



# How radial is the photospheric magnetic field?

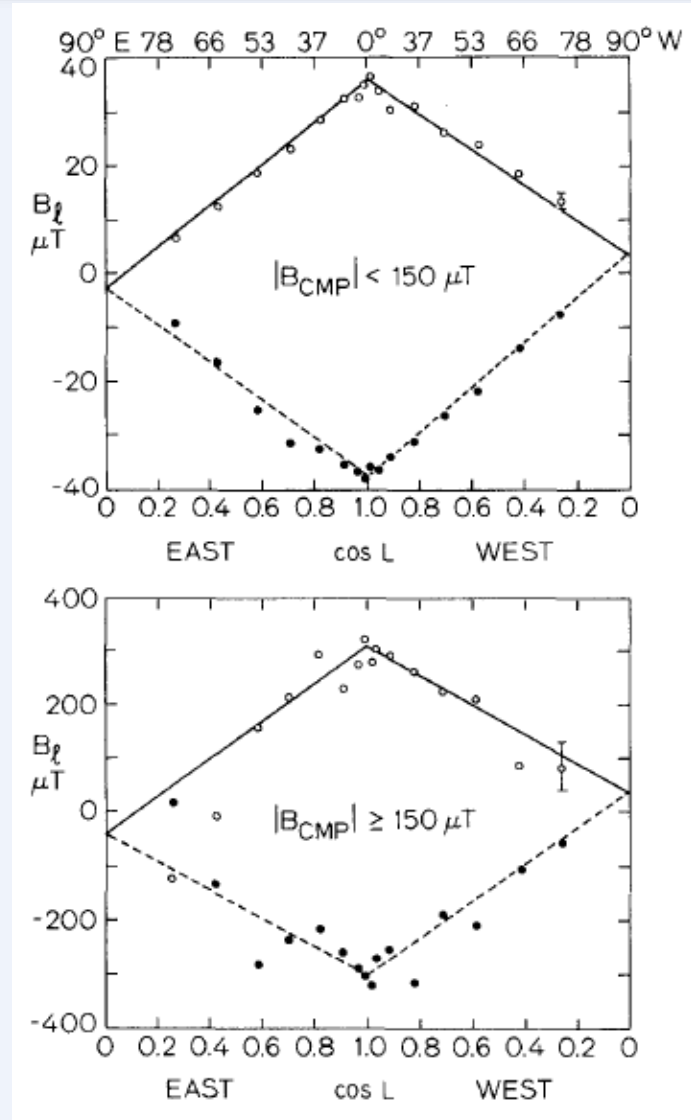
Ilpo Virtanen, Alexei Pevtsov and  
Kalevi Mursula

[Ilpo.Virtanen@oulu.fi](mailto:Ilpo.Virtanen@oulu.fi)

- Line-of-sight observations of the photospheric magnetic field started in late 1950s and calibrated digital data exist since mid 1970s.
- Information about the radial magnetic field  $B_r$  is important especially for coronal and heliospheric models.
- The simplest and most widely used assumption is that the photospheric magnetic field is radial and  $B_{LOS}$  is a projection of the radial field.
- **Pseudo-radial magnetic field**

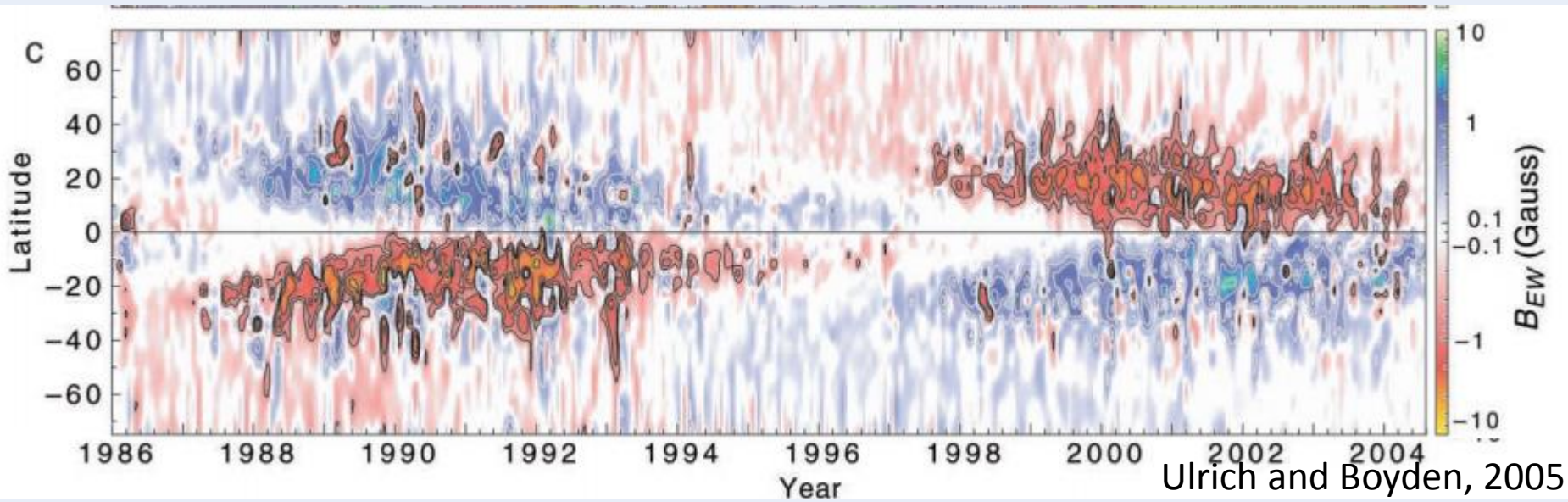
$$B_r = B_r^{PSEUD} = \frac{B_{LOS}}{\cos \lambda}$$

- Originally justified by Svalgaard (1978).
- Observed magnetic field in the same region is proportional to the cosine of the angle from central meridian.
- This method does not pay attention to meridional inclination of the magnetic field.
- Assumption of radial photospheric magnetic field is used practically in all the studies which involve synoptic maps of the photospheric magnetic field.
- How valid it is?

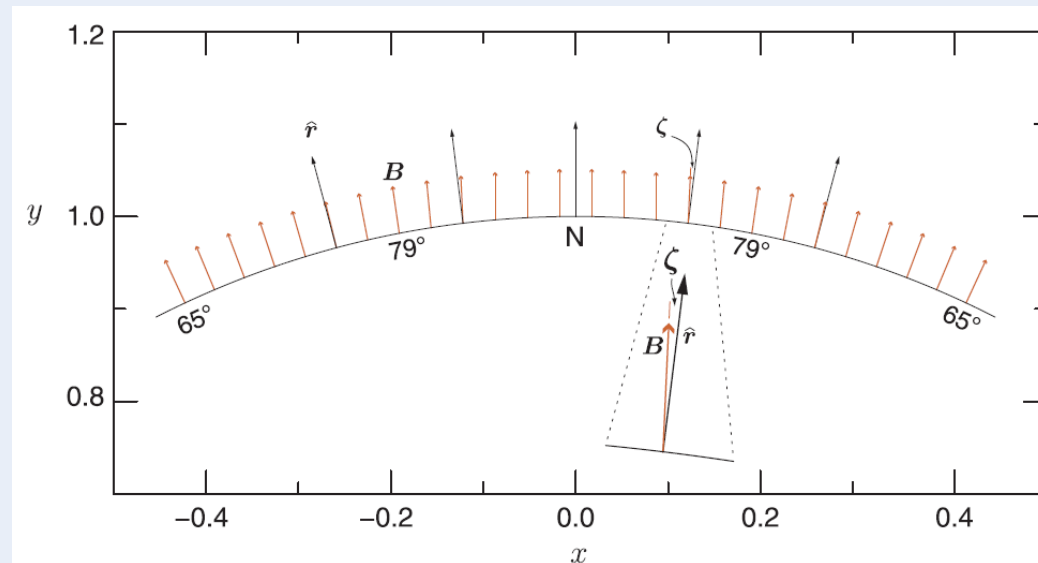


Svalgaard et al., 1978

- The average large scale **toroidal magnetic field (East-West,  $B_\phi$ )** can be derived using observations on consecutive days, since viewing angle changes about 14 degrees/day.
- A systematic pattern of toroidal magnetic field was found already in 1970s. (*Howard, 1974; Svalgaard et al. 1978 and Duvall et al., 1979*).
- The average  $B_\phi$  is systematic, but rather small.
- Net tilt in the direction of rotation (to the west) of  $0.6^\circ$  (*Shrauner and Scherrer, 1993*)

