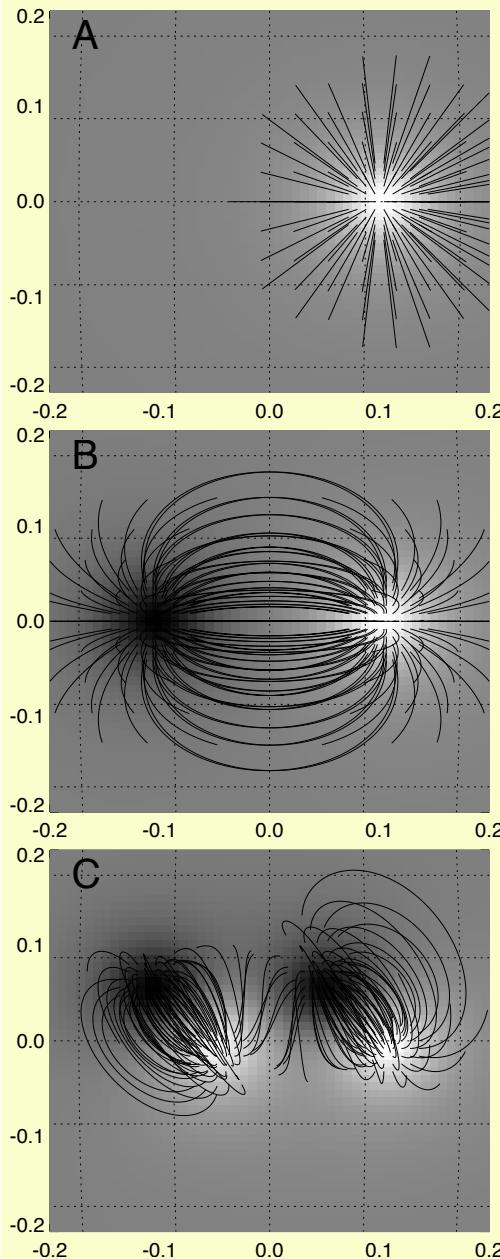
$$B_r(r, \theta) = B_0 \left(\frac{d^2}{r^2} \right) \frac{1}{(1 + b^2 r^2 \sin^2 \theta)} , \quad (32)$$

$$B_\varphi(r, \theta) = B_0 \left(\frac{d^2}{r^2} \right) \frac{b r \sin \theta}{(1 + b^2 r^2 \sin^2 \theta)} , \quad (33)$$

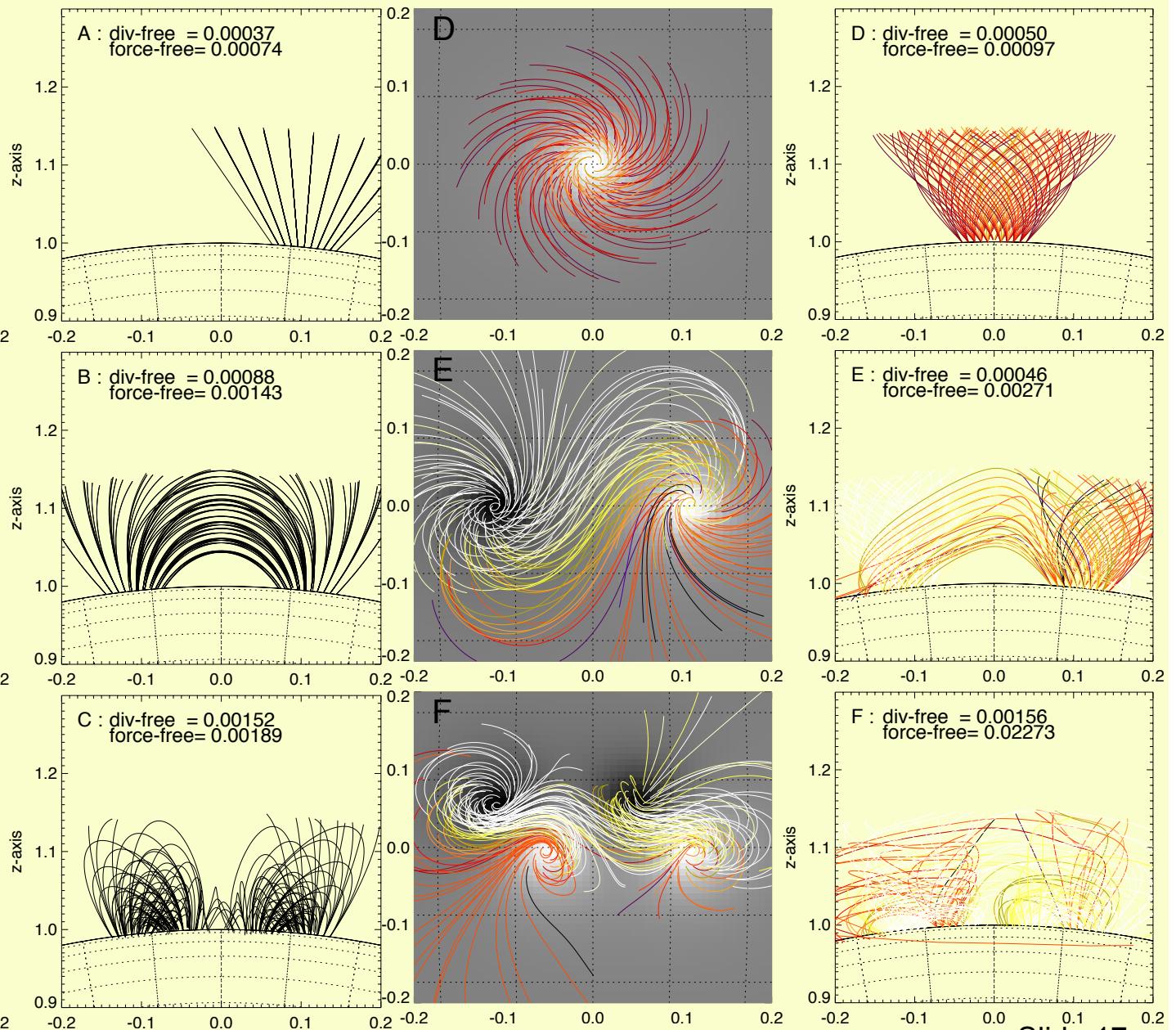
$$B_\theta(r, \theta) \approx 0 , \quad (34)$$

$$\alpha(r, \theta) = \frac{2b \cos \theta}{(1 + b^2 r^2 \sin^2 \theta)} . \quad (35)$$

Untwisted (potential) fields

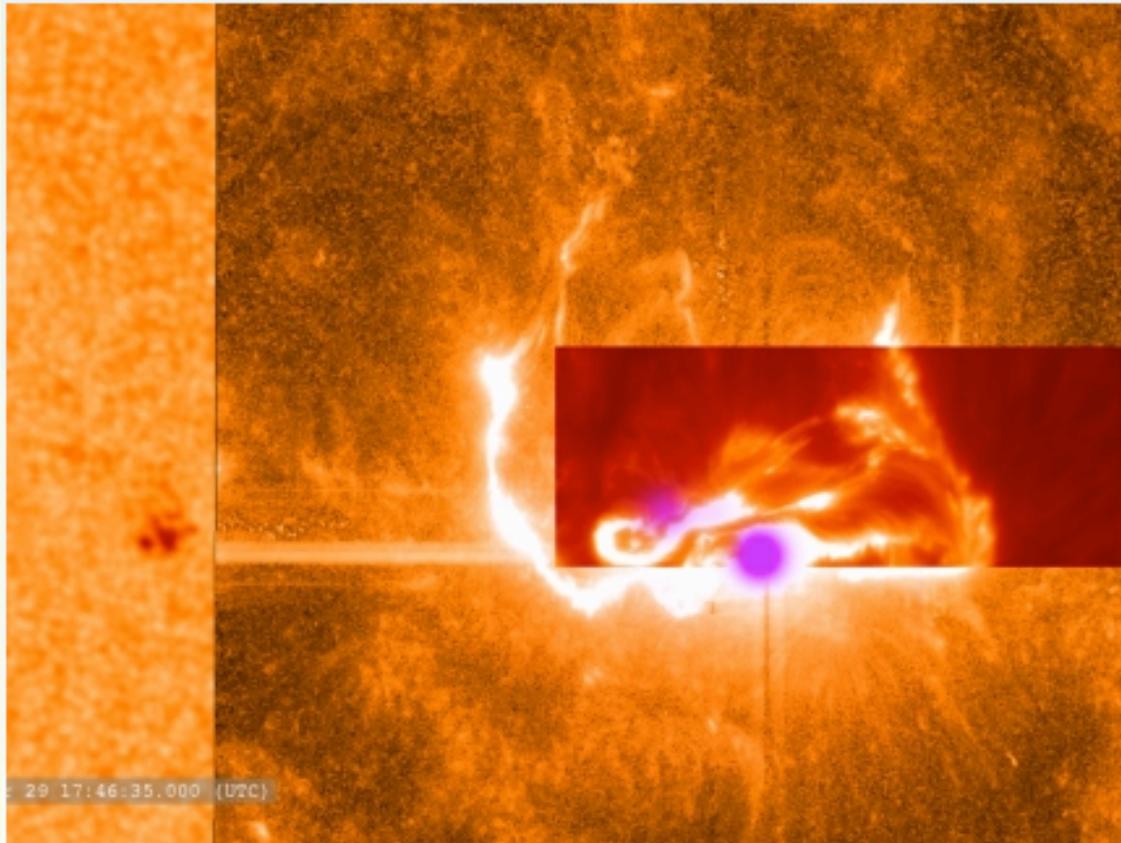


Twisted (non-potential) fields



Outline of Talk:

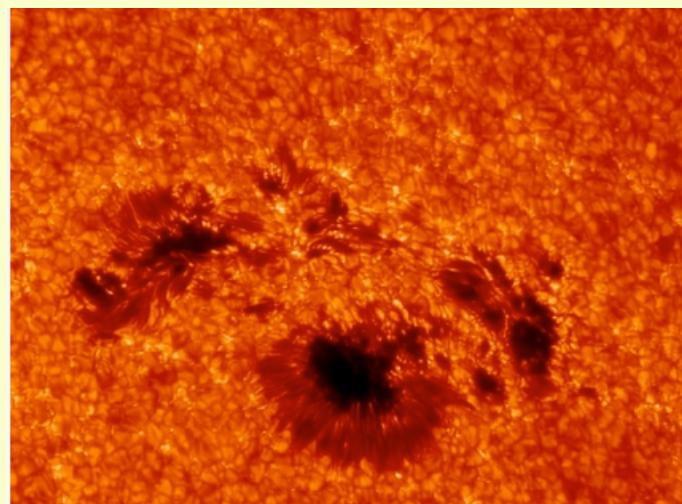
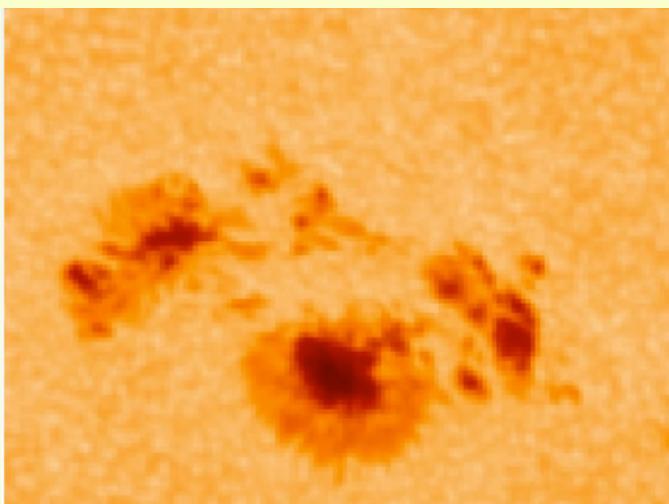
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March 29 X-class Flare - 1

This combined image shows the March 29, 2014, X-class flare as seen through the eyes of different observatories. SDO is on the bottom/left, which helps show the position of the flare on the sun. The darker orange square is IRIS data. The red rectangular inset is from Sacramento Peak. The violet spots show the flare's footpoints from RHESSI.