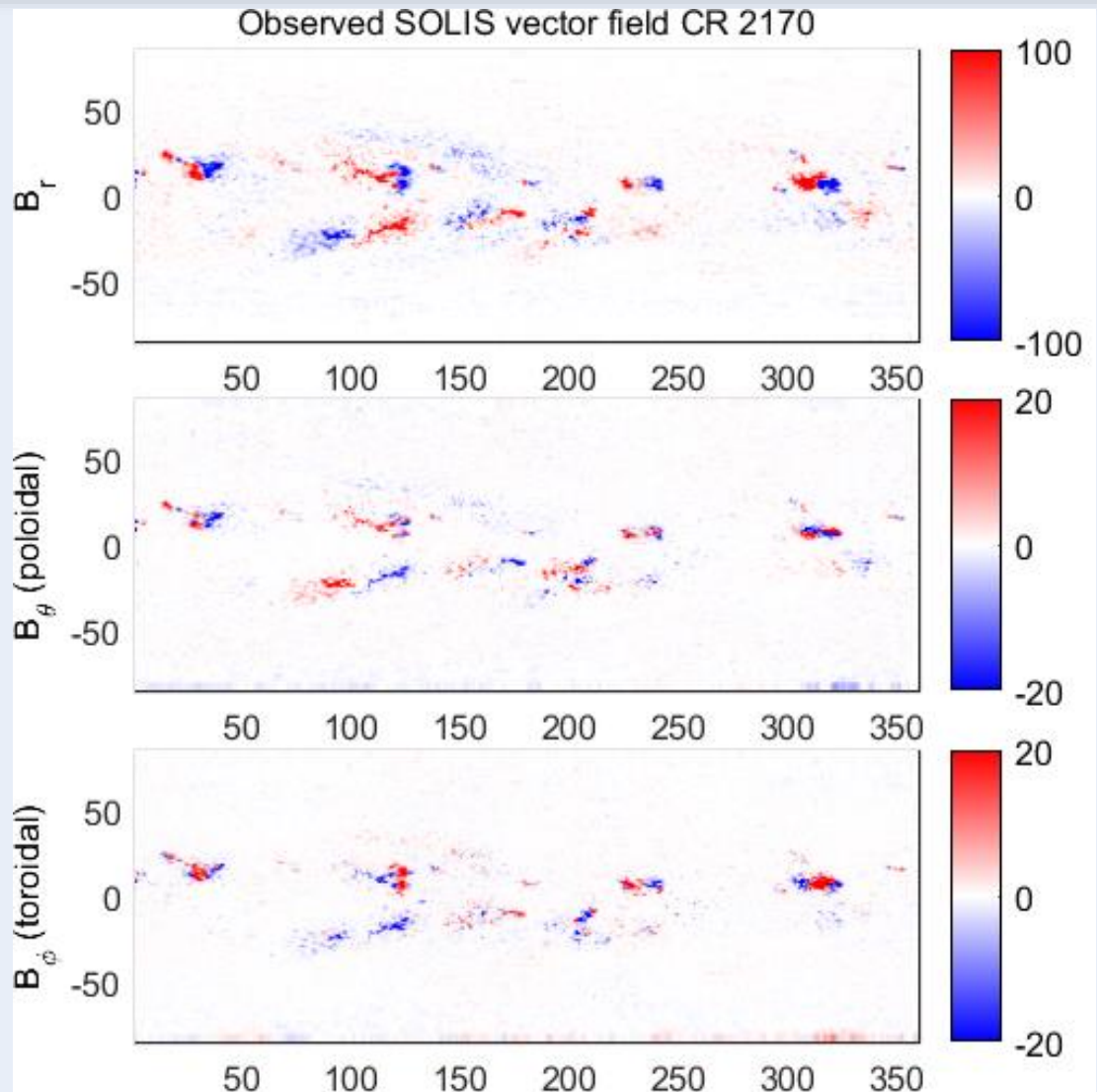


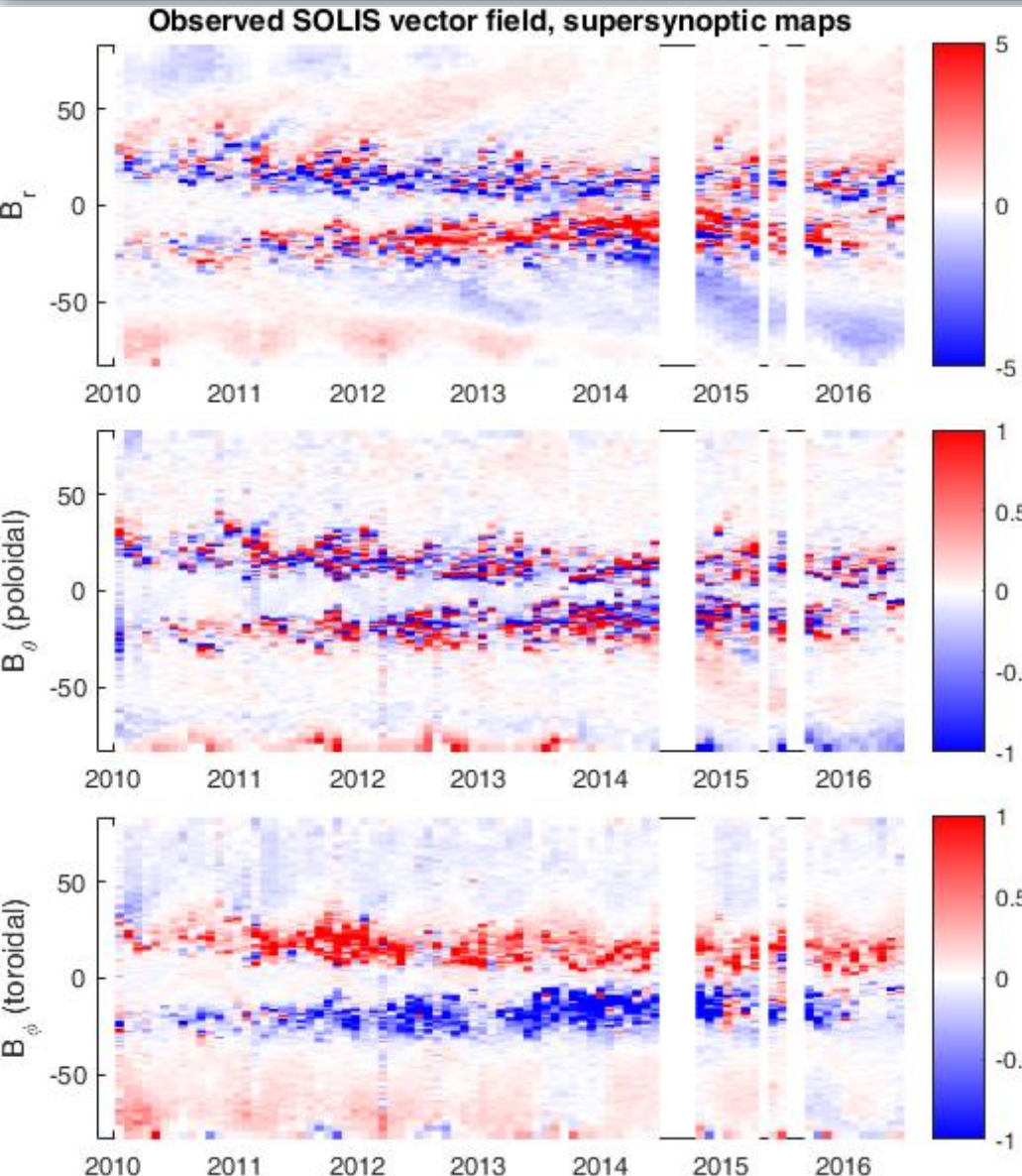
- **Poloidal field (North-South,  $B_\theta$ )** is more difficult to derive from  $B_{LOS}$  observations since the latitudinal vantage point only varies  $\pm 7.25$  degrees per year.
- Equatorward inclination of the photospheric magnetic field is often assumed, since coronal magnetic field is known to expand "super-radially" in the 'polar coronal holes.
- Ulrich et al.(2013) suggested that the polar field is few degrees inclined poleward, but the field lines don't converge anyway.
- This assumption and related correction decrease the annual oscillation in observations.





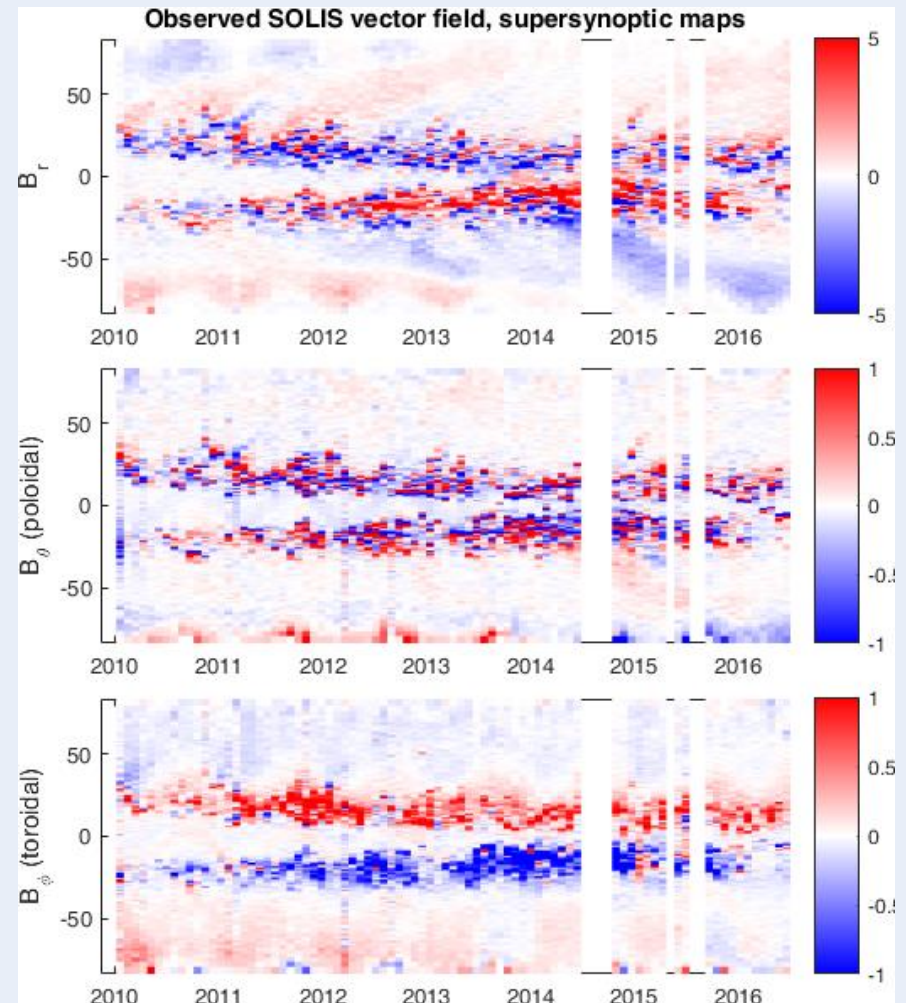
- Synoptic maps of full vector magnetic field should provide us information about the inclination and azimuth of the magnetic field.
- Different data sets:
  - SOLIS, NSO 180\*360 pixels
  - HMI, "random calibration" 1440\*3600
  - HMI random, 360\*720
  - HMI random, 180\*360
  - HMI radial, 180\*360





- Longitudinal averages (supersynoptic maps, magnetic butterfly diagram) for three vector components, SOLIS/VSM observations.
- $B_r$  and  $B_\theta$  have typically same sign in the north but opposite signs in the south.
- **This indicates equatorward inclination of the field**
- $B_\phi$  depicts expected patterns in active regions, following Hale rule but weaker field indicate systematic eastward tilt.

- Very weak  $B_\varphi$  and  $B_\theta$  in low latitudes, where both components correspond to transverse component in the observations.
- Faint annual "wave" of positive or negative polarity in  $B_\varphi$  and  $B_\theta$  between active region belts.
- Is the instrument sensitivity too low to observe weak transverse fields?
- The annual variations due to the vantage point effect appear already around 50-60° latitude in vector field.





- Inclination: Angle between vector and radial direction, varies from  $0^\circ$  to  $90^\circ$ .

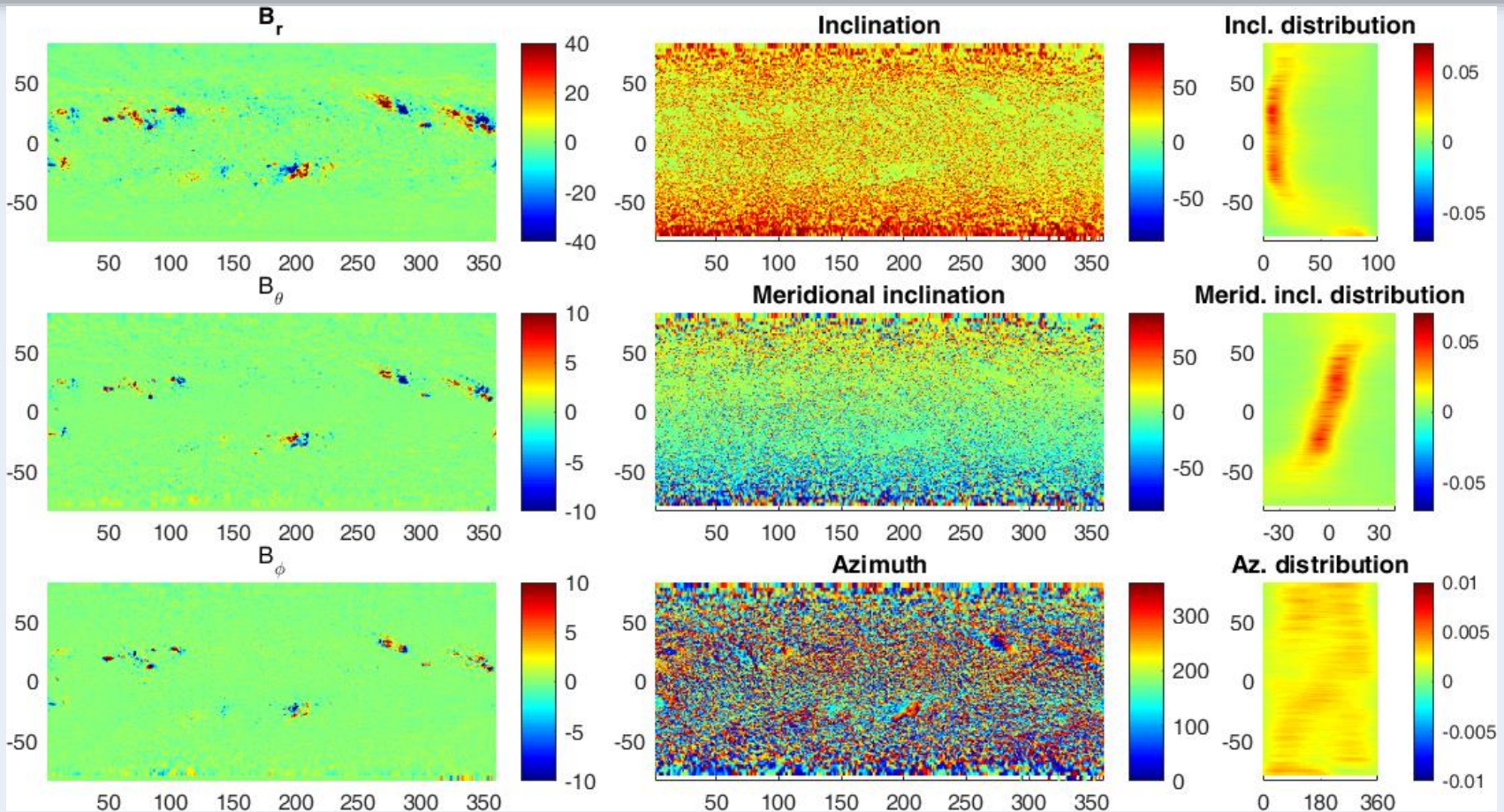
$$I = \arctan\left(\frac{\sqrt{B_\theta^2 + B_\phi^2}}{|B_r|}\right)$$

- Meridional inclination: Angle between  $\hat{r}$  and  $\mathbf{B}$ -vector projection to  $r$ - $\theta$  -plane, varies from  $-90^\circ$  to  $90^\circ$ .