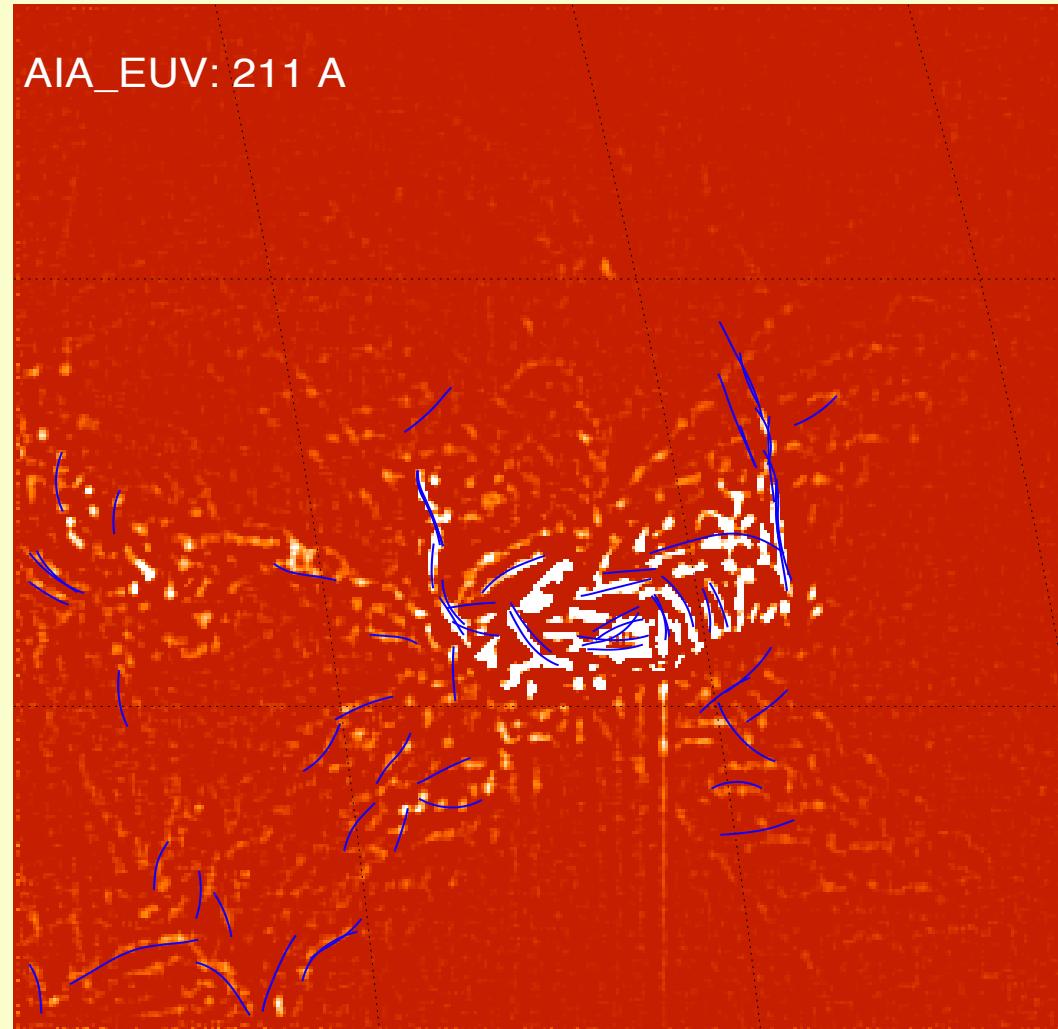
[Link to associated news item](#)



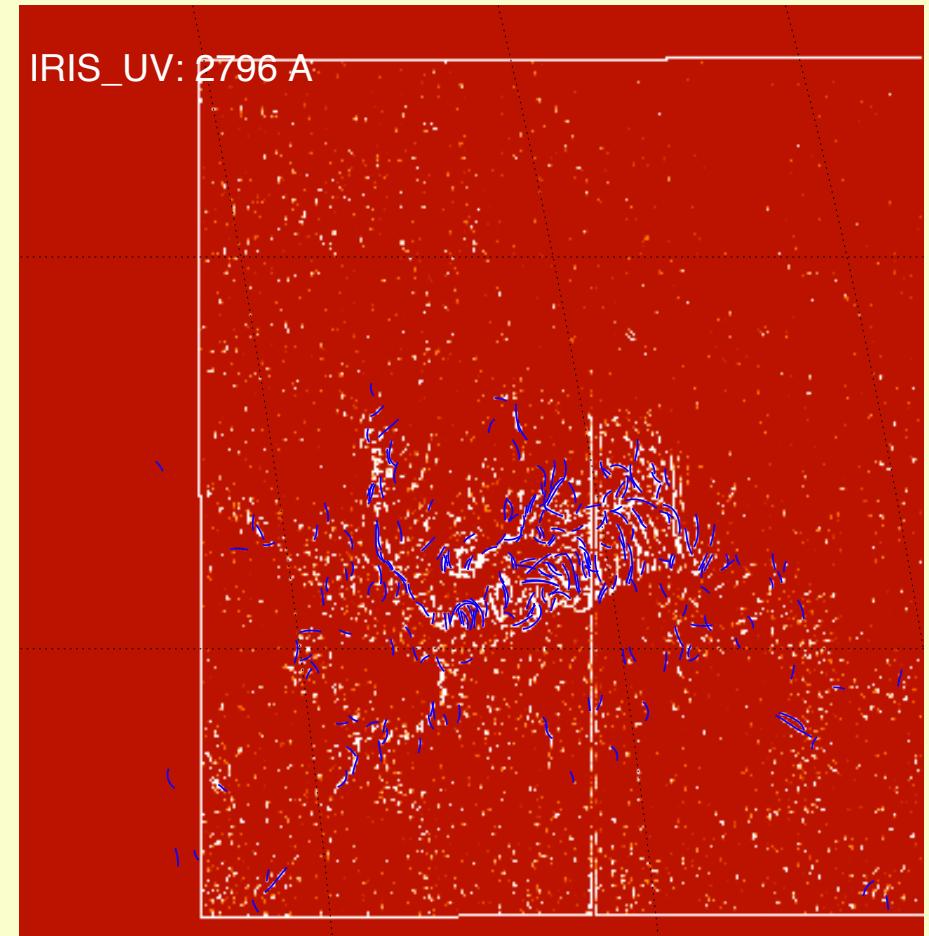
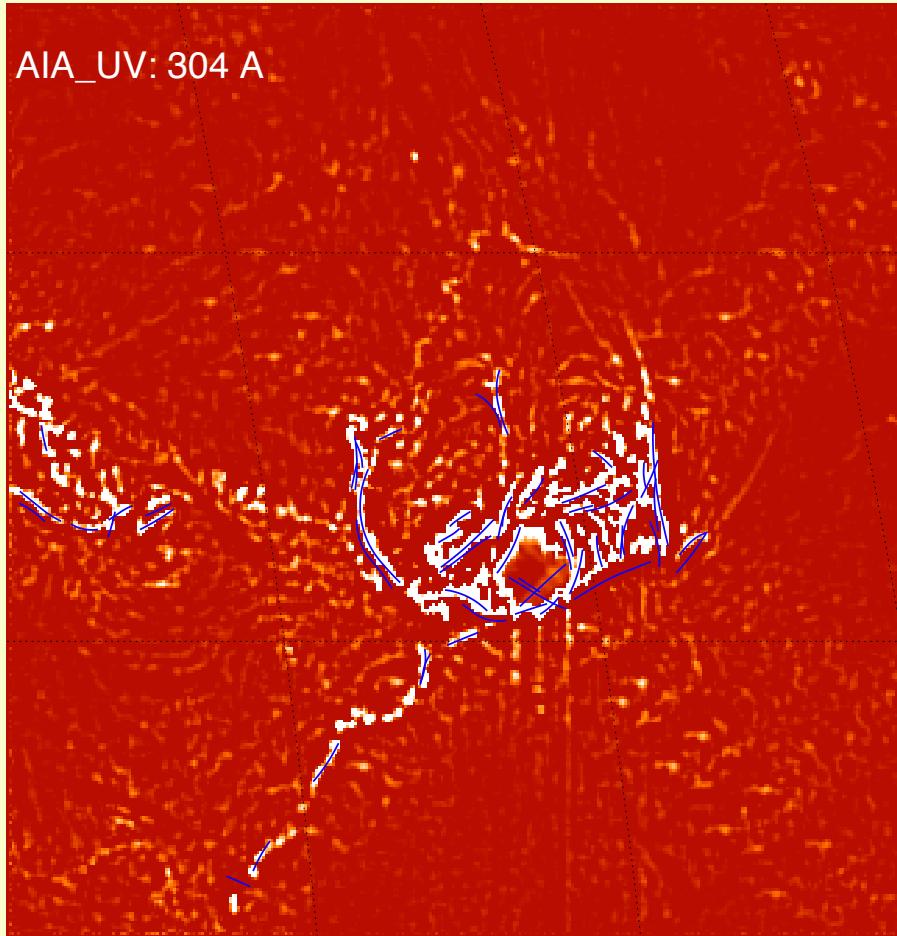
NSO IBIS G-band