$$I_m = \arctan\left(\frac{B_\theta}{B_r}\right)$$

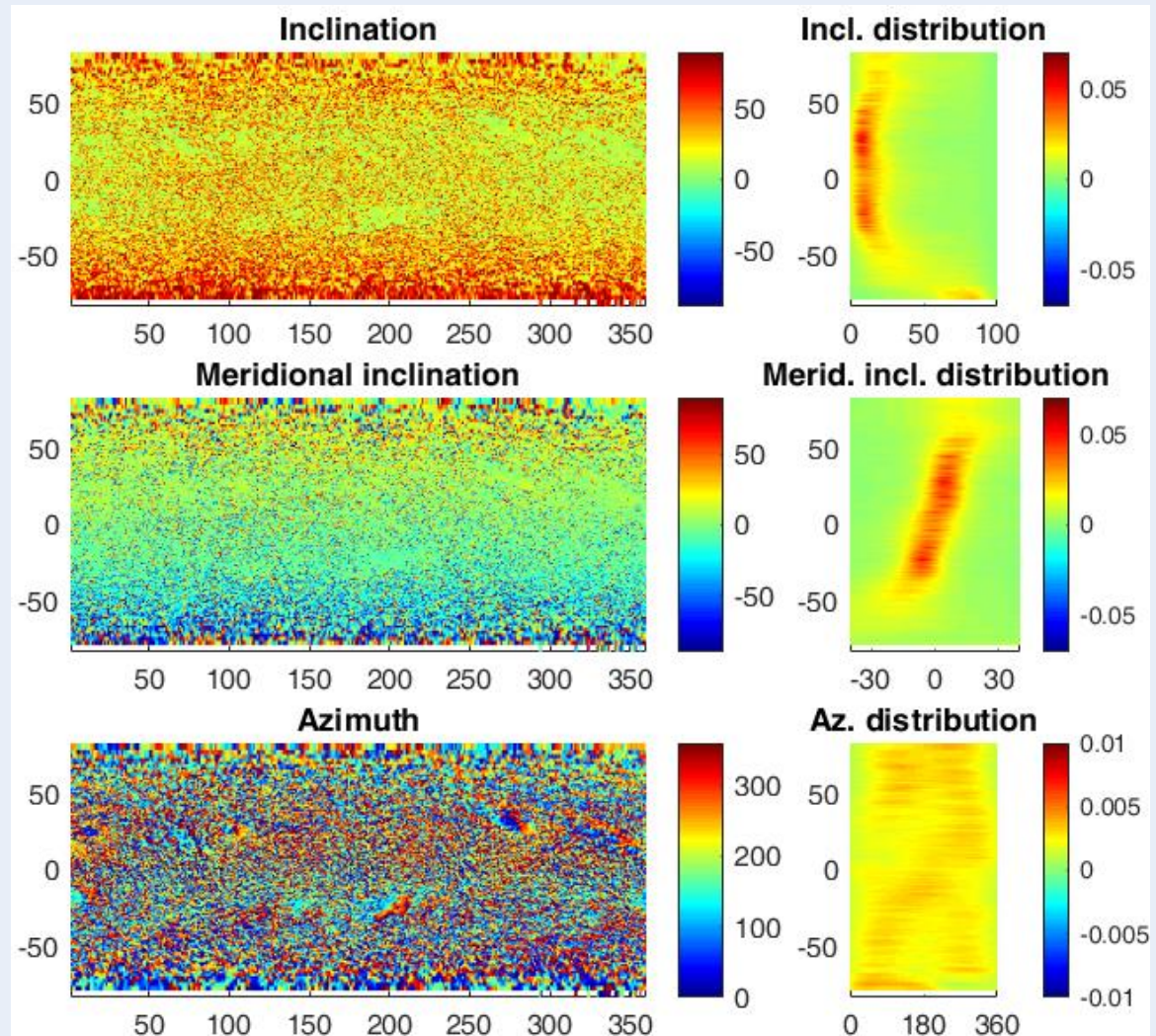
- Azimuth: Angle between  $\hat{\varphi}$  and  $\mathbf{B}$ -vector projection to  $\varphi$ - $\theta$  -plane, zero in the direction of positive  $B_\varphi$  and increases clockwise from  $0^\circ$  to  $360^\circ$ .

$$A = \arctan\left(\frac{B_\theta}{B_\phi}\right) - \left(\frac{B_\phi}{|B_\phi|} - 1\right) * 90^\circ,$$



- Left:  $B_r$ ,  $B_\theta$ ,  $B_\phi$ , Carrington rotation 2100, SOLIS observations
- Middle: Inclination, meridional inclination and azimuth.
- Right: Distributions of angles in latitude bins

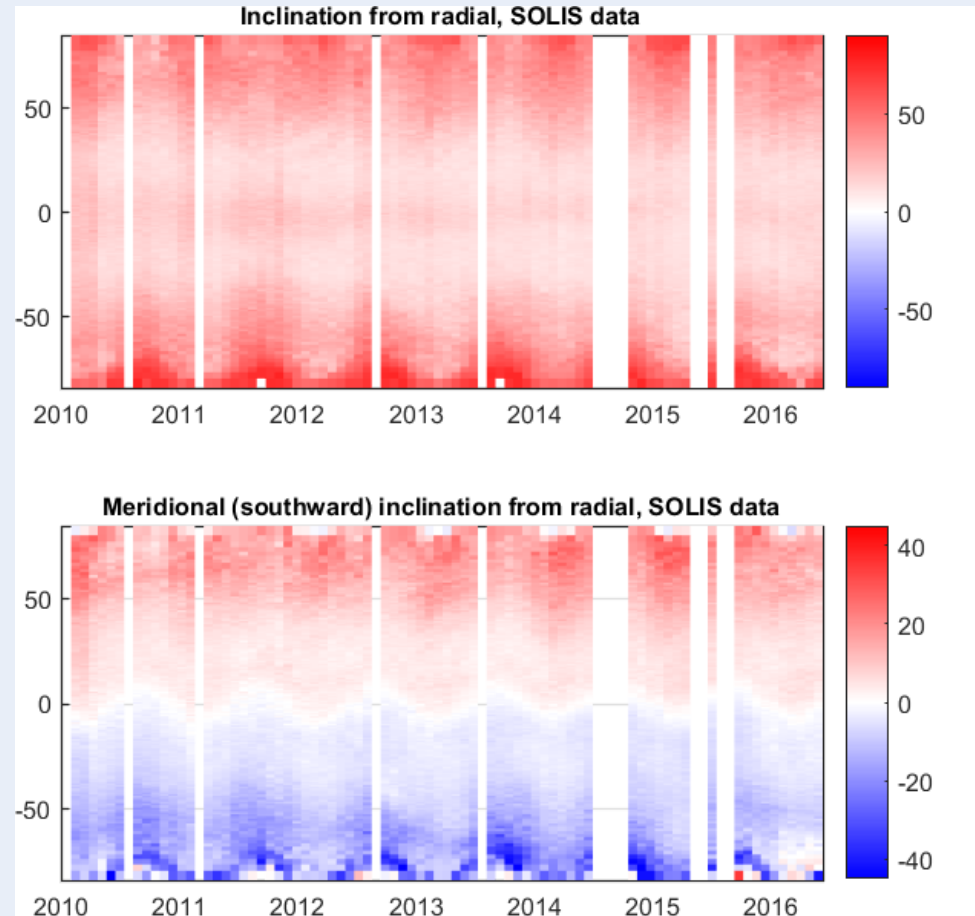
- Field orientation is most radial in active regions.
- Inclination and meridional inclination have obvious latitudinal patterns.
- Field is inclined towards the equator.
- Azimuth distribution is wider and most typical directions are northward and southward.