Slide 19

Automated Tracing of Coronal Loop Structures

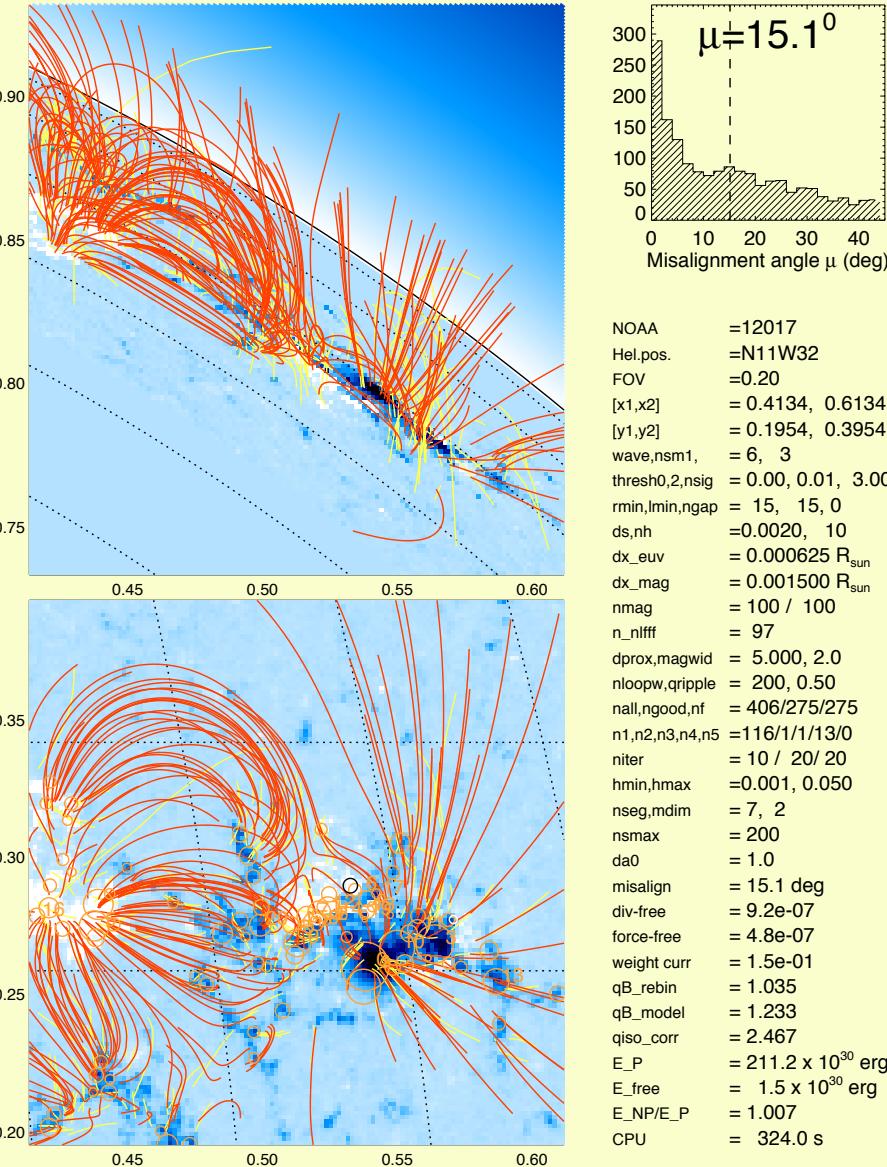


Automated Tracing of Chromospheric Structures

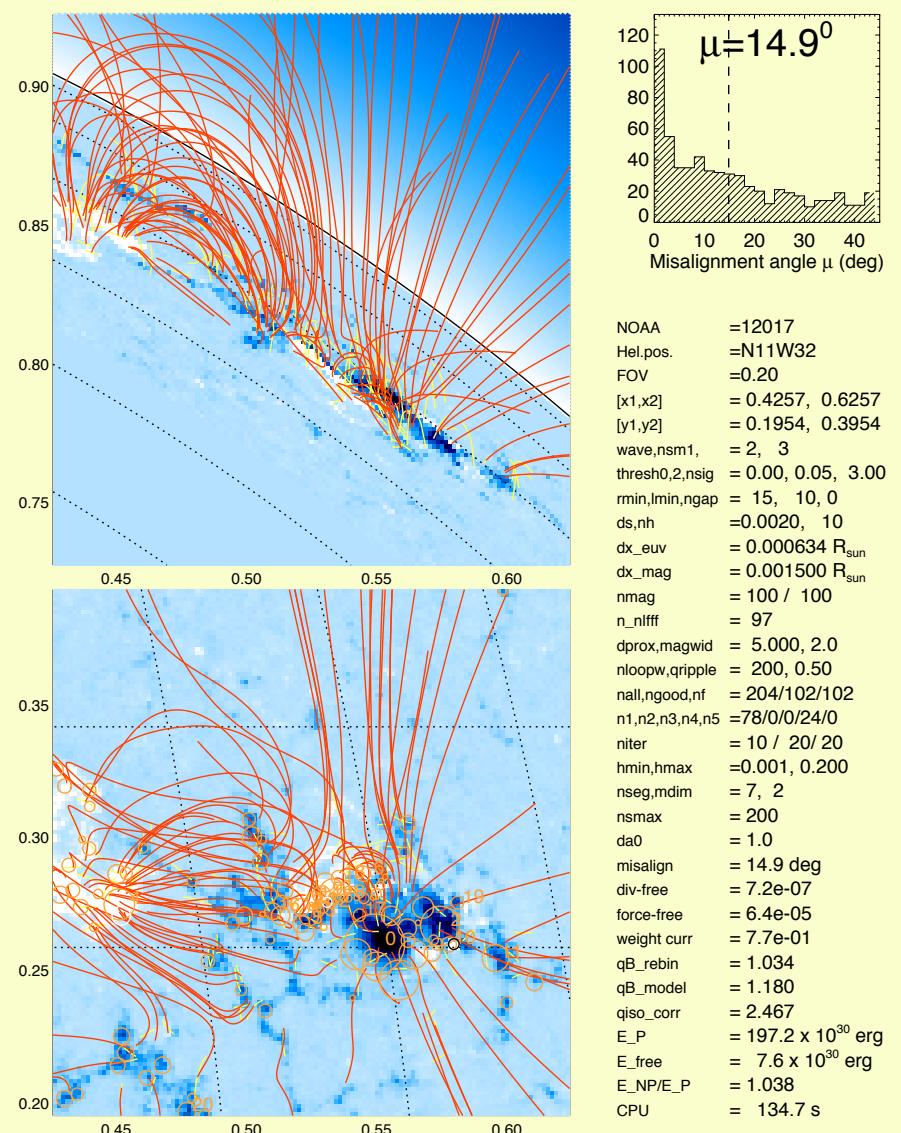


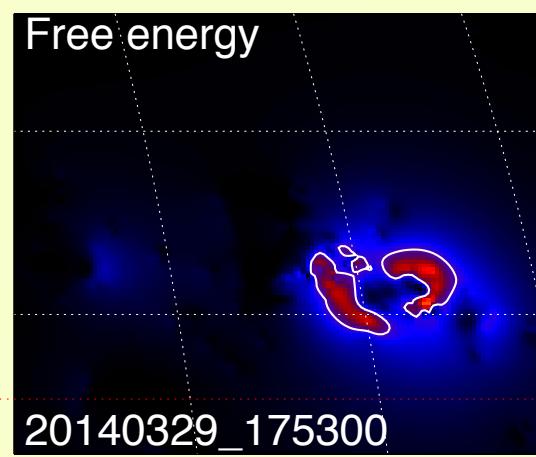
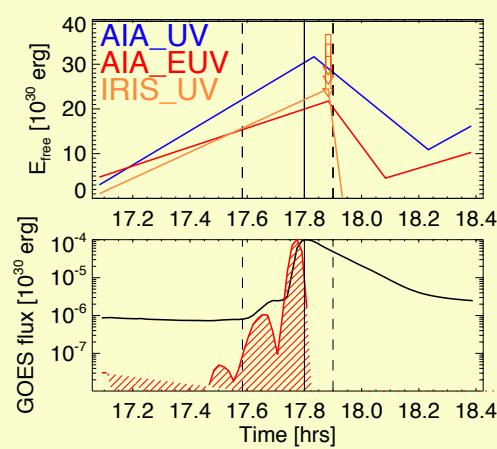
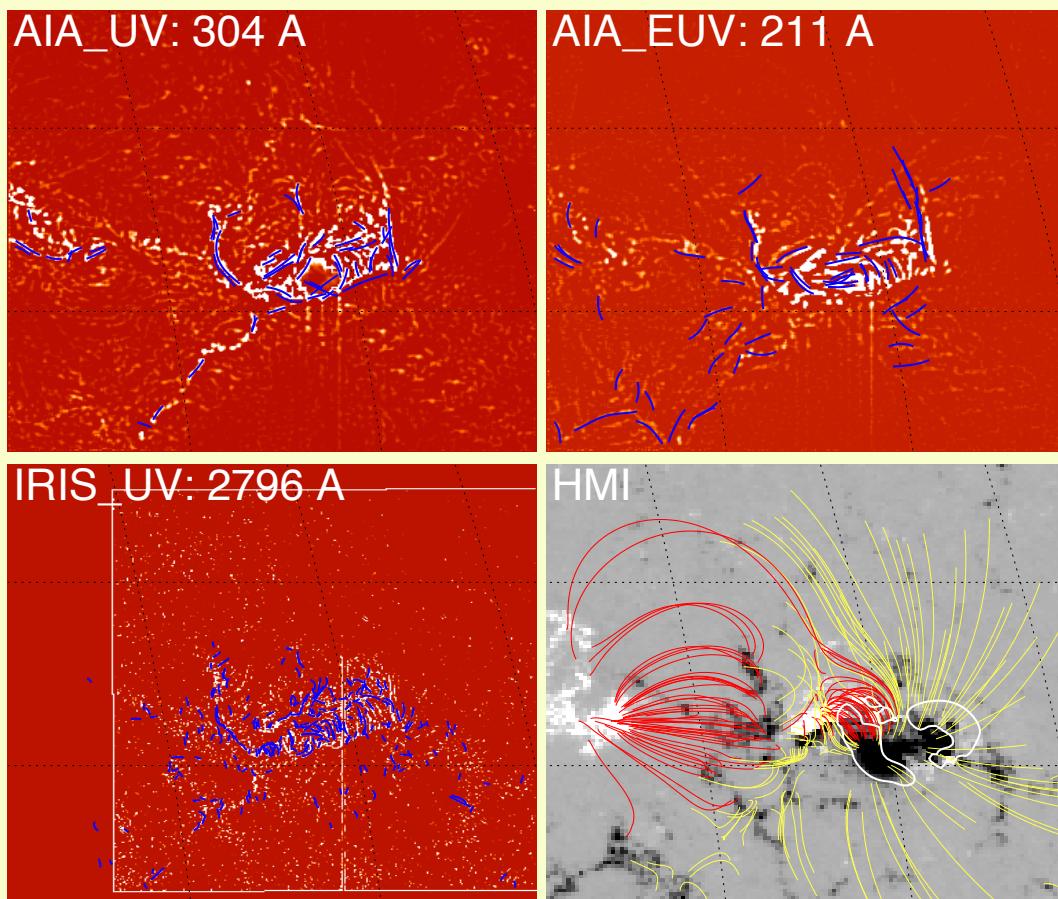
Non-linear Force Free Field (VCA-NLFFF) before and after flare

20140329_170500, EVENT=592, FRAME= 0 / 26, RUN=AIA_EUV_01



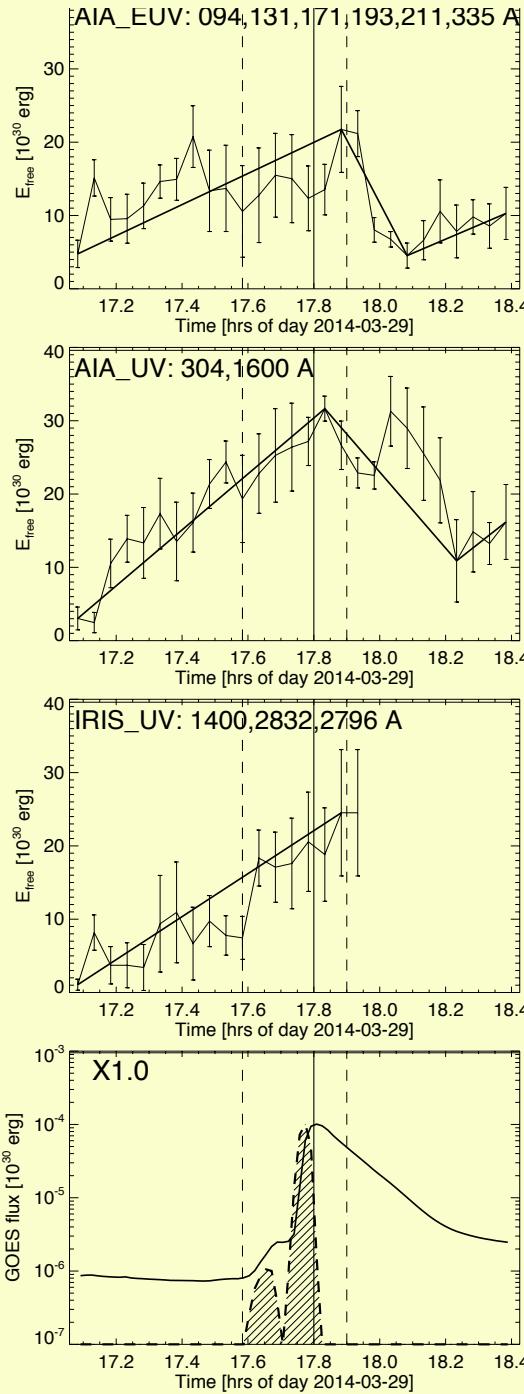
20140329_182300, EVENT=592, FRAME=26 / 26, RUN=AIA_UV_05





Slide 23

Time evolution of free energy:



GOES 1-8 Å flux
& time derivative

Coronal (AIA-EUV)

Chromospheric (AIA-UV)

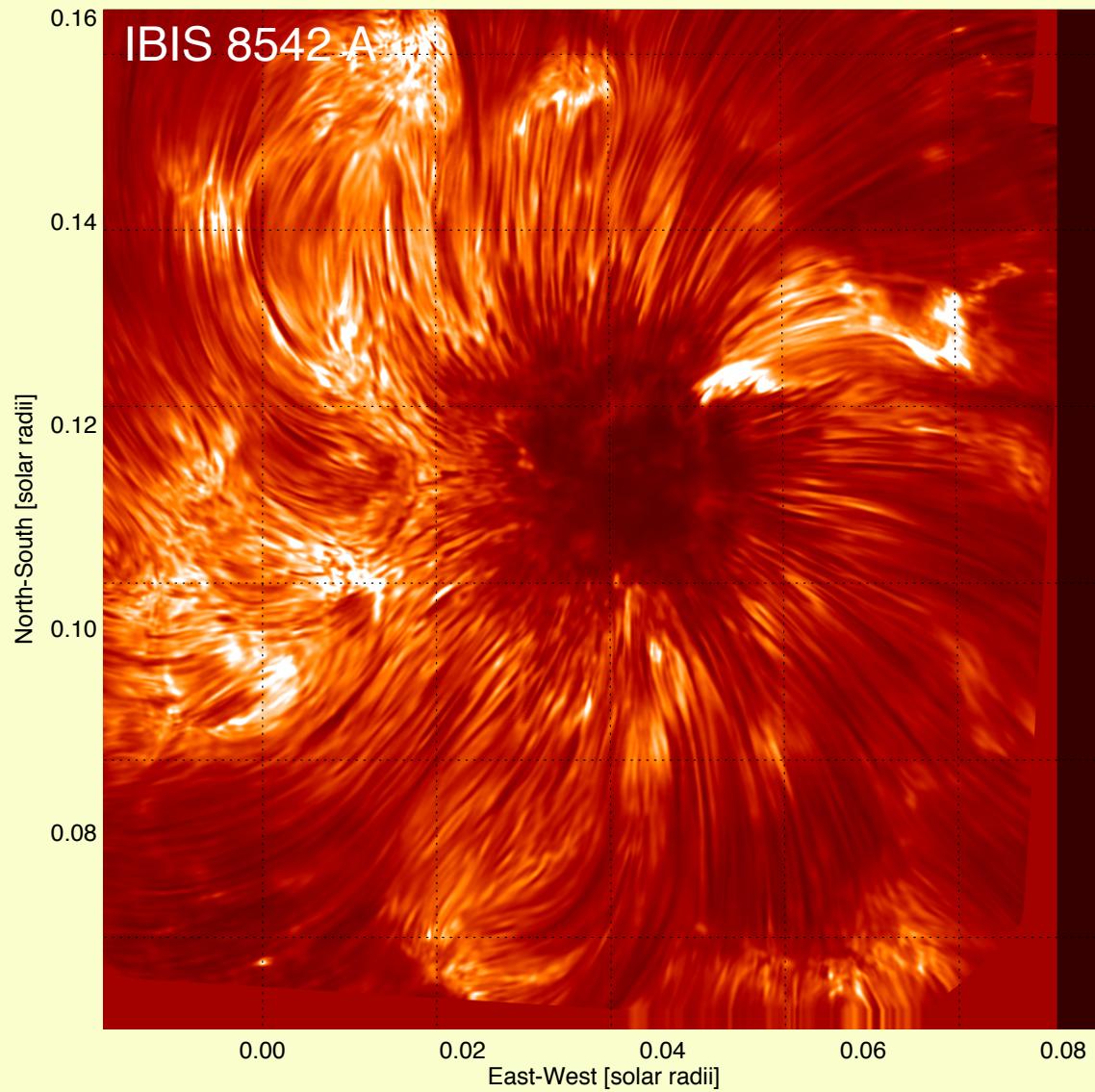
Chromospheric (IRIS)

Observations with AIA, IRIS, IBIS, & ROSA

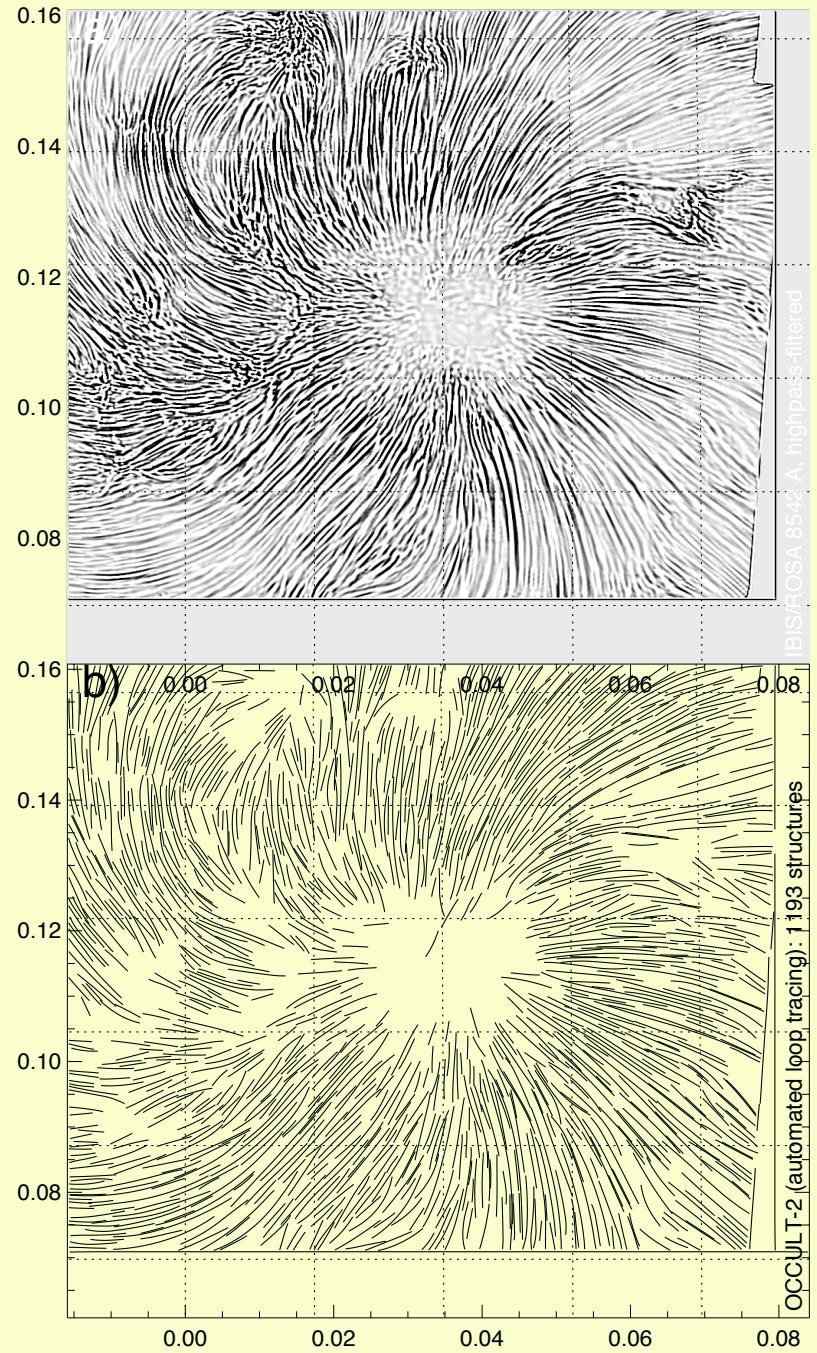
Observation date and time [UT]	Active Region NOAA	Heliographic Position [deg]	Instrument	Wavelength Å	Temperature range $\log(T[K])$
2010-08-03 15:23:00	11092	N12W02	AIA	171, 193, 211	5.8-7.3
2010-08-03 15:23:00	11092	N12W02	AIA	304	4.7
2010-08-03 15:23:00	11092	N12W02	IBIS	8542	3.8
2010-08-03 15:23:00	11092	N12W02	IBIS	6563	3.8
2014-08-24 14:06:38	12146	N09W25	AIA	171, 193, 211	5.8-7.3
2014-08-24 14:06:38	12146	N09W25	AIA	304	4.7
2014-08-24 14:06:38	12146	N09W25	ROSA	6563	3.8
2014-08-30 14:40:22	12149	N12W44	AIA	171, 193, 211	5.8-7.3
2014-08-30 14:40:22	12149	N12W44	AIA	304	4.7
2014-08-30 14:40:22	12149	N12W44	IRIS	2796	3.7-4.2
2014-08-30 14:40:22	12149	N12W44	ROSA	6563	3.8