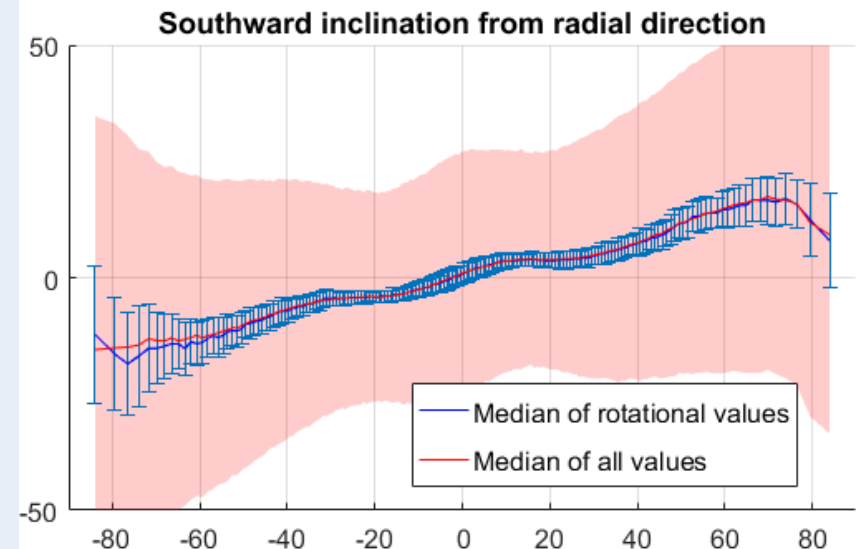
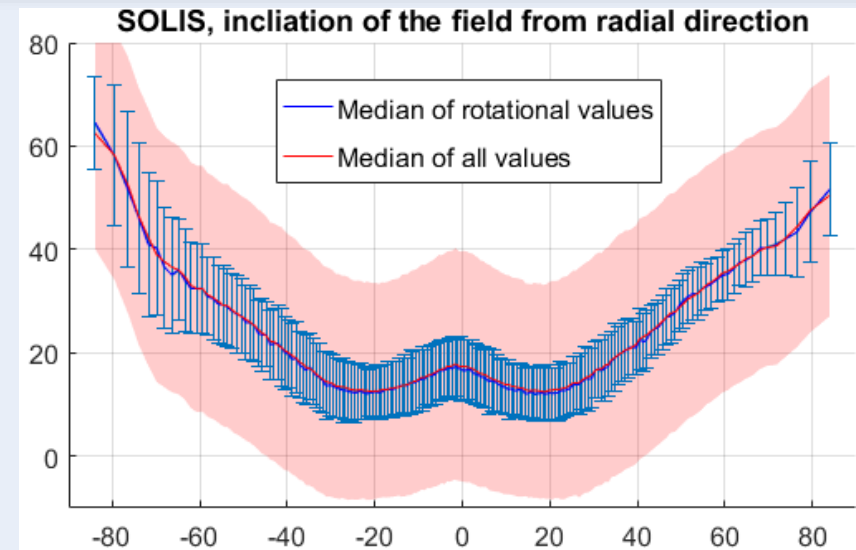
- Longitudinal medians of inclination and meridional inclination.
- Inclination is smallest in mid-latitudes around active regions and increases toward poles and equator.
- Meridional inclination has a systematic pattern of being negative in the south and positive in the north

→ Magnetic field is inclined towards the equator in any latitude.



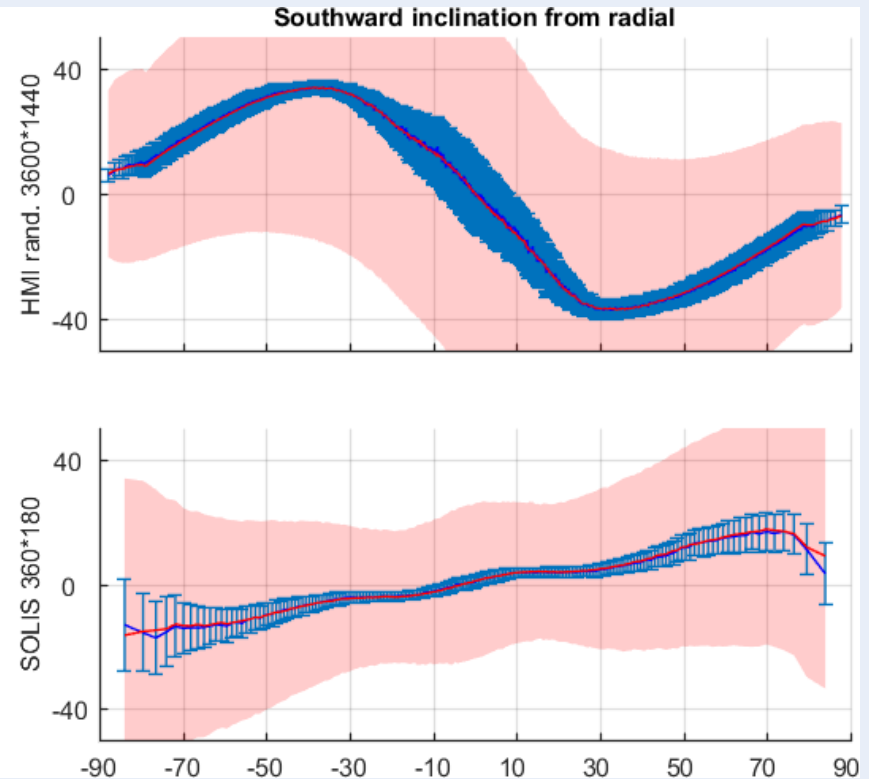
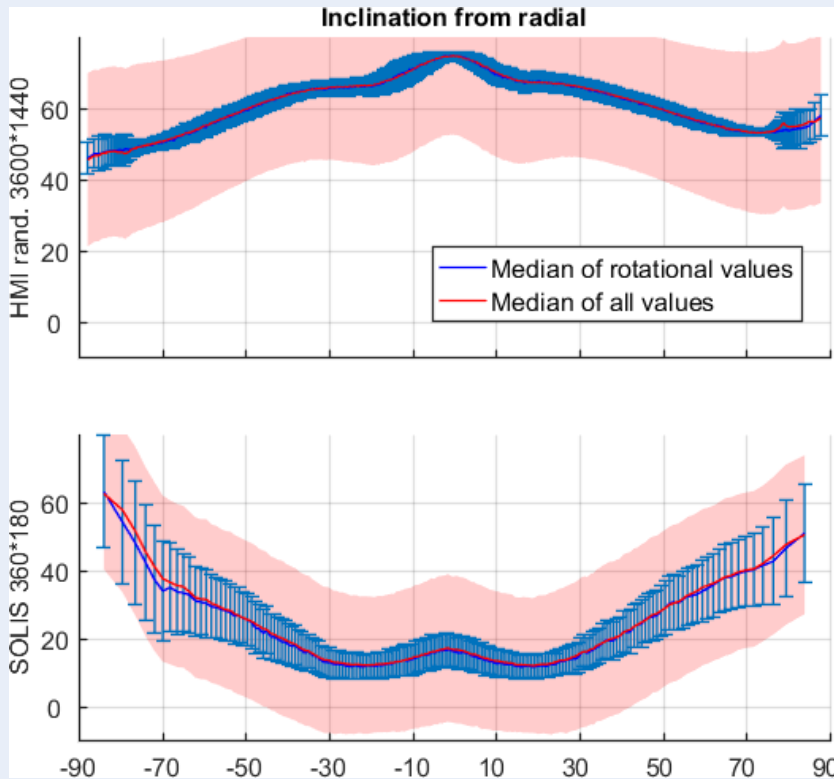


- Average inclination and meridional inclination of the magnetic field based on all SOLIS synoptic vector maps in 2010-2016.
- One sigma error bars.
- Variations are quite large
- Systematic poleward increase of the inclination angle.
- Field is inclined towards equator.



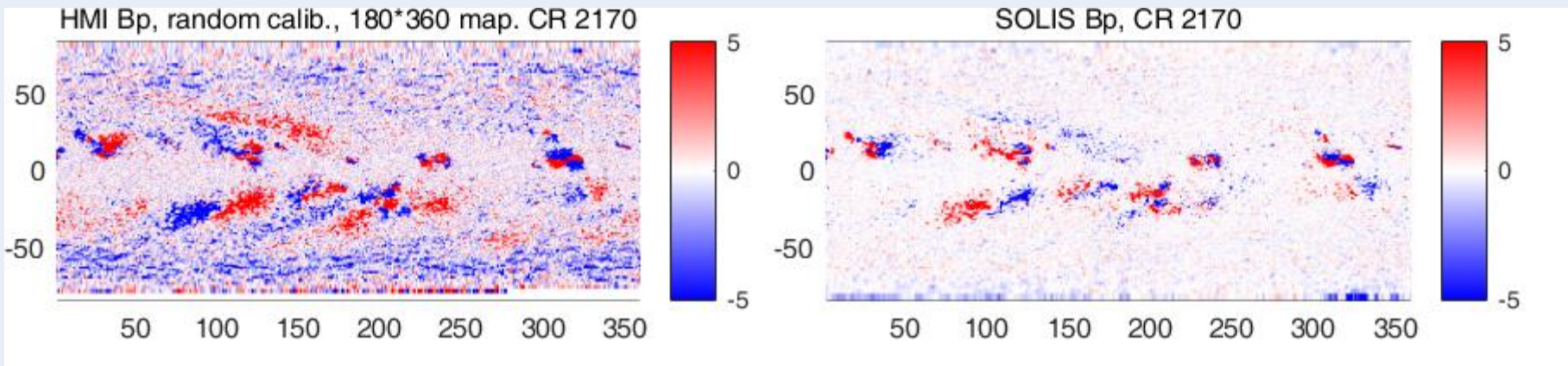
- SOLIS/VSM vector field observations depict that the photospheric magnetic field has a systematic pattern of equatorward inclination.
- This allows to correct derivations of the pseudo-radial magnetic field from line-of-sight observations, radial polar field would decrease significantly.
- However, comparison between SOLIS and HMI lead to unexpected results, two instruments do not agree.