Aschwanden, Reardon, and Jess (2016; ApJ subm).

IBIS Ca II 8542 Å image of active region NOAA 11092,
observed on 2010 Aug 3, 15:03-15:43 UT, FOV=0.1 R_{sun} , pixel=0.1"



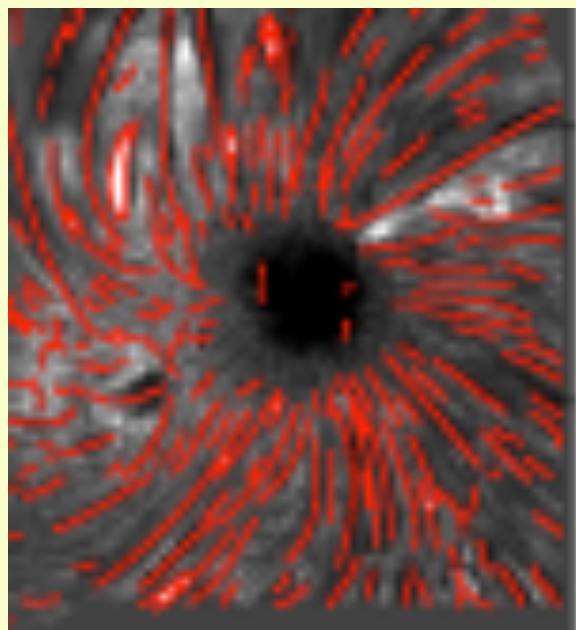
Aschwanden, Reardon & Jess
(2016)



Highpass-filtered image of IBIS
8542 A

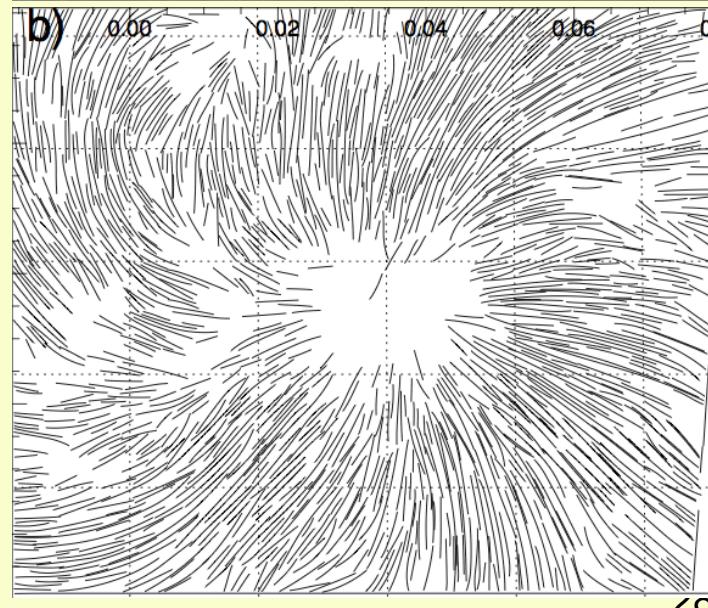
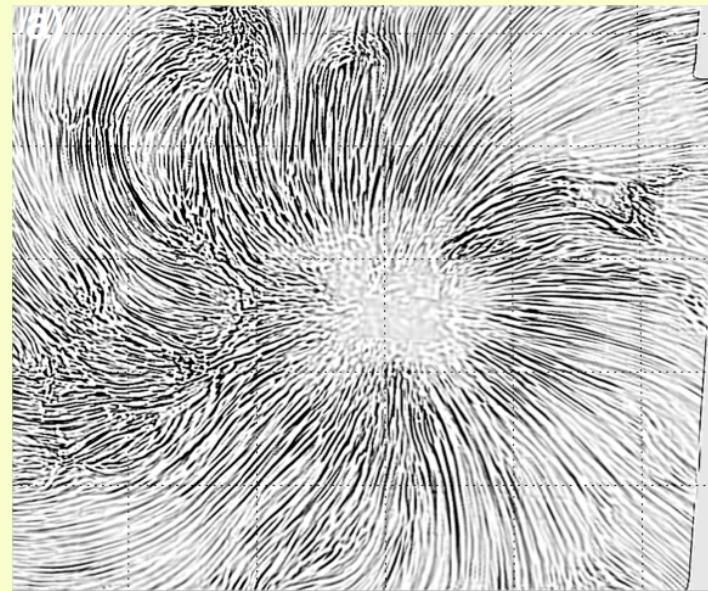
Automated tracing of curvi-linear
Features with OCCULT-2 code
→ 1193 features

Union-finding algorithm

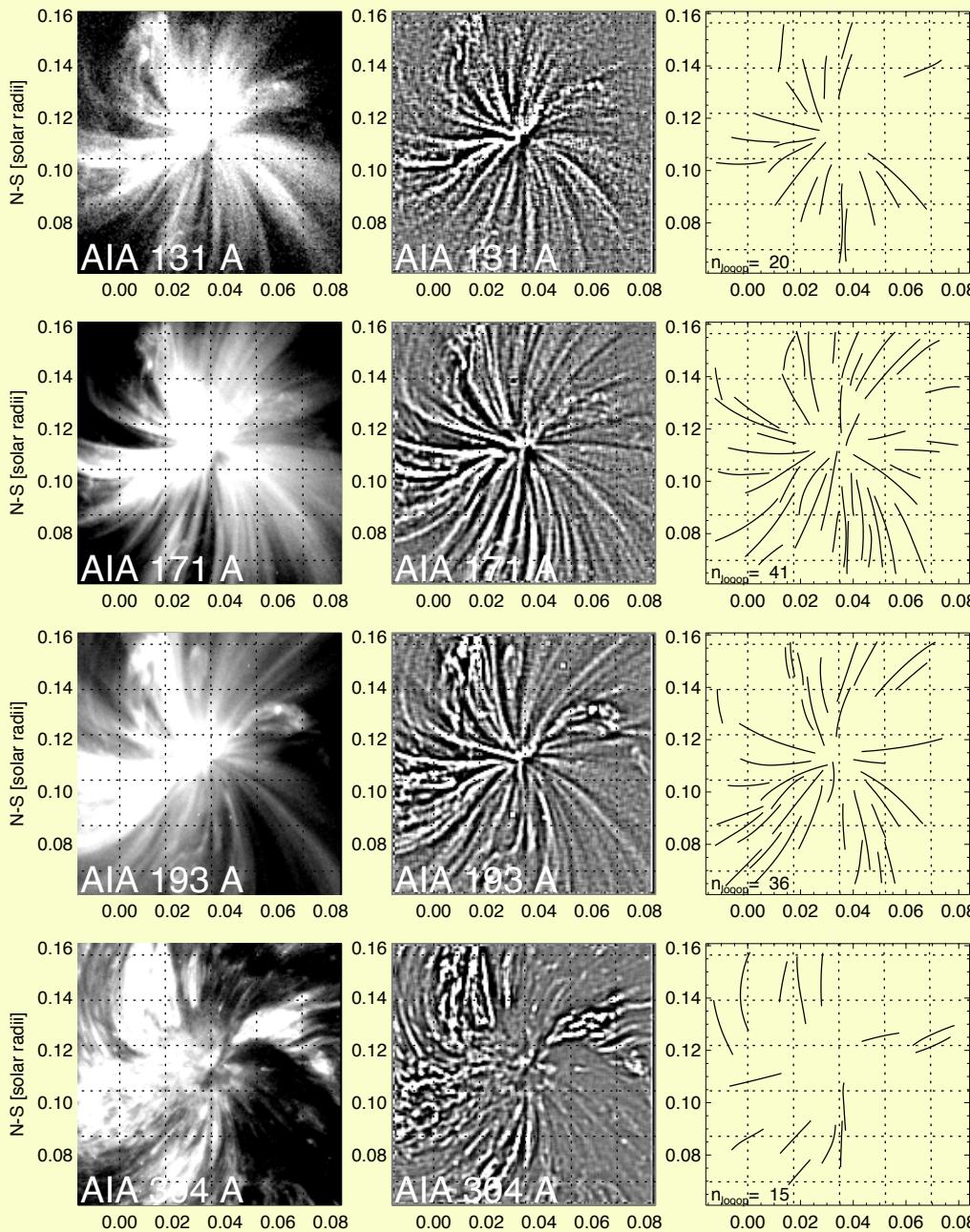


Sedgewick (2002); Jing et al. (2011)

Oriented Coronal CURvature Loop Tracing algorithm (OCCULT-2)



Aschwanden et al. (2013; 2016)

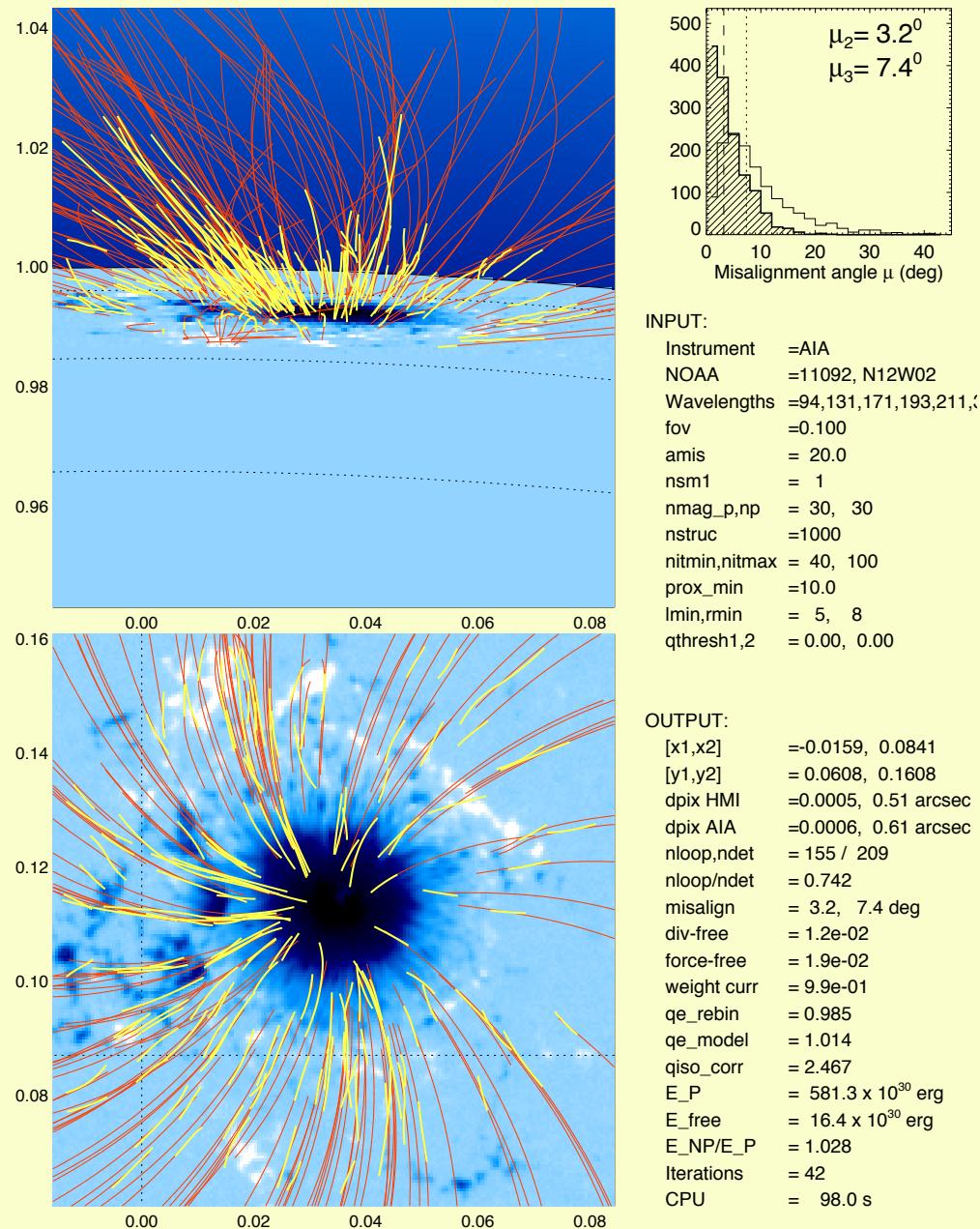


Tracing of coronal loop structures in 131, 171, 193, 304 Å

AIA/SDO (0.6" pixel) has a 6 times lower resolution than IBIS (0.1" pixels)

The number of pixels is 36 times smaller, explaining the smaller number of detected structures:
N=15-41 in AIA, vs.
N=1193 fibrils in IBIS

20100803_152300, time step=1, AIA/SDO 94, 131, 171, 193, 211, 335 Å

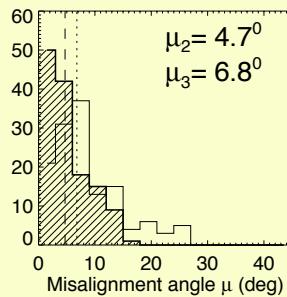
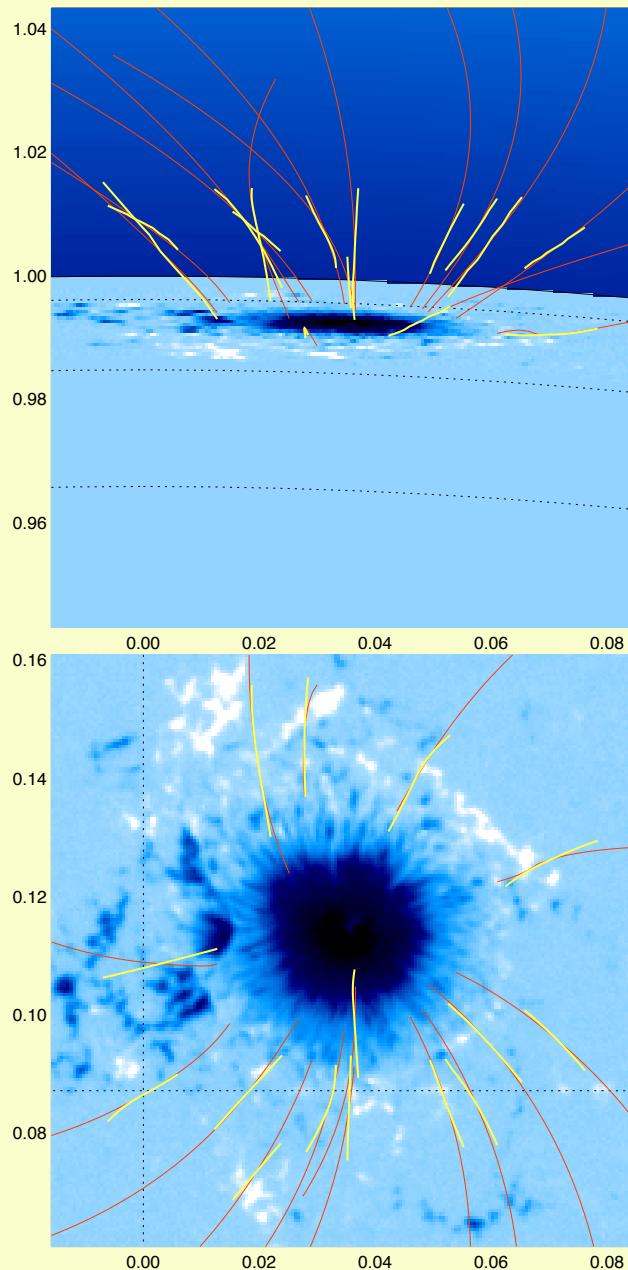


Forward-fitting of VCA-NLFFF code to 209 structures detected with AIA and traced with OCCULT-2 (yellow)

The NLFFF field (red) has a potential energy of $E_P = 581 \times 10^{30}$ erg, and a free energy of $E_{np} = 16 \times 10^{30}$ erg, With $E_{np}/E_p = 1.028$

Misalignment angles:
3.2 deg (2D)
7.4 deg (3D)

20100803_152300, time step=1, AIA/SDO 304 A



INPUT:

Instrument	=AIA
NOAA	=11092, N12W02
Wavelengths	=304 A
fov	=0.100
amis	= 20.0
nsm1	= 3
nmag_p,np	= 30, 30
nstruc	=1000
nitmin,nitmax	= 40, 100
prox_min	=10.0
lmin,rmin	= 5, 8
qthresh1,2	= 0.00, 0.00

OUTPUT:

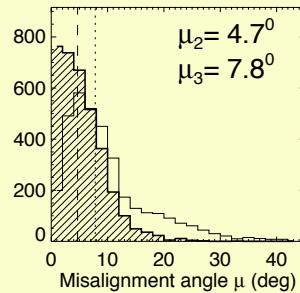
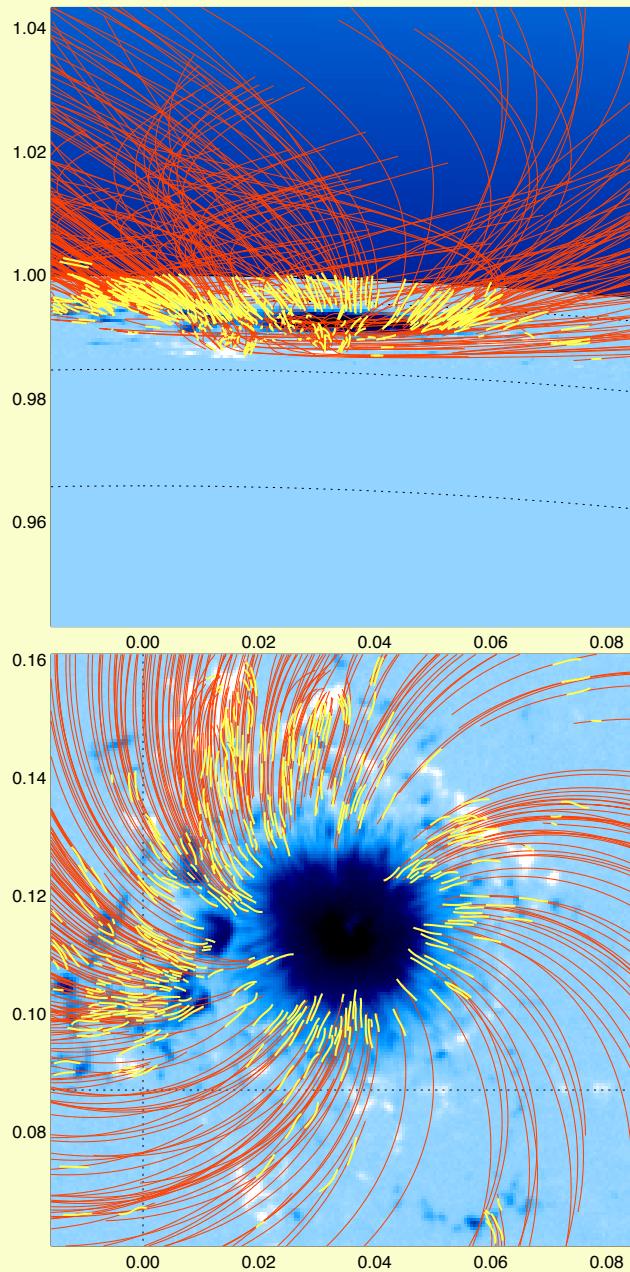
[x1,x2]	= -0.0159, 0.0841
[y1,y2]	= 0.0608, 0.1608
dpix HMI	= 0.0005, 0.51 arcsec
dpix AIA	= 0.0006, 0.61 arcsec
nloop,ndet	= 15 / 22
nloop/ndet	= 0.682
misalign	= 4.7, 6.8 deg
div-free	= 1.2e-02
force-free	= 1.9e-02
weight curr	= 9.9e-01
qe_rebin	= 0.985
qe_model	= 1.014
qiso_corr	= 2.467
E_P	= 581.3×10^{30} erg
E_free	= 24.9×10^{30} erg
E_NP/E_P	= 1.043
Iterations	= 45
CPU	= 18.1 s