- SOLIS and HMI results do not agree



- HMI shows poleward decrease of overall inclination angle.
- HMI also depicts that magnetic field is in general inclined poleward from radial.

- $B_r$  typically agrees, but,  $B_\theta$  and  $B_\phi$  only agree in strong fields and have opposite signs in two data sets especially in plages.
- This directly leads to opposite results for inclination.





# Alternative method to estimate meridional inclination

- Comparison between observed radial vector field  $B_r$  ("true radial") and pseudo-radial field derived from line-of-sight observations assuming that field is radial.
- If field is radial:

$$B_r = B_r^{PSEUD} = \frac{B_{LOS}}{\cos \lambda}$$

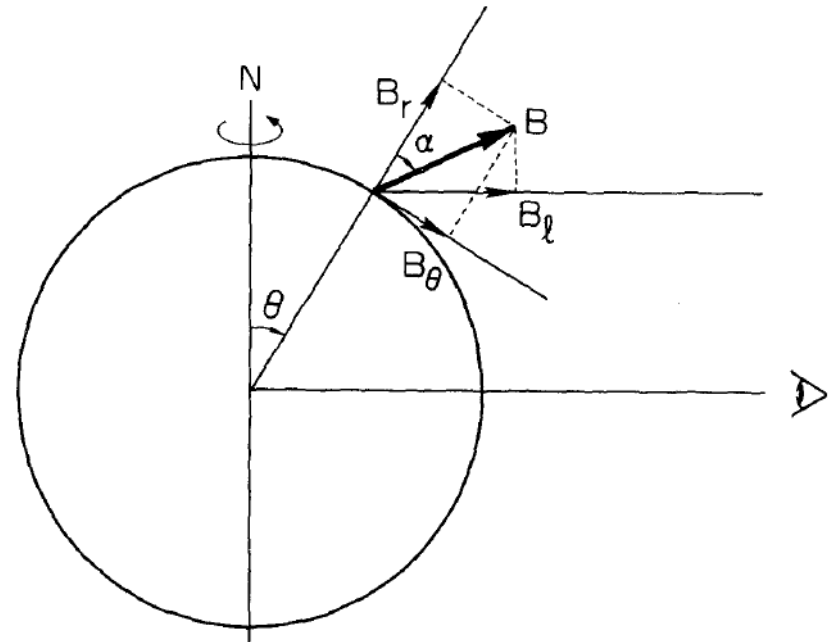
- For equatorward inclination

$$B_r < B_r^{PSEUD}$$

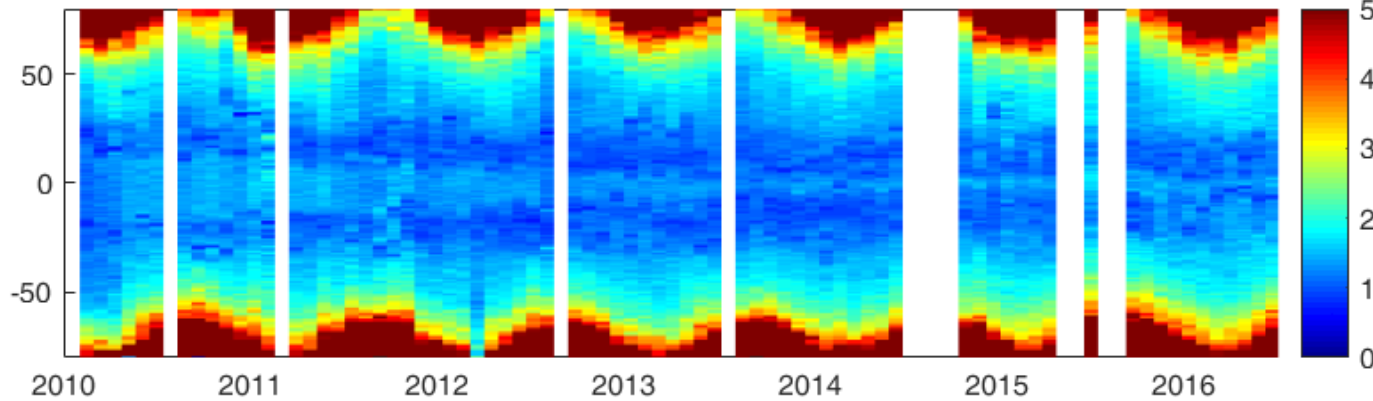
- For poleward inclination

$$B_r > B_r^{PSEUD}$$

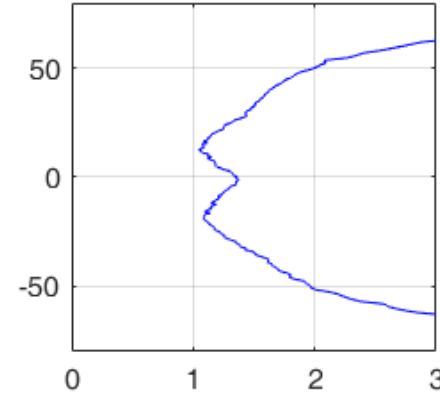
Assuming that the instrumental effects don't play role



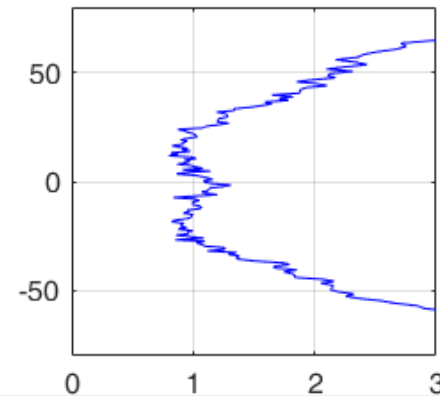
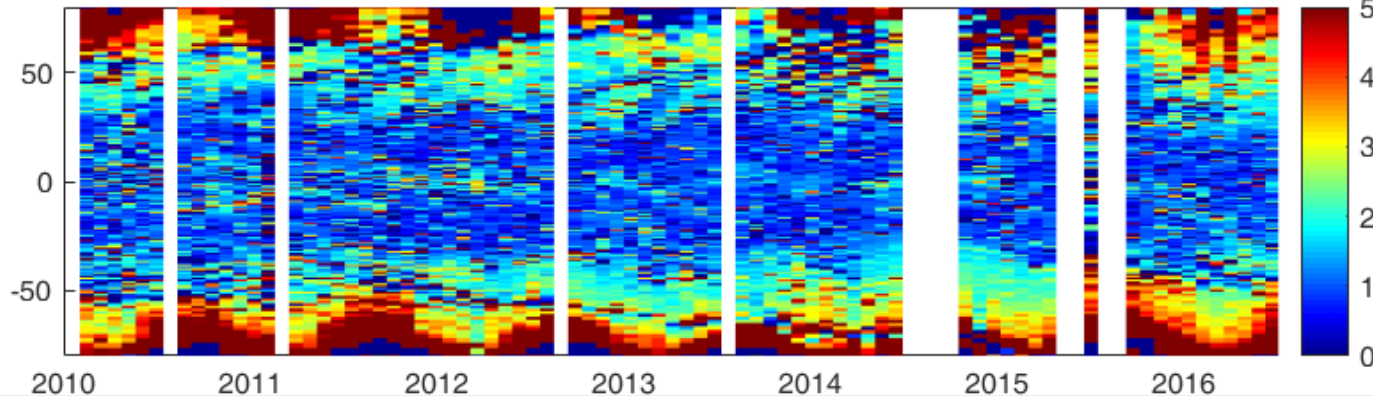
SOLIS, ratio between longitudinal averages of absolute values  $|B_r^{PSEUD}|$  and  $|B_r^{vect}|$