Forward-fitting of VCA-NLFFF code to 22 structures detected with AIA 304 and traced with OCCULT-2 (yellow)

The NLFFF field (red) has a potential energy of $E_P = 581 \times 10^{30}$ erg, and a free energy of $E_{NP} = 24 \times 10^{30}$ erg, With $E_{NP}/E_P = 1.043$

Misalignment angles:
4.7 deg (2D)
6.8 deg (3D)

20100803_152300, time step=1, IBIS 8542 A



INPUT:

Instrument =IBIS
 NOAA =11092, N12W02
 Wavelengths =8542 A
 fov =0.100
 amis = 20.0
 nsm1 = 1
 nmag_p,np = 30, 30
 nstruc =1000
 nitmin,nitmax = 40, 100
 prox_min =10.0
 lmin,rmin = 5, 8
 qthresh1,2 = 0.00, 0.00

OUTPUT:

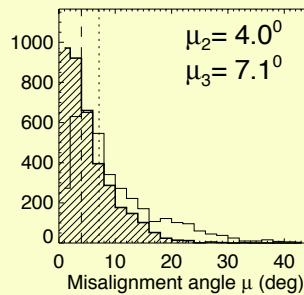
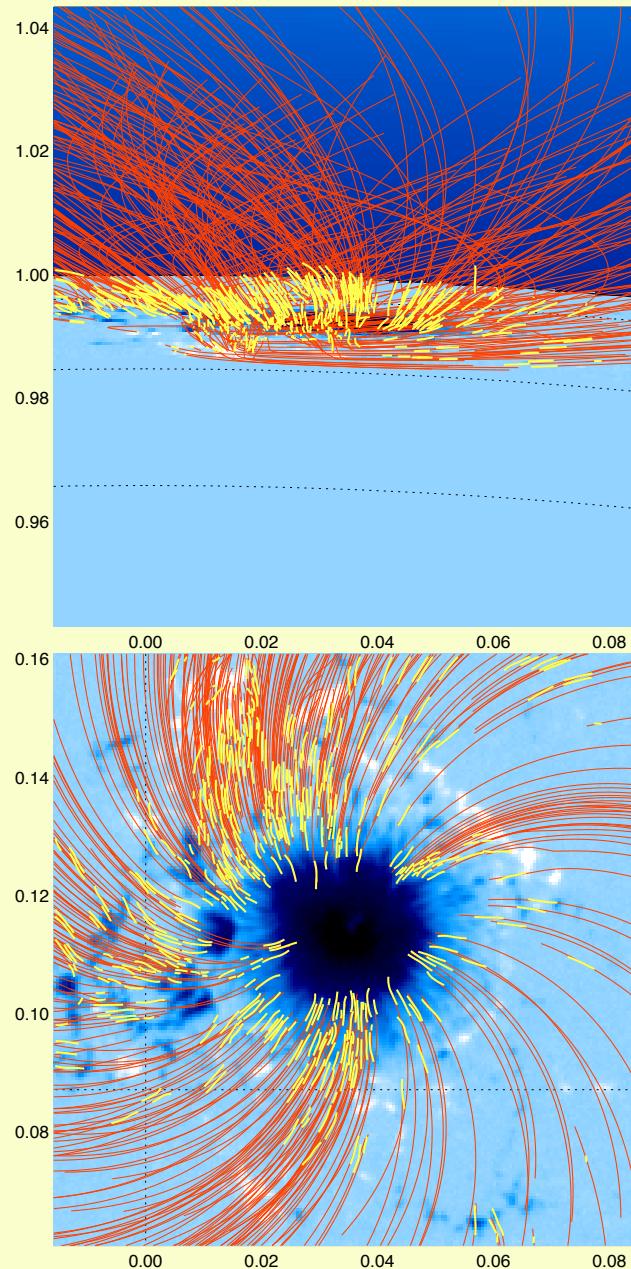
[x1,x2] =-0.0159, 0.0841
 [y1,y2] = 0.0608, 0.1608
 dpix HMI =0.0005, 0.51 arcsec
 dpix IBIS =0.0001, 0.10 arcsec
 nloop,ndet = 386 / 703
 nloop/ndet = 0.549
 misalign = 4.7, 7.8 deg
 div-free = 1.2e-02
 force-free = 1.9e-02
 weight curr = 9.9e-01
 qe_rebin = 0.985
 qe_model = 1.014
 qiso_corr = 2.467
 E_P = 581.3 x 10³⁰ erg
 E_free = 92.5 x 10³⁰ erg
 E_NP/E_P = 1.159
 Iterations = 53
 CPU = 339.4 s

Forward-fitting of VCA-NLFFF code To 703 structures detected with IBIS 8542 A and traced with OCCULT-2 (yellow)

The NLFFF field (red) has a potential energy of $E_P = 581 \times 10^{30}$ erg, and a free energy of $E_{np} = 92 \times 10^{30}$ erg, With $E_{np}/E_p = 1.159$

Misalignment angles:
 4.7 deg (2D)
 7.8 deg (3D)

20100803_152300, time step=1, IBIS H-alpha 6563 A



INPUT:

```

Instrument      =IBIS
NOAA          =11092, N12W02
Wavelengths   =6563 A
fov            =0.100
amis           = 20.0
nsm1           = 1
nmag_p,np     = 30, 30
nstruc         =1000
nitmin,nitmax = 40, 100
prox_min       =10.0
lmin,rmin     = 5,  8
qthresh1,2    = 0.00, 0.00

```

OUTPUT:

```

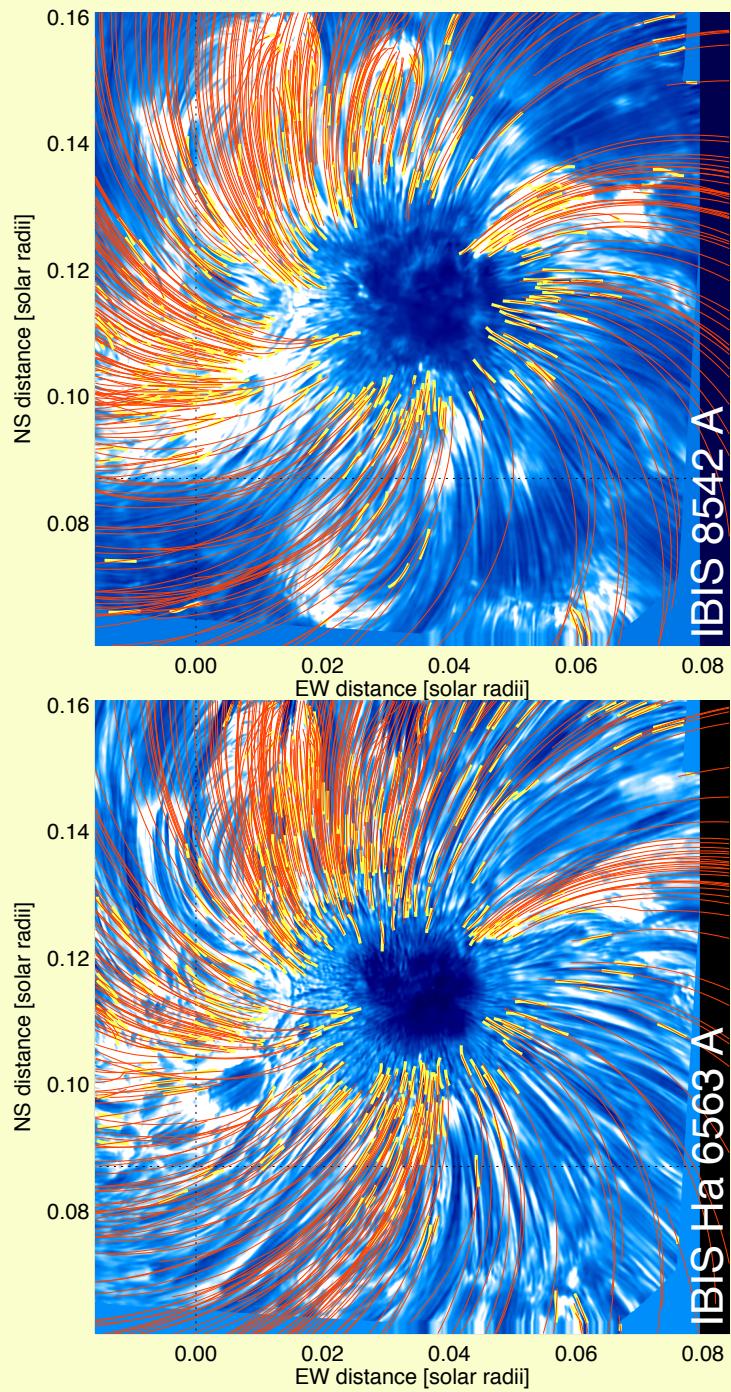
[x1,x2]      =-0.0159, 0.0841
[y1,y2]      = 0.0608, 0.1608
dpix HMI     =0.0005, 0.51 arcsec
dpix IBIS    =0.0001, 0.10 arcsec
nloop,ndet   = 419 / 751
nloop/ndet   = 0.558
misalign     = 4.0,  7.1 deg
div-free      = 1.2e-02
force-free    = 1.9e-02
weight curr  = 9.9e-01
qe_rebin     = 0.985
qe_model     = 1.014
qiso_corr    = 2.467
E_P          = 581.3 x 1030 erg
E_free        = 64.4 x 1030 erg
E_NP/E_P     = 1.111
Iterations    = 53
CPU          = 356.2 s