Median

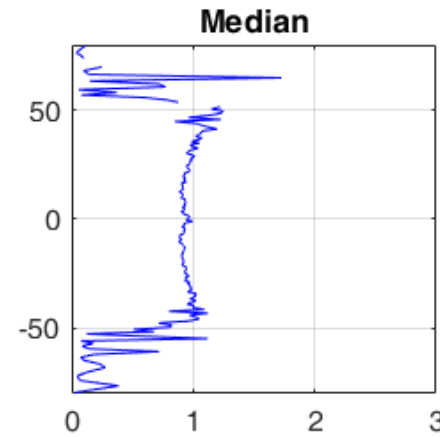
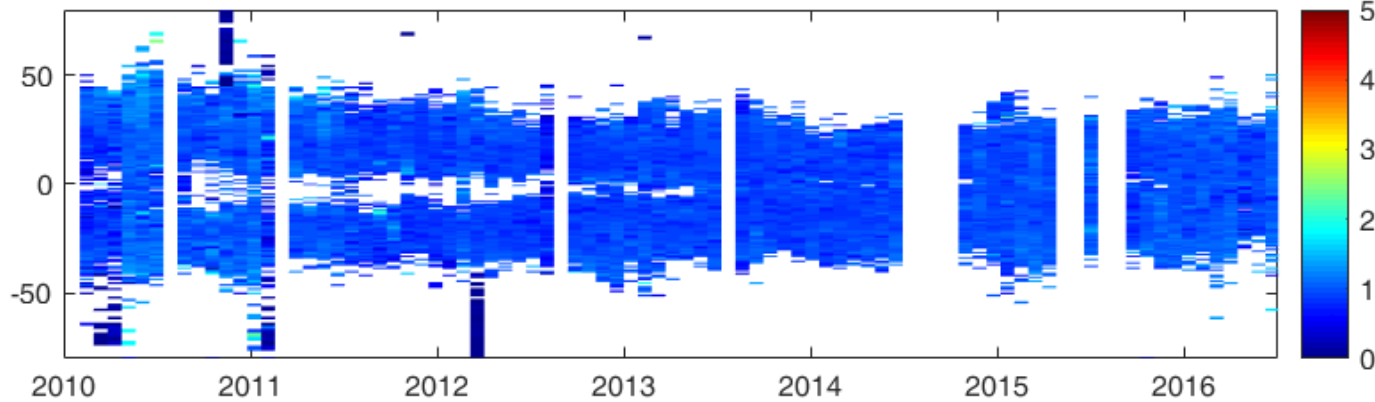


Ratio between longitudinal averages of  $B_r^{PSEUD}$  and  $B_r^{vect}$

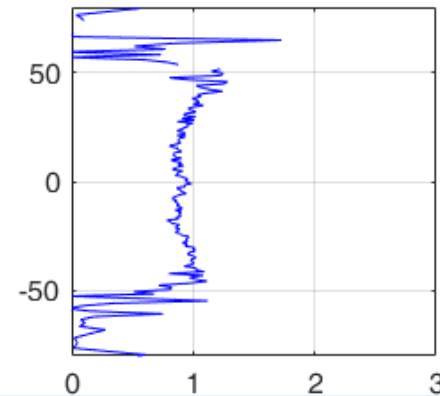
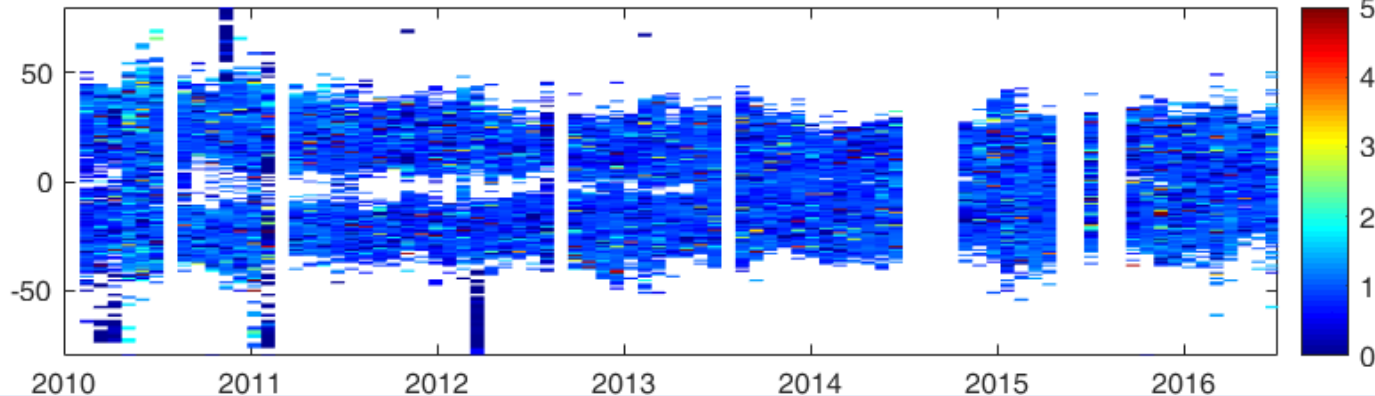


- Vector radial has the same magnitude in active regions, but in the other latitudes pseudo-radial magnitude is larger.
- This would indicate that field inclination is equatorward.

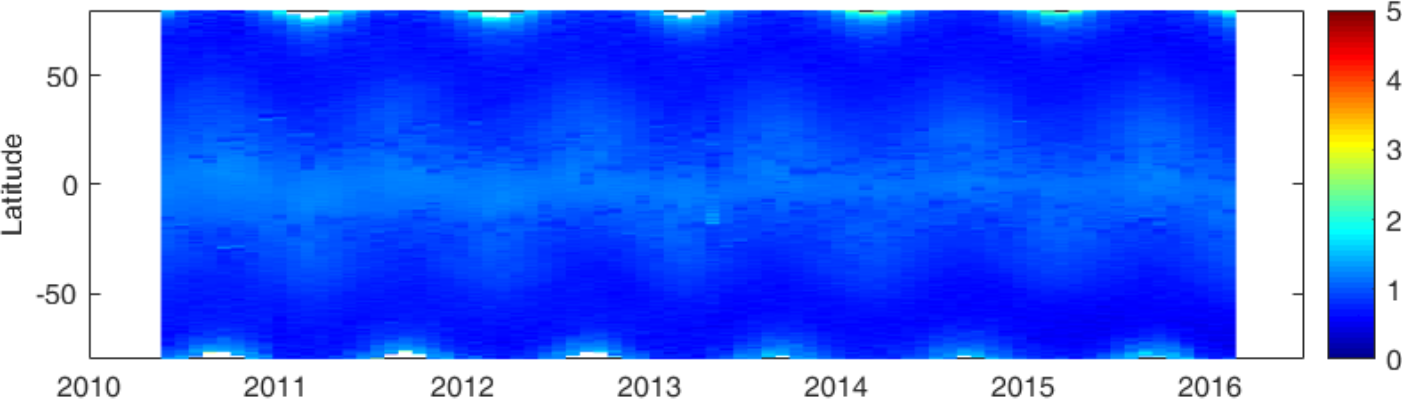
SOLIS, ratio between longitudinal averages of absolute values  $|B_r^{PSEUD}|$  and  $|B_r^{vect}|$