```

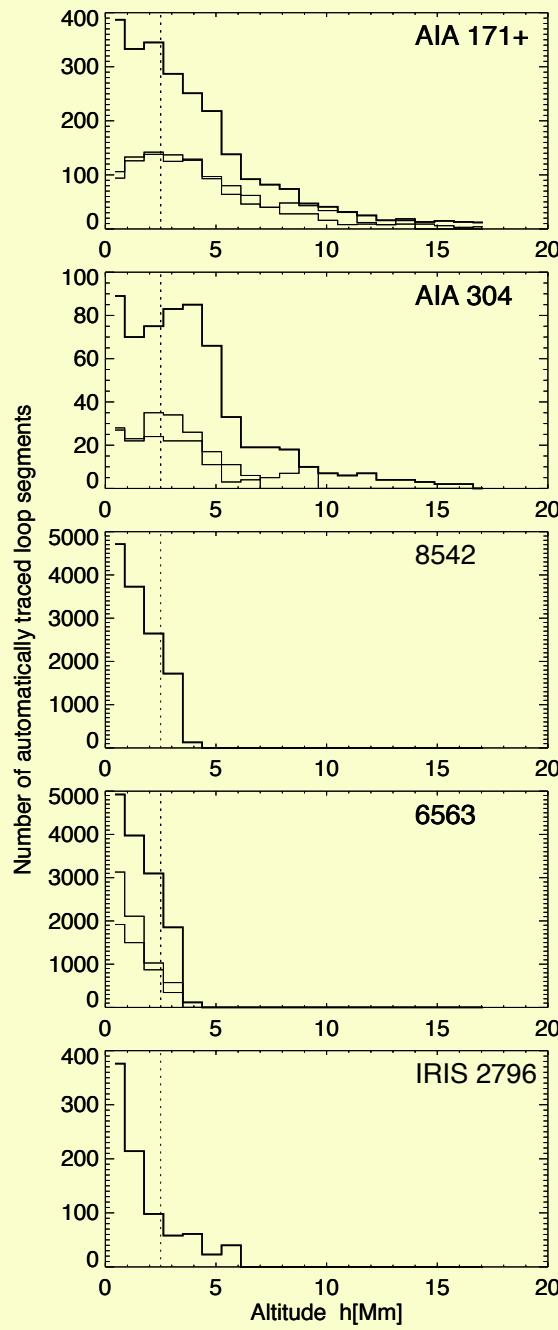
Forward-fitting of VCA-NLFFF code
To 703 structures detected with IBIS
Ha 6563 A and traced with OCCULT-2 (yellow)

The NLFFF field (red) has a potential energy of $E_P = 581 \times 10^{30}$ erg, and a free energy of $E_{np} = 64 \times 10^{30}$ erg, With $E_{np}/E_p = 1.111$

Misalignment angles:
4.7 deg (2D)
7.8 deg (3D)



Overlay of forward-fitted
VCA-NLFFF solution
on fibril structures
detected with [the OCCULT-2 code](#),
Overlayed on
IBIS Ha 6563 A (bottom)
and Ca II 8542 A (top)
Images.



Altitude contribution function

The altitude distribution of the automatically traced curvi-linear elements is obtained from the 3D-model of the magnetic non-potential field solution (VLA-NLFFF).

Chromospheric fibrils observed in Ca II 8542 Å, Hα 6563 Å, and IRIS Mg II 2796 appear to be confined to altitudes of $h < 4000$ km.

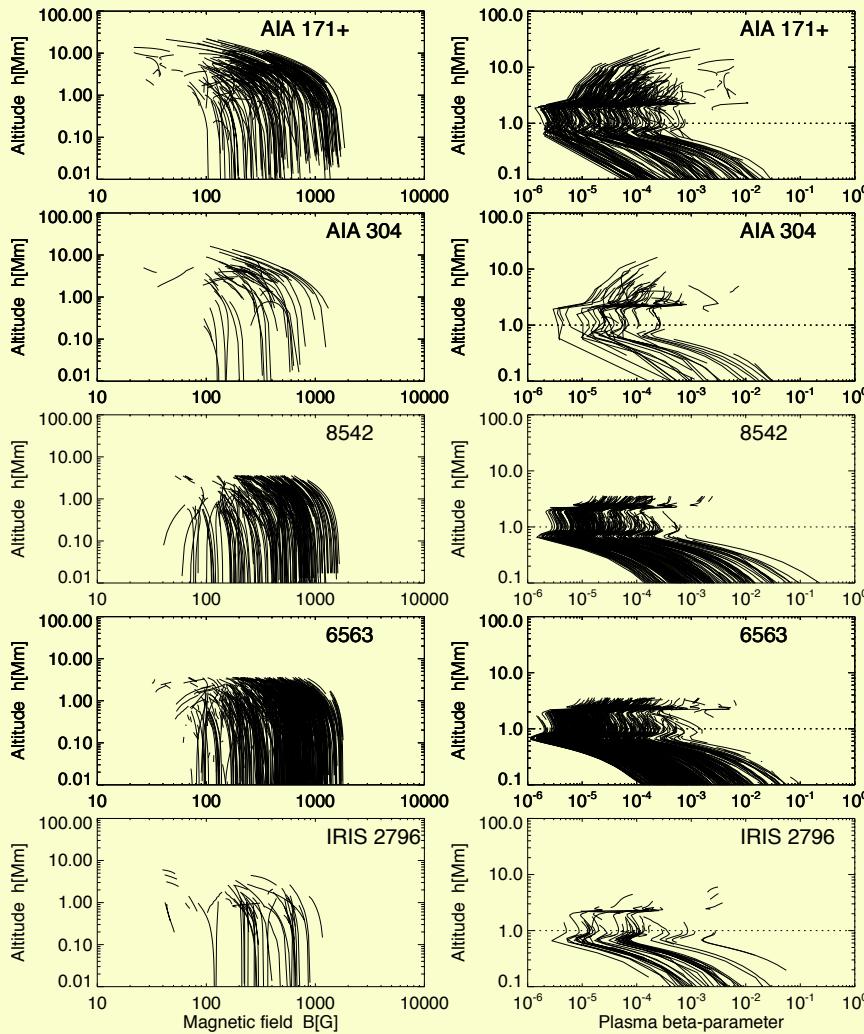
Coronal loops observed with AIA 121, 171, 193 Å as well as 304 Å extend to altitudes up to $h < 15,000$ km.

Free energy in active regions

Observation date	Instrument	Detected loops n_{det}	Fitted loops n_{loop}	Misalignment angle 2-D μ_2 [deg]	Misalignment angle 3-D μ_3 [deg]	Potential energy E_P [10^{30} erg]	Free energy ratio q_{free}
2010-08-03	AIA 171+	222 ± 76	167 ± 36	$5.0^\circ \pm 3.2^\circ$	$7.8^\circ \pm 0.5^\circ$	571	0.03 ± 0.01
2010-08-03	AIA 304	63 ± 27	38 ± 14	$4.2^\circ \pm 0.4^\circ$	$7.2^\circ \pm 0.9^\circ$	571	0.06 ± 0.03
2010-08-03	IBIS 8542	656 ± 121	338 ± 62	$4.0^\circ \pm 0.6^\circ$	$7.1^\circ \pm 0.7^\circ$	571	0.13 ± 0.04
2010-08-03	IBIS 6563	712 ± 114	421 ± 75	$4.0^\circ \pm 0.4^\circ$	$7.2^\circ \pm 0.8^\circ$	571	0.11 ± 0.01
2014-08-24	AIA 171+	186 ± 88	82 ± 30	$5.5^\circ \pm 1.3^\circ$	$8.9^\circ \pm 1.5^\circ$	551	0.18 ± 0.06
2014-08-24	AIA 304	45 ± 21	17 ± 6	$7.4^\circ \pm 2.2^\circ$	$7.5^\circ \pm 1.5^\circ$	551	0.11 ± 0.05
2014-08-24	ROSA 6563	654 ± 98	232 ± 75	$6.5^\circ \pm 1.3^\circ$	$8.5^\circ \pm 1.8^\circ$	551	0.26 ± 0.01
2014-08-30	AIA 171+	190 ± 87	83 ± 34	$5.4^\circ \pm 1.2^\circ$	$10.9^\circ \pm 2.4^\circ$	559	0.10 ± 0.05
2014-08-30	AIA 304	43 ± 22	16 ± 7	$7.0^\circ \pm 1.0^\circ$	$10.7^\circ \pm 2.4^\circ$	559	0.10 ± 0.09
2014-08-30	IRIS 2796	206 ± 52	65 ± 19	$6.1^\circ \pm 1.4^\circ$	$11.3^\circ \pm 2.5^\circ$	559	0.26 ± 0.01
2014-08-30	ROSA 6563	556 ± 89	299 ± 79	$6.6^\circ \pm 0.5^\circ$	$14.2^\circ \pm 2.3^\circ$	559	0.17 ± 0.04

The free energy is underestimated by a factor of 2-4 from coronal loops compared with chromospheric fibrils observed with IBIS and/or ROSA
 → Is larger amount of nonpotential or free energy due to higher spatial resolution? Are chromospheric fibrils more non-potential than coronal loops?

Plasma β -parameter of chromospheric tracers



$$\beta(h) = \frac{p_{th}(h)}{p_{mag}(h)} = 6.94 \times 10^{-15} n_e(h) T_e(h) B(h)^{-2} .$$

The magnetic field of traced coronal loops and chromospheric fibrils varies in the range of $B=100-1000$ G.

The plasma β -parameter of fibrils and loops varies in a range of $B=10^{-5}-10^{-1}$,
 → Confirms magnetic confinement in corona and upper chromosphere.

Outline of Talk:

- 1) Previous work on chromospheric magnetic fields
- 2) The VCA-NLFFF method to compute magnetic fields:
 - 2.1 Potential field from buried magnetic sources
 - 2.2 Automated tracing of curvi-linear features
 - 2.3 Forward-fitting of nonpotential magnetic field
- 3) Data Analysis:
 - AIA/SDO, HMI/SDO
 - IRIS
 - IBIS
 - ROSA
- 4) Conclusions:
 - **Suitability of chromospheric field tracing**
 - **Altitudes of chromospheric magnetic field tracers**
 - **Coronal vs. chromospheric free energy**

Conclusions:

- (1) Chromospheric images reveal crisp curvi-linear structures (loop segments, fibrils, spicules) that are extremely well-suited for constraining magnetic models.
- (2) The chromospheric fibrils are field-aligned with the best-fit VCA-NLFFF solution within a misalignment angle of 4° - 7° .
- (3) The free (non-potential excess) energy obtained from coronal loops under-estimates that of chromospheric features by a factor of 2-4.
- (4) Chromospheric features are confined to altitudes of $h < 4000$ km, while coronal structures are detected up to $h < 15,000$ km
- (5) The plasma β -parameter is $\beta = 10-5-10-1$ for fibrils and loops, and the magnetic field is $B = 100-1000$ G.
- (6) Chromospheric data are important for magnetic modeling and free energy estimates for flares, CMEs, and coronal heating.

SSW

VCA-NLFFF code: <http://www.lmsal.com/~aschwand/software/>
OCCULT-2 code: <http://www.lmsal.com/~aschwand/software/>



Appendix :

The Vertical-Current Approximation Nonlinear Force-Free Field Code –
Description, Performance Tests, and Measurements of Magnetic
Energies Dissipated in Solar Flares

(Aschwanden 2016, subm.)

Vertical Current Approximation Non-Linear Force-Free Field (VCA-NLFFF) Code