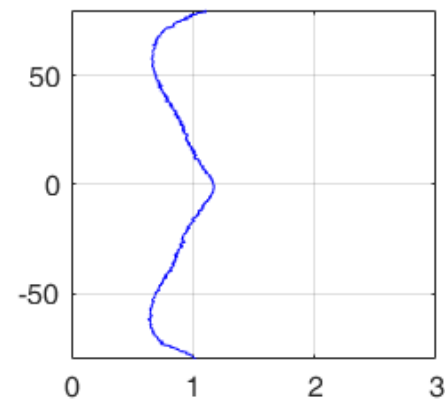
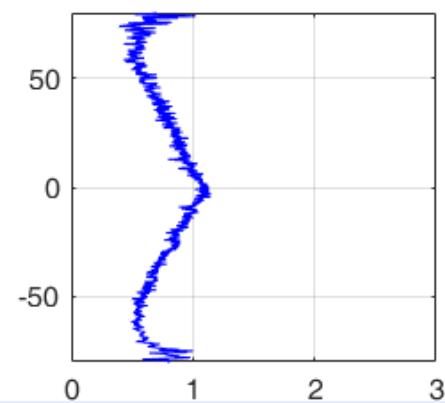
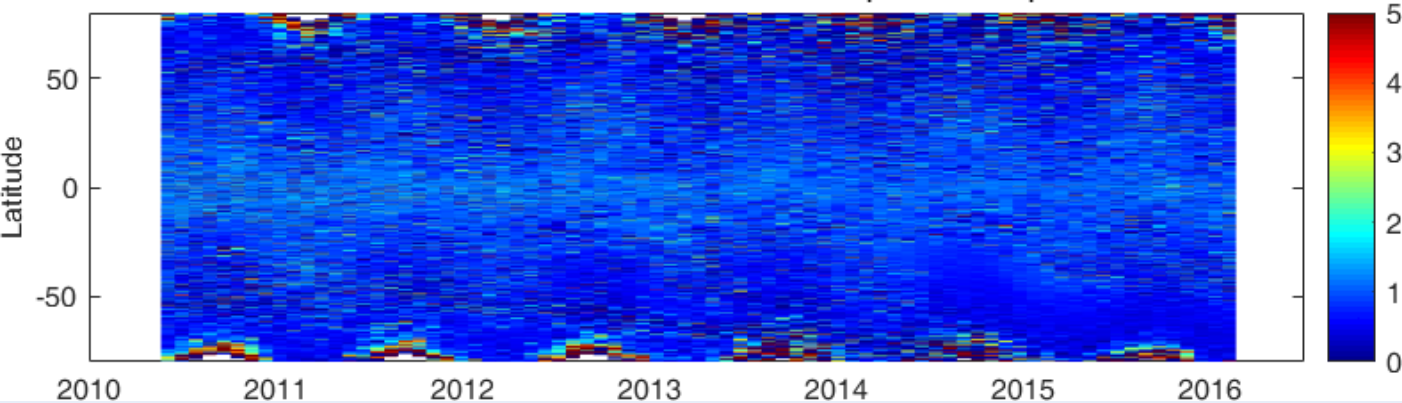
Ratio between longitudinal averages of  $B_r^{PSEUD}$  and  $B_r^{vect}$



- Same as previous slide, but only pixels where  $|B_r|$  exceed one sigma threshold are considered.
- Latitudinal profile of the ratio is now way different.

HMI, ratio between longitudinal averages of absolute values  $|B_r^{\text{PSEUD}}|$  and  $|B_r^{\text{vect}}|$ 

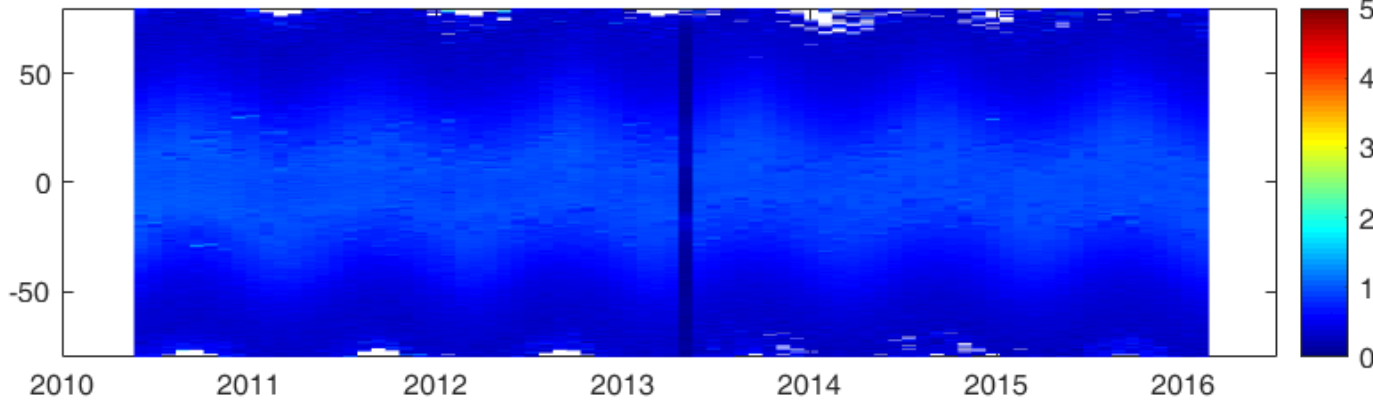
Median

Ratio between longitudinal averages of  $B_r^{\text{PSEUD}}$  and  $B_r^{\text{vect}}$ 

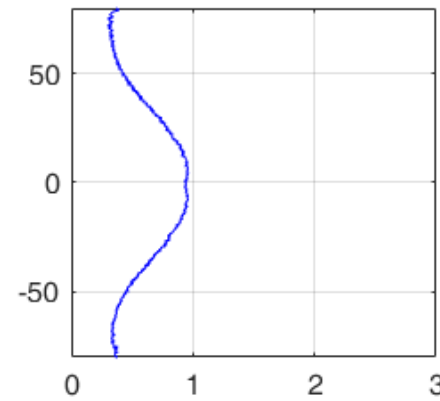
- In HMI vector radial and pseudo-radial have the same magnitude around active regions, but in the other latitudes vector radial magnitude is larger.



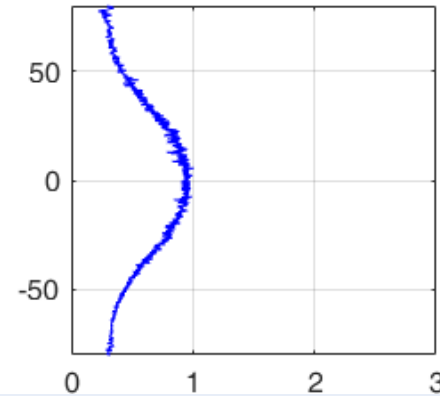
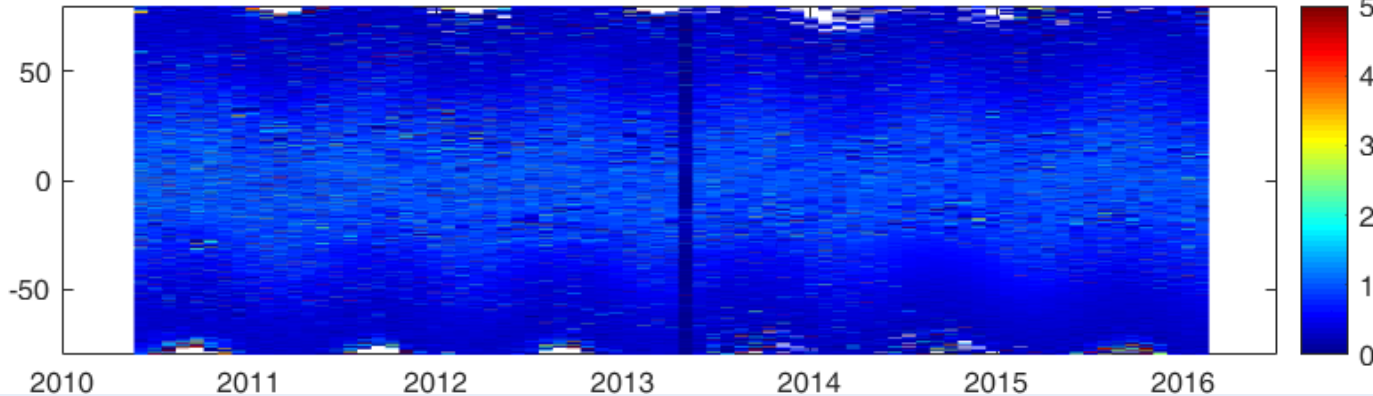
HMI, ratio between longitudinal averages of absolute values  $|B_r^{PSEUD}|$  and  $|B_r^{vect}|$



Median



Ratio between longitudinal averages of  $B_r^{PSEUD}$  and  $B_r^{vect}$



- Same as previous slide, but only pixels where  $B_r$  exceed one sigma threshold are considered.
- Different profile also for HMI when considering only strong fields.

- SOLIS/VSM and HMI vector field observations indicate that photospheric magnetic field is systematically tilted from radial.
- SOLIS depicts that tilt is towards equator and HMI that tilt is towards poles.
- Comparison between vector radial and pseudo-radial fields don't solve this conflict, **both data sets are self consistent.**
- Ratio between vector radial and pseudo radial is non-linear.
- HMI results also depend on resolution and disambiguation method.
- High latitude observations are less noisy and field strength is larger in HMI.
- **Obvious contradiction between two data sets, no final conclusions yet.**